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Characteristics of inherent coupling structure of model climates

Xiuhua Zhu

CEN, University of Hamburg

Bundesstrasse 53, 20146 Hamburg, Germany

xiuhua.zhu@uni-hamburg.de

0049 41173 153

Page 1 of 47

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18 **Abstract**

19 This work proposes a framework to examine interactions of climate modes that are identified as
20 leading EOF modes; their coupling structure is unveiled through correlation analysis and helps
21 constructing a regression model, whose performance is compared across GCMs, thereby providing
22 a quantitative overview of model performances in simulating mode-interaction. As demonstration
23 surface temperature is analyzed for five CMIP5 PiControl simulations. Along with the seasonal
24 land and ocean modes, four interannual modes are identified: Tropical Mode (TM) associated with
25 the Hadley circulation, Tropical Pacific Mode (TPM) characterizing a zonal temperature contrast
26 between the eastern tropical Pacific and the Atlantic-Indian ocean, and two annular modes: Arctic
27 Mode (AM) and Ant-arctic Mode (AAM). All GCMs converge on the following: 1) TM strongly
28 couples with seasonal signals of the previous year; 2) TPM leads TM by 1 year, thus a weaker
29 zonal temperature contrast in the tropics contributes to warming in the entire tropical band one year
30 later; 3) AM weakly couples to TM at a one-year lead, suggesting a colder north pole may contrib-
31 ute to colder tropics. In addition, all GCMs do not support a linear coupling between AAM and
32 TM. The above-learned coupling structure is incorporated to construct an optimum regression
33 model that demonstrates considerable predictive power. The proposed approach may both serve as
34 a useful tool for dynamical analysis and lend insight into GCM differences. Its merit is demon-
35 strated by the finding that different representations of the mean seasonal cycle in GCMs may ac-
36 count for the GCM-dependence of relative contributions of seasonal and inter-annual modes to TM
37 variability.

38 **keywords**

39 Mode interaction, GCM, Hadley Circulation, Trans-basin connection, tropics-subtropics connec-
40 tion

41 **1. Introduction**

42 Global warming is drawing increasing attention largely due to a growing media coverage that often
43 associates disastrous impacts of climate extremes with anthropogenic warming. Prior to such an
44 attribution task, an essential step that has to be undertaken is to separate anthropogenically forced
45 climate signals from natural variability, which is by no means an easy task (Hasselmann 1993;
46 Hegerl and Zwiers 2011; Santer et al. 2011; Lee and Ouarda 2012; Frankcombe et al. 2015). Along
47 this way general circulation models (GCMs) become a powerful tool with increasing importance,
48 but also pose enormous challenges. This concerns model construction, validation, and projection,
49 not only in the technical sense, since it requires knowledge of computer science, mathematics and
50 climate physics, but also in the scientific sense, namely, how faithful GCMs represent key pro-
51 cesses governing the climate system.

52 On the one hand, GCM performances have been extensively evaluated regarding how key climate
53 modes and processes are reproduced, which include among many others the Hadley cell (HC) (e.g.,
54 Hu et al., 2013; Grise and Davis 2020), the Asian Monsoon system (e.g., Mishra et al. 2018; Preethi
55 et al. 2019), ENSO (e. g. Guilyardi, 2006; Chen et al. 2017; Lu et al. 2018), the Atlantic Multide-
56 cadal Oscillation and the Atlantic Meridional Overturning Circulation (Zhu et al. 2006; Drijfhout
57 et al. 2011; Weaver et al. 2012; Zhang and Wang 2013). On the other hand, model comparison has
58 seldom touched how well the interaction between climate modes is reproduced, despite a large

59 collection of observational and model evidences suggesting climate variability continuum (Huy-
60 bers and Curry 2006; Dommenges and Latif 2008; Fraedrich et al. 2009; Lovejoy 2018), which
61 essentially characterizes cross-scale linkages.

62 Take HC as an example. Some of its basic features remain challenging for GCMs. For instance,
63 the thermodynamic structure of the HC shows significant discrepancies between models and rea-
64 nalysis data (e.g., Mitas and Clement 2006). And, although there is a broad agreement between
65 models and observations that the tropics are expanding in the recent decades, no consensus has
66 been reached on the exact magnitude (e.g., Johanson and Fu, 2009; Hu et al., 2013; Grise and Davis
67 2020) and the cause of such a forced expansion (e.g., Nguyen et al., 2015; Allen and Kovilakam,
68 2017; Amaya et al., 2018). In addition, abundant studies reveal that the HC closely interacts with
69 the annual cycle (e.g., Bowman and Cohen 1997; Kang and Lu 2012; Baker et al. 2018), ENSO
70 (e.g., Oort and Yienger 1996; Quan et al. 2004), and the annular modes from both hemispheres
71 (e.g., Previdi and Liepert 2007). Moreover, HC's response to global warming may be highly sen-
72 sitive to the thermal forcing's meridional structure: when the thermal forcing is confined to a nar-
73 row region around the equator, HC contracts, which resembles its response to El-Nino events,
74 whereas a forcing with wider meridional extent produces global warming-like HC expansion (e.g.,
75 Tandon et al. 2013; Baker et al. 2018).

76 All these studies suggest that GCM climates that differ in details of simulated internal climate
77 variability and model dynamics may account for their different responses to global warming (Shep-
78 herd 2014; Staten et al. 2018). However, model-intrinsic coupling/interactions on its own, i.e., ir-
79 respective of the variation of the external forcing, have seldom been discussed, although a deep
80 understanding about the former is prerequisite for learning about the latter, because forced re-
81 sponses are often projected onto the leading intrinsic modes of the climate system (e.g., Hurrell
82 1995; Branstator and Selton, 2009; Zhu et al. 2016).

83 This study attempts to develop a framework devoted to examining interactions of the most influ-
84 ential climate modes in a given climate as such that it shall aid model comparison, particularly
85 regarding how mode-interaction is represented. Within this framework, the following goals are
86 addressed: i) to identify those climate modes that are most fundamental and active in undisturbed
87 GCM climates; ii) to explore how these inherent climate modes couple with each other globally;
88 and iii) to find out whether, and how, the identified coupling structure differs from one GCM to
89 another. The focus is on inherent climate modes that are identified in global surface temperature
90 fields through the EOF analysis, and their interactions are assessed by lead-lag correlation. Based
91 on the identified coupling structure, a suitable regression model is introduced and applied as a
92 model intercomparison tool to provide quantitative measures of mode interaction. A companion
93 analysis on the coupling structure in forced simulations will be discussed separately.

94 This work is organized as follows: section 2 introduces data and analysis method, section 3 presents
95 the complete analysis of the undisturbed simulation of MPI-ESM-MR (PiControl), which serves to
96 guide the construction and selection of regression models in section 4; section 5 presents analyses
97 of PiControl simulations of four additional GCMs and discusses the possible GCM dependence of
98 the coupling structure; main results are summarized in section 6, and section 7 presents discussion
99 and conclusion.

100 **2. Data and Method**

101 Surface temperature (ST) fields of PiControl simulations (forced by preindustrial conditions) from
102 five CMIP5 climate models (listed in Table-1) are analyzed. First, monthly ST time series of year
103 i and month m , $X_{i,m}$, with $i = 1 \dots Y$, $m = 1 \dots 12$, undergo a time-scale decomposition in a mathe-
104 matical sense, $X_{i,m} = \bar{X}_i + X'_{i,m}$, where annual means \bar{X}_i describe variations on interannual scales
105 and monthly deviations $X'_{i,m}$ predominantly reflect the seasonal cycle and its possible change on

106 longer time scales. Hereafter they are referred to as interannual and seasonal components (IAC and
107 SC), respectively. Subsequently, these two components of the global ST fields are subjected to the
108 correlation-matrix based EOF analysis (with area weighting considered).

109 The correlation-matrix based EOF analysis is applied because, in comparison to the covariance-
110 matrix based alternative, it is less influenced by variables with stronger variability. For instance, it
111 is well known that temperature records in polar regions have larger variances than those in lower
112 latitudes, which is referred to as 'polar amplification' in the case of global warming (e.g. Smith et
113 al. 2018). A covariance-matrix based EOF is expected to capture such a *contrast in genuine varia-*
114 *bility* in the first place, which is greatly mitigated by the normalization procedure (temporal anom-
115 ally divided by local standard deviation) prior to the correlation-matrix based EOF. It is expected
116 that, through the normalization, the correlation-based EOF analysis is able to capture structures
117 that are otherwise hidden behind the genuine structure of variances.

118 **3. An exploratory analysis**

119 This section first introduces EOF results of the IAC and SC in the PiControl simulation of MPI-
120 ESM-MR. The first leading EOF mode of the IAC is selected to showcase how the coupling struc-
121 ture (CS) between climate modes is identified.

122 **3.1 Interannual component (IAC)**

123 The first IAC EOF mode (16.2% of the total variance) shows strong loadings predominantly in the
124 tropical band and, in particular, over the tropical ocean; meanwhile, anomalies with an opposite
125 sign occur in the mid-latitude oceans (Figure 1a). Hereafter it is referred to as the tropical mode
126 (TM). The second and third modes (7.5% and 7.2% of the total variance), in contrast to the first

127 mode that accentuates the lower latitudes, are characterized by strong temperature anomalies in
128 either polar region (Figures 1 b-c) and referred to as the Arctic mode (AM) and the Antarctic mode
129 (AAM), respectively. The fourth mode (5% of the total variance) (Figure 1d) is characterized on
130 the one side by warm anomalies over the Eurasia Continent and cold anomalies over the Arctic and
131 Canadian Archipelago and, on the other side, by trans-basin temperature gradients with negative
132 anomalies over the Maritime continent and the tropic Atlantic and warm anomalies over the eastern
133 tropical Pacific. As is soon to be revealed, only the trans-basin temperature gradients in the tropics
134 interact with TM, which forms the focus of this study. Thus it is referred to as the tropical Pacific
135 mode (TPM).

136 The significance of these four EOF modes is inspected with a Monte-Carlo test. Specifically, 50
137 subsets of 300-year ST fields are randomly selected from the entire 1000-year ST fields; each sub-
138 set is subjected to the EOF analysis. It is expected that physically meaningful modes would be
139 persistent and robust and thus retain their rank in the hierarchy. It is found that i) the match between
140 the EOFs of the Monte-Carlo subsets and their counterparts in Figures 1a-d is evidenced by a spatial
141 correlation of at least 0.75 in 75% of the 50 subsets (bottom edge of boxes in Figure S1-a); ii) while
142 TM (TPM) always remains on its first (fourth) place in ranking, AM and AAM switch their ranking
143 positions in some of the subsets, which is consistent with their explained variance being almost
144 equal. More importantly, taking this into account, iii) the relative ranking of the four leading modes
145 is well-kept in all Monte Carlo subsets (Figure S1-b).

146 **Physical embedding of IAC modes**

147 TM describes two essential aspects of the tropical circulation, i.e., the Walker cell and the Hadley
148 cell. It characterizes a zonal contrast in sea level pressure (SLP) between the Indo-Pacific warm
149 pool and the central and eastern tropical Pacific and depicts a negative phase of the Walker cell
150 with sinking motion over the Maritime continent (Figure 1e). Meanwhile, its high loadings occur

151 off the equator (being around 10°S and 10°N in the eastern tropical Pacific, Figure 1a) and corre-
152 spond to the equinoctial pattern of the HC (Figure 1i) as has been depicted in Dima and Wallace
153 (2003). Such an equatorially symmetric structure forms strong contrast with the seasonally-revers-
154 ing solstitial pattern that associates with the monsoons (see their Figures 3-6). Stronger TM
155 (warmer tropics) is linked with a strengthening and contraction of the HC (Figure 1i), which re-
156 sembles the HC response to a narrow forcing centered at the equator (termed as El Niño-like HC
157 contraction in Tandon et al. 2013), in contrast to the global warming like HC expansion. The latter
158 occurs when the thermal forcing with wider meridional extent is applied (Tandon et al. 2013) and
159 has been simulated by most CMIP GCMs under global warming (Lu et al. 2008; Lucas et al. 2014;
160 Vallis et al. 2015).

161 To further substantiate the close connection of TM with warming or cooling over the *entire tropical*
162 *band*, tropical mean surface temperature (averaged between 20°S and 20°N, TMT hereafter) is
163 correlated to the TM principal component and a linear correlation of almost 1 is obtained. Next,
164 their causal relation is examined following Liang (2014). The information flow from TMT to TM
165 is -0.36 and that from TM to TMT is 0.54 (nats per unit time), which indicates that knowledge of
166 TM provides *noise* (positive information flow) to TMT (thus increases its uncertainty), whereas
167 knowledge of TMT decreases TM's uncertainty and thereby increases its predictability. Consider-
168 ing their close-to-1 correlation coefficient, therefore, TMT as the temperature indicator of the entire
169 tropical band is *a defining feature* of TM. In this sense, TM should be viewed as the manifestation
170 of the Hadley circulation on surface temperature.

171 Both AM and AAM are characterized by a weaker pressure gradient between middle and high
172 latitudes (Figures 1f, g) and thus correspond to negative phases of the northern and southern annular
173 modes, respectively (Marshall 2003; Gillet et al. 2006). One interesting feature worth noting is that

174 AM features cold high-pressure anomalies over the Arctic, whereas AAM features warm high pres-
175 sure-anomalies over the Antarctic.

176 In comparison to TM, TPM also features a similar zonal contrast in SLP in the tropics (Figure 1h),
177 but its expression in the meridional mass stream function is considerably weaker (Figure 1j).
178 Meanwhile, its strong loadings in high latitudes (Figure 1d) suggest a possible signal mixture,
179 which more likely occurs to lower-ranked EOF modes, because the lower the rank of one eigen-
180 value, the more modes that are required to be orthogonal to, and the more likely its pattern is dic-
181 tated by mathematical constraints, rather than by physical or dynamical causes.

182 In order to explore what is more essential for the TPM, its loading in high latitudes or the zonal
183 temperature/SLP gradients in the tropics, the EOF analysis is applied to ST fields taken from two
184 subdomains: North of 40°N and the tropical band between 30°S and 30°N. The first leading EOF
185 mode of the two subdomain analyses shows high spatial similarity to AM and TM, respectively,
186 with spatial and temporal correlations of almost 1. The second mode in both cases corresponds well
187 to TPM spatially (spatial correlation coefficients: 0.9 and 0.96) and also temporarily (both with a
188 temporal correlation of 0.69). Therefore, they jointly capture the spatial features of TPM in high
189 and low latitudes (Figure 1d). Their principle components are correlated to that of TM. As is soon
190 to be discussed in section 3.3, TPM leads TM by 1 year with a strong positive correlation coeffi-
191 cient, which, as an indication of mode interaction, is unambiguously captured *only* by the TPM
192 features in the tropics (Figure S2). Therefore, it is the trans-basin temperature/SLP gradient in the
193 tropics that is engaged in the interaction between TPM and TM.

194 Although TM and TPM both show a similar zonal contrast in SLP in the tropical Pacific (Figures
195 1e, h), a discernible characteristic marks their difference: TM is characterized by an overall warm-
196 ing/cooling of the entire tropical band, being the weakest near the Maritime Continent. In contrast,
197 TPM emphasizes a zonal see-saw pattern with warming/cooling in the central and eastern tropical

198 Pacific and cooling/warming in the Atlantic-Indian Ocean (Figures 1a,d, Figures 1k,l), which is
199 still visible at the upper troposphere (Figures 1m,n). Such a see-saw pattern in ST and SLP between
200 the tropical Pacific and the Atlantic-Indian Ocean has been recognized as part of the natural varia-
201 bility in a prediction system and can be considerably better predicted than ENSO (Chikamoto et al.
202 2015; Kosaka 2018).

203 **3.2 Seasonal component (SC)**

204 The first two SC EOF modes account for 74.1% and 14.6% of the total variance (not shown). In
205 order to seek a decomposition that further eases physical understanding, factor analysis is per-
206 formed to rotate these two EOFs ('rotatefactors' in Matlab). Two patterns with almost equal contri-
207 butions to the total variance (45% and 44%) are obtained, both showing clear inter-hemispheric
208 temperature contrast. The first mode has strong loadings prevailingly over land, while the second
209 one shows strong loadings mainly over the ocean (Figures 2a-b), thus hereafter they are named as
210 the land mode (LM) and the ocean mode (OM), respectively.

211 In the course of a year, LM peaks in July and reaches its low in January, while approximately one
212 month later OM reaches its high (low) in August-September (February-March) (Figure 2c). This
213 one-to-two month delay results from the large difference in effective heat capacity between the
214 ocean and the land.

215 The typical monsoon regimes deserve some special consideration here. The interplay between the
216 two SC modes indicated by their phase difference (Figure 2c) demonstrates vividly how LM and
217 OM work with and against each other in different months of the seasonal evolution. For instance,
218 the earliest Asian monsoon onset (withdrawal) is reported to occur in May (September) over the
219 Indian Peninsular and the Indo-China Peninsular (Wang and LinHo 2001). Figure 2c suggests that
220 the early occurrence of monsoon signals in these regions may mainly result from LM that increases

221 its contribution considerably in May (compared with its almost zero contribution in April); in June-
222 August, the dominance of control shifts from LM to OM while both are still sharing the same sign
223 and further enhance the monsoon. The subsequent withdrawal in September mainly reflects the
224 sharp decrease of LM from August to September while OM remains more or less stable. The re-
225 constructed climatological monthly ST field is presented in the supplement (Figure S3-a).

226 **3.3 Coupling structure (CS)**

227 The focus of this section is to examine how the first leading IAC mode (TM) interacts with both
228 SC modes and IAC modes by calculating the lead-lag correlation between the corresponding prin-
229 ciple components . Therefore, the analysis here is restricted to linear relationships.

230 **I. TM statistics**

231 The quantile-quantile plot (QQ-plot) suggests that TM exhibits no systematic deviation from the
232 normal distribution (Figure 3a), which is also supported by various statistical tests for normality
233 at 5% significance level (e.g. the Jaque-Bera test and the Anderson-Darling test, hereafter referred
234 to as JB and AD test).

235 **II. Cross-correlations**

236 **TM-IACs coupling:** The strongest correlation is found between TM and TPM (the fourth IAC
237 mode) when the latter leads the former by 1 year (Figure 3b). A further cross-spectrum analysis
238 reveals strong coherence between the two at frequency of around 4, 5 and 7 years that is character-
239 istic of ENSO periodicity (not shown). Therefore, TM and TPM jointly describe the tropical circu-
240 lation that is strongly imprinted by ENSO dynamics. In comparison, the correlation between TM
241 and the other two modes (AM and AAM) is much weaker, in particular, the TM-AAM correlation
242 hardly exceeds the 95% confidence levels.

243 **TM-SCs coupling:** The cross-correlation between TM and SC modes at lag -1 (SC modes lead
244 TM by 1 year) is distinctly different from that at lag 0 and 1. The following details are noted:

245 i) The LM- and OM-TM correlations at lag -1 follow approximately a monotonic evolution with
246 comparable magnitudes, i.e., the OM-TM correlation evolves from positive to negative values
247 and has its positive (negative) extrema in January (December), while the LM-TM correlation
248 shows a similar pathway but with opposite signs.

249 ii) The TM-OM correlations at lag 0 and 1 are oscillatory swinging from its negative to positive
250 phase. The intensity extrema occur around April and October and not at the beginning and end
251 of the year, as noted for lag -1 when it varies monotonically with time.

252 iii) The TM-LM correlation decreases monotonically (from positive to negative) at lag 1 and al-
253 most mirrors the pattern at lag -1, whereas at lag 0 positive correlation is found near the middle
254 of the year (around June) and weak negative correlation in September-October. Another note-
255 worthy feature is that the LM-TM correlation at lag 0 is considerably weaker than that of the
256 OM, but both are of comparable magnitude at other lags.

257 The coupling of TM with SC modes and IAC modes at lag -1 (when they lead TM by 1 year) guides
258 us to use this information to introduce a regression model diagnostic for TM, which is presented in
259 the next section.

260 **4. Regression model and its predictive quality**

261 This section sets out in search of a combination of variables (principle components of the four IAC
262 modes and two SC modes) to construct a regression model of TM with the highest explanatory
263 power measured by Bayesian information criterion (BIC); the adjusted r-squared is calculated as a
264 complementary measure.

265 It is worth pointing out that BIC is selected because it measures goodness of fit, whereas another
266 information measure, the Akaike Information Criterion (AIC), which is originally derived from a
267 predictive view point, is more suitable for measuring predictive accuracy of a model to predict new
268 data. For an in-depth explanation on the differences between AIC and BIC, readers are referred to
269 Sober (2002) and Shmueli (2010).

270 **4.1 Regression model**

271 The regression model of TM is expressed as follows:

$$272 \quad TM(t) = c + IAC^+(t - 1) + SC^+(t - 1, m) + \epsilon \quad (1)$$

273 in which c is a constant, ϵ is white noise with zero mean, IAC^+ denotes the principle components
274 of inter-annual modes and SC^+ denotes those of the seasonal modes in month m of year $t-1$. Written
275 in full expansion one obtains

$$276 \quad IAC^+(t - 1) = a_1 * TM(t - 1) + a_2 * AM(t - 1) + a_3 * AAM(t - 1) + a_4 * TPM(t - 1)$$

277 (2)

$$278 \quad SC^+(t - 1, m) = b_1 * LM(t - 1, m) + b_2 * OM(t - 1, m) \quad (3)$$

279 If only the first term on the right side of equation 2 is considered and the SC^+ term set to zero,
280 equation 1 represents an AR (1) model of TM.

281 The task here is to find out a combination of various (or all) modes that appear in equations 2 and
282 3 to achieve the maximum explanatory power. BIC serves as the selection criteria for the best
283 regression model; the adjusted r-squared is also calculated as a supplementary check. Two SC
284 modes are regarded as being inseparable because only the two together can closely capture the full
285 seasonal cycle.

286 The regression model selection is conducted in two steps:

287 **Step-1:** to examine the relative contribution of seasonal and inter-annual variability to the variabil-
288 ity of TM (keeping only SC^+ or only IAC^+ in equation 1 in their full expansion as in equations 2
289 and 3). For comparison, the full regression model (SC^+ plus IAC^+ in full expansion) is also as-
290 sessed. When only SC^+ is considered, the model performance is examined for each month, only
291 the month with top performance is presented, which turns out to be December (thus $m=12$); this
292 also applies to the full model.

293 The top performance (with the lowest BIC value) among the three regression models evaluated
294 here turns out to be the full regression model (gray bar in Figure 4a). One also learns that the IACs-
295 only regression model, in comparison to the SCs-only option, has a higher r-squared value and a
296 lower BIC (BIC: 2403 vs. 2702; r^2 : 37% vs. 15%), suggesting a higher contribution of inter-annual
297 modes to TM variability.

298 **Step-2:** to find the most relevant IAC modes for the regression model. Both SC modes and TM
299 itself (term 1 in equation 2) are included by default; subsequently, all possible combinations of the
300 remaining three IACs are added into the default model and their performances are compared. Note
301 that the full model (SC^+ plus IAC^+ in full expansion) is listed in the last column of Figure 4b (and
302 as well in Figure 4a).

303 The best performance is delivered by the regression model that excludes AAM (gray bar in Figure
304 4b), which is consistent with the weak and insignificant AAM-TM correlation in Figure 3b. This
305 final optimum model, in comparison to the full regression model, has a further reduced BIC value
306 (by 12), whereas the adjusted r-squared values of both options are almost identical and do not help
307 distinguish them further.

308 **4.2 Predictive quality**

309 A statistical model with high explanatory power is often assumed to show reasonable prediction
310 quality, although it should be emphasized that the regression model being selected in the previous
311 section is because of its high *explanatory power* (measured by BIC), not due to its *prediction skill*
312 that is better measured by AIC. In fact, when using AIC as the selection criteria, the top perfor-
313 mance regression model would be instead the full model (SC^+ plus IAC^+ in full expansion in equa-
314 tion 2, last column in Figures 4a, b), because AIC tends to select more general models when n is
315 large (here $n=1000$) (Burnham and Anderson 2004).

316 To assess the prediction quality, the 1000-yr data is divided into two equal parts, the first 500 years
317 as the training data, and the second half as holdout/validation data. Model parameters are deter-
318 mined from the training data (see Table 2) and kept constant for predicting the second 500 yrs.

319 The parameters determined from the training period lie closely to those estimated from the entire
320 period and well within the 95% confidence intervals. The prediction shows a correlation of 0.74
321 with the target holdout data (Figure 5), which lies well above 0.47 that is achieved by an AR (1)
322 model of TM.

323 **5. GCM dependence**

324 To explore whether the coupling structure (CS) revealed above is GCM dependent, this section is
325 devoted to analyzing ST fields of PiControl simulations of additional four GCMs listed in Table 1.
326 Given that the four IAC modes in MPI-ESM-MR (Figures 1a-d) correspond well to well-known
327 climate processes with their characteristic spatial domains, they are used as orthogonal bases, onto

328 which (compressed) ST fields from these four GCMs are projected, which allows *only* the infor-
329 mation of these physically meaningful modes to be extracted; the resulting temporal loadings are
330 then treated as principle components, from which the explained variances are calculated.

331 Prior to the projection, monthly ST fields are first interpolated onto the T63 grid employed in MPI-
332 ESM-MR; their inter-annual parts are compressed (or filtered) by keeping only the first k EOF
333 modes, k is the effective number of spatial degrees of freedom, estimated following Fraedrich et al.
334 (1995) and Bretherton et al. (1999). The reconstructed fields with the leading k modes are then
335 considered for projection. A brief summary on variance reduction that ensues from data compres-
336 sion and projection is presented in Figure S4.

337 The following results are noted:

338 1) **Normality test:** The null hypothesis that TM follows a normal distribution is rejected in NCAR-
339 CCSM4 and GISS-E2-R (Figures 6a, j) but not in IPSL-CM5A-LR and MRI-CGCM3 (Figures 6d,
340 g) at a 5% significance level ($P < 0.01$, in AD and JB test).

341 2) **TM-IACs coupling:** The TM-TPM coupling at lag 1 that is observed in MPI-ESM-MR (positive
342 correlation when TPM leading, Figure 3b) is found in all GCMs (yellow line, Figures 6 b, e, h, k)
343 but being the weakest in IPSL-CM5A-LR (close to 0.2); the TM-AM coupling that is manifested
344 as negative correlation at lag 1 in MPI-ESM-MR (blue line, Figure 3b) is also found in all GCMs
345 but barely exceeding the 95% confidence levels in MRI-CGCM3 and GISS-E2-R (blue line, Fig-
346 ures 6b, e, h, k); the TM-AAM correlation differs from GCM to GCM being in general rather weak
347 (red lines, Figure 6b, e, h, k).

348 3) **TM-SCs coupling:** MRI-CGCM3 differs greatly from the other three GCMs and is discussed
349 separately shortly afterwards. The other three GCMs share with MPI-ESM-MR the following com-

350 mon features: i) TM closely correlates to the seasonal LM (OM) that increases (decreases) monot-
351 onously at lag -1 (when SC modes leading by 1 year) with maximum intensity in December; ii)
352 The evolution pattern at lag -1 is mirrored at lag 1, in particular, in the case of the seasonal LM; iii)
353 at lag 0, the correlation between TM and the seasonal LM is generally weaker than that with the
354 seasonal OM; furthermore, the TM-OM correlation at lag 0 and lag 1 distinguishes itself from that
355 in the preceding year with an oscillatory behavior, with maximum intensity in early spring and
356 September-October (instead of in December).

357 In comparison, the TM-SCs correlation is not well established in MRI-CGCM3 at all three time
358 lags (Figure 6i), suggesting a rather limited role of seasonal components in influencing TM varia-
359 bility in this GCM. In NCAR-CCSM4 and GISS-E2-R the TM-SCs correlation at lag 1 (SC modes
360 leading by 1 year) is much stronger (~ 0.6 for TM-OM and 0.4 for TM-LM in December) than that
361 in IPSL-CM5A-LR, which hints at a larger contribution of the seasonal modes in these two model
362 climates.

363 The results above are further confirmed in the regression model selection process: i) In IPSL-
364 CM5A-LR and MRI-CGCM3, regression models that comprise only SC modes as explanatory
365 variables ('SCs') have lower r-squared values and larger BIC than those comprising only IAC
366 modes ('IAC(1-4)') (Figures 7b,c), suggesting a dominant contribution of IAC modes to TM vari-
367 ability. In contrast, ii) in NCAR-CCSM4, these two regression models ('SCs' and 'IAC(1-4)') have
368 almost equal BIC and r-squared values, thus they make comparable contributions, whereas iii) in
369 GISS-E2-R, seasonal modes ('SCs') make considerably larger contributions than IAC modes to
370 TM variability. Predictions made by these selected models are presented in Figure S5.

371 What is common among all GCM climates is that the third IAC mode (AAM) does not help to
372 explain TM variability, at least not in linear terms with a one-year lead. In all GCMs except GISS-

373 E2-R, the optimum regression models all comprise the first, second, and fourth IAC modes (TM,
374 AM, and TPM), whereas in GISS-E2-R only TM and TPM are included.

375 **6. Summary**

376 This study has proposed an approach to identify mode interaction, which in a way looks for com-
377 mon characteristics from different GCM climates in undisturbed PiControl simulations. Climate
378 modes are identified by means of the EOF analysis that is applied to the inter-annual and monthly
379 components of the ST field (IAC and SC), respectively. The lead-lag correlation between these
380 modes serves as an indicator of mode interaction and subsequently helps to develop a regression
381 model hierarchy that describes their interaction in a linear format. The systematic selection process
382 for the optimum regression model not only provides an objective perspective for understanding
383 climate dynamics but also makes it possible to quantitatively compare the coupling structure in
384 different GCMs thereby providing hints for model improvements.

385 The correlation-matrix based EOF has been employed to capture patterns that are otherwise hidden
386 behind the genuine variance contrast that is characteristic of the Earth climate, namely, i) on inter-
387 annual time scales, large ST variation in high latitudes contrasts weak variability in the tropics, and
388 the central and eastern tropical Pacific is loaded with considerably stronger variability than the
389 surrounding oceans (Figure S3-b); ii) on a seasonal scale, the temperature variability over high
390 latitude continents is much stronger than the rest of the world, particularly, in the northern Hemi-
391 sphere (Figure S3-c). Owing to the correlation-matrix based EOF analysis, the leading four IAC
392 EOF modes capture intrinsic climate modes that essentially manifest the equator-to-pole tempera-
393 ture gradient of the Earth climate (TM, AM, and AAM) and the zonal thermal contrast in the tropics
394 (TPM). These modes correspond closely to well-known climate processes: i) TM characterizes a
395 weaker (stronger) Walker cell and a stronger (weaker) Hadley circulation on interannual time

396 scales. Being nearly symmetric about the equator, TM differs greatly from the cross-equatorial
397 pattern of the Hadley circulation that associates with the monsoon systems (e.g. Dima and Wallace
398 2003); ii) AM and AAM correspond to the northern and southern annular modes, respectively; iii)
399 TPM emphasizes the see-saw pattern between the eastern tropical Pacific and the Atlantic-Indian
400 Ocean, for which the signals in the tropical Atlantic are essential. Such a pattern closely resembles
401 the pan-tropical dipole-like SST variability that is induced by temperature anomalies in the Atlantic
402 (Li et al. 2016) and exhibits higher predictability than ENSO (Chikamoto et al. 2015; Kosaka 2018).

403 It is worth stressing that it shall not be taken for granted that this set of modes necessarily comes
404 out so clearly — it is certainly not the case, if the covariance-matrix based EOF had been used.
405 Therefore, *being able to identify these most fundamental climate modes at once* is a vivid demon-
406 stration of the capability and usability of the proposed analysis approach. It is simple but powerful
407 and this merit should be acknowledged accordingly.

408 Since these four interannual modes in the MPI-ESM climate are (geographically) cleanly separated,
409 they serve as orthogonal bases, onto which the ST fields of other GCM simulations are projected.
410 Such a projection allows *only* the information of the corresponding *physical* modes to be extracted
411 so that the resulting interaction is less contaminated by mode mixing.

412 Factor analysis in combination with the EOF analysis captures a stable pair of seasonal modes (LM
413 and OM), with almost equal contributions to the seasonal cycle. The one-to-two month phase lag
414 of OM behind LM results from the seasonal variation of the incoming solar radiation and the dif-
415 ference in effective heat capacity between land and sea. Unlike the typical assumption of being
416 stable and self-repeating, the seasonal cycle captured by SC modes is not constant in time (gray
417 spread in Figure 2c) and thus suggest a modulated seasonal cycle even in undisturbed climates,
418 which has proven to be essential for ENSO's seasonal phase locking (Wu et al. 2008; Hamlington
419 et al. 2019).

420 The following groups multi-model results into two categories:

421 **Similarities**

422 i) All five GCMs simulate a stronger TM (warmer tropics, stronger and contracted equinoctial
423 cells of the HC and a weaker Walker cell) being preceded by a stronger TPM (warmer tropical
424 Pacific and colder Atlantic-Indian ocean) by one year;

425 ii) Most GCMs tend to agree on a close but weak association between AM and TM: a stronger
426 AM (colder north pole) is associated with a weaker TM (colder tropics) one year later. This
427 correspondence is also manifested by a negative coefficient for AM ($b_2 < 0$) in statistical models
428 (even though AM is not included into the optimum statistical model in GISS-E2-R in the end).

429 iii) AAM does not seem to be important for TM variability in all GCM climates, at least not in a
430 linear format with a one-year time lag.

431 iv) All GCMs simulate strong coupling between seasonal modes and TM, which shows time-var-
432 ying features.

433 When the former leads the latter by 1 year (lag -1), the correlation evolves monotonically in
434 the annual course. Specifically, the OM-TM correlation turns from positive to negative values
435 and has its positive (negative) extrema in January (December), while the LM-TM correlation
436 follows a similar pathway but with opposite signs. The above feature differs completely from
437 that at lag 0 and lag 1, in which the TM-OM correlation evolution is rather oscillatory. Another
438 interesting feature is that the TM-LM correlation at lag 1 almost mirrors its seasonal evolution
439 at lag -1.

440 **Differences**

- 441 1) TM follows a normal distribution in three out of five models (IPSL-CM5A-LR, MRI-CGCM3,
442 MPI-ESM-MR);
- 443 2) The relative contribution of the seasonal and inter-annual modes to TM variability varies
444 greatly from GCM to GCM: in IPSL-CM5A-LR, MRI-CGCM3 and as well MP-ESM-MR, the
445 SC contributes much less than the IAC to TM variability, while GISS-E2-R simulates the op-
446 posite and NCAR-CCSM4 simulates similar contributions from SC and IAC.

447 **7. Discussion and conclusion**

448 This study has focused on identifying the coupling structure that characterizes internal climate dy-
449 namics and proposed a quantitative approach to comparing the coupling structure in different
450 GCMs. This approach makes it possible to obtain an overview on whether and how the GCM-
451 simulated coupling structure converges or differs across models. It is unfolded in three steps, first,
452 the most fundamental and active climate modes are identified for model climates by a correlation
453 matrix-based EOF analysis, second, the coupling structure of these climate modes is identified by
454 a lead-lag correlation analysis; third, the revealed correlation relationship is used to develop an
455 optimum regression model that enables a quantitative comparison across models. The thereby
456 gained knowledge may be envisaged as a step towards a follow-on targeted in-depth investigation
457 into the underlying physical processes and the factors that lead to model convergence/dependence.

458 The results reported in this study are from GCM control simulations under preindustrial conditions.
459 On the other hand, similar analyses of the ERA20C reanalysis data also reveal the main coupling
460 characteristics reported here (not shown). For instance, after carefully removing the transitional
461 trend from the reanalysis data, TM and TPM as the dominating modes in the tropics, together with
462 AM and AAM, form the first four leading interannual (correlation-matrix based) EOF modes,
463 which account for 16%, 8%, 7% and 5% of the total variance, respectively (36% in total); TPM

464 shows its highest positive correlation with TM at a one-year lead; and the lead-lag correlation be-
465 tween both SCs and TM highly resembles that in Fig. 3c.

466 Therefore, the fact that all five GCMs simulate a strong TPM-TM coupling on inter-annual time
467 scales provides an encouraging manifestation of model convergence on tropical dynamics. How-
468 ever, once seasonal variation is brought into discussion, model results tend to diverge owing to
469 GCMs' high sensitivity to detailed structures of the simulated tropical SST that exerts strong influ-
470 ences on the ENSO-Hadley circulation interaction (Guilyardi 2006; Feng and Li 2013; Guo and
471 Tan 2018 a,b; Feng et al. 2019). In fact, different relative contributions of SC and IAC modes to
472 TM variability may relate to the model-dependent mean state and seasonal cycle (Bellenger et al.
473 2014), which can be seen in the seasonal statistics of the Nino34 index (Figure S6). The following
474 features are particularly noteworthy: i) For MRI-CGCM3 the strongest warming occurs in boreal
475 winter (instead of boreal summer); ii) For IPSL-CM5A-LR the strongest standard deviation occurs
476 in May-June (instead of in winter months), and iii) For all GCMs except MPI-ESM-MR there exists
477 a temperature minimum in September, which is followed by warming through December. All these
478 features are absent in observations (Magnusson et al. 2013; Tan et al. 2020), pointing to strong
479 model bias in simulating the very basic climatic features in the tropics, which is beyond the current
480 scope and not discussed here. However, it may, in fact, help to explain why the relative contribution
481 of seasonal modes to TM variability in the optimum statistical models varies from GCM to GCM
482 (Figure 4a and Figures 7a-d).

483 Note that the two SC modes in Figure 2 are rotated from the leading two EOFs of the seasonal
484 component. The current decomposition is selected because i) the interhemispheric thermal contrast
485 that predominates in both modes is consistent with the seasonal change in the solar radiation that
486 is irrespective of ocean or land, and ii) it clearly captures the one-to-two month lag of OM behind
487 LM, which results from the large difference in effective heat capacity between the ocean and the

488 land. It is worth pointing out that the strong correlation of TM with SC modes from December of
489 the previous year (Figure 3c) does not depend on the eigenvector basis chosen.

490 The Arctic-Tropics linkage that is captured by all five GCMs has already been reported by other
491 modelling studies (e.g. Lin et al. 2002; Jia et al. 2009; Hegyi et al. 2014; Kim and Ahn 2015;
492 L'Heureux et al. 2017), but a clear lead-lag relationship has not yet been deciphered, which, at least
493 partly, has to do with the choices of numerical models (e.g., atmosphere-only model or Atmos-
494 phere-Ocean coupled GCM) and initial and forcing conditions (e.g., idealized forcing for sensitiv-
495 ity studies or forcing directly taken from atmospheric reanalysis data) that greatly differ between
496 studies. The Arctic-Tropics interaction has global impacts and likely involves the stratosphere -
497 troposphere coupling and jet dynamics (e.g., Jia et al. 2009; Hegyi et al. 2014; Kim and Ahn 2015).

498 Indications have been found that seasonal signals are actively involved in the Arctic-Tropics con-
499 nection. Below a brief introduction is presented and a more elaborated discussion is planned for a
500 follow-on report. Specifically, in positive AM years (colder-than-normal Arctic, corresponding to
501 negative Arctic Oscillation) the seasonal cycle is stronger than normal, which is mainly realized by
502 the intensified land mode (LM) around its peak time, namely, in May-June-July-August and No-
503 vember-December, respectively (not shown). As a consequence, the Eurasian continent is anoma-
504 lously warm/cold in boreal summer/winter, while in comparison, the AM-Ocean Mode (OM) cor-
505 relation is notably weaker. The above feature stems from the fact that AM-related cooling /warming
506 over the Arctic unavoidably alters the thermal contrast between the Arctic and the Eurasia continent
507 and consequently the contrast between continents and oceans (via the strong gearing of LM and
508 OM). Keeping in mind that in boreal winter, the Siberia-Mongolian High dwells in the cold Eurasia
509 and dictates the strength of the East Asian winter monsoon (EAWM), by modulating the East Asian
510 trough and the overlying jet stream. Therefore, positive AM enhances the Siberia-Mongolian High
511 by further cooling Eurasia and consequently strengthens the EAWM. This result is consistent with

512 the larger picture that emerges out of previous studies despite their different perspectives: negative
513 Arctic Oscillation (corresponding to positive AM) being accompanied by strong Siberian High and
514 strong EAWM (e.g., Gong et al. 2001; Wu and Wang 2002; He et al. 2017), whereby the East
515 Asian trough and the upper-level jet stream make important contributions (Jeong and Ho 2005; Li
516 et al. 2014; Luo and Zhang 2015; Chowdary et al. 2019). Down in the tropics, anomalously strong
517 EAWM weakens the El Nino-related Walker circulation thus favoring La Nina conditions (Chen
518 et al. 2000; Ma et al. 2018), which lends support to the negative sign of the AM-TM correlation
519 reported in Fig. 3b.

520 Along this line, the weak loose TM-AAM connection (Fig. 3b) may relate to the weaker seasonal
521 signals in the southern hemisphere owing to the absence of large landmass like Eurasia. This indi-
522 rectly supports the vital role the seasonal component plays in the pole-tropics interaction. On the
523 other hand, many important aspects of this coupling are not yet fully understood. For instance, how
524 does EAWM variability interact with ENSO? Where is the key region for the interaction with the
525 Walker Circulation, ENSO, and the Hadley circulation to take place? Is it the South China Sea,
526 near the Maritime continents, or the Indian Ocean (Chen et al. 2000; Wang and Wu 2012; Lee and
527 McBride, 2016)? Another piece of thought-provoking information is that, given the active role of
528 the seasonal signal in the Arctic-Tropics connection, a quite common experiment design that in-
529 volves atmosphere models forced by prescribed surface temperature patterns with a climatological
530 seasonal cycle is doomed to miss the seasonal signal as an active player, so does the resultant mode-
531 interaction structure. This aspect should be taken into account when interpreting the results of these
532 sensitivity studies.

533 One question worth discussing concerns how TM and TPM are related to ENSO. ENSO essentially
534 depicts abnormal conditions in the zonal temperature gradient in the tropical Pacific, where both

535 TM and TPM have considerable loadings (Figures 1a, d). ENSO indicators that are retrieved lo-
536 cally, including area-averaged sea surface temperature in Niño regions((Trenberth and Stephaniak
537 2001) and the related leading EOF patterns of temperature in the tropical Pacific sector (e.g., Xu et
538 al. 2017), unavoidably also comprise signals from TM and TPM. How to differentiate between
539 them is rather intricate, if possible at all. For instance, both TM and TPM comprise a zonal see-
540 saw pattern in the tropical Pacific. How to distinguish these patterns from that of ENSO has so far
541 rarely been discussed. Such a discussion requires *unambiguous* definitions of these modes, and it
542 concerns fundamental questions that are more of philosophical nature: *what is ENSO? how to*
543 *define ENSO?* Moreover, TM not only links the tropics and the subtropics via the Hadley circula-
544 tion but it also connects all tropical oceans through the Walker cell (Figures 1a, e, I, k, m). There-
545 fore, its spatial scale is much larger than that of ENSO, which by definition prioritizes signals in
546 the tropical Pacific. By focusing only on locally retrieved measures, it is almost impossible to as-
547 sess to which extent TM exerts its effects on these ENSO indicators, and most likely the detected
548 climate signals are *exclusively* attributed to ENSO.

549 Keeping these complications in mind, it is thus not surprising to obtain large (and statistically sig-
550 nificant) correlation coefficients between TM/TPM and the nino34 index (not shown). In fact, the
551 first two leading EOFs in Xu et al. (2017), which the authors refer to as *the eastern and central*
552 *Pacific El Nino (EP- and CP- El Nino)*, show high spatial resemblance to TM and TPM, respec-
553 tively. This study suggests that their *EP-El Nino pattern* may be viewed as a manifestation of a
554 predominant contribution of the HC (TM) within the tropical Pacific; TM mainly represents the
555 equator-to-pole temperature gradient that drives the HC and it is of primary importance for the
556 Earth climate (in comparison to ENSO), which provides a reasonable explanation for the much
557 higher variances of *the EP-El Nino type* with respect to *the CP-El Nino type* (e.g., Xu et al. 2017;
558 Freund et al. 2019).

559 It is worthwhile mentioning that, although all five GCMs analyzed in this study are free of long-
560 term trends, it is not always the case. For this reason, some GCMs are not included in this study
561 (e.g., GFDL-CM3). In fact, the coupling structure studied here shows strong sensitivity to the trend
562 removal technique, which, while capturing most of the trend signal, also extracts part of the inher-
563 ent variability (through overfitting). This aspect will be discussed in a companion study.

564 In summarizing, this study presents how to obtain a quantitative measure of mode interaction by
565 identifying the model-intrinsic coupling structure and consequently searching the optimum statis-
566 tical model. Such an approach helps to identify those key processes that are active (or inactive) in
567 model climates. It generates an overview over model capabilities and brings insight into model
568 strengths and weaknesses, which may guide us for tasks like assigning model weights in a multi-
569 model ensemble approach. For instance, MRI-CGCM3 that simulates the weakest coupling be-
570 tween seasonal components and TM, in fact, has a strongly biased mean seasonal cycle in the trop-
571 ical Pacific which, as a sign of low profile, then justifies a low weight for MRI-CGCM3, at least
572 when seasonal variation in this region is of concern.

573

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579

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790 **Tables**

791 Table -1: Five PiControl GCM simulations

792

PiControl	MPI-ESM-MR	NCAR_CCSM4	IPSL-CM5A-LR	MRI-CGCM3	GISS-E2-R
Duration (years)	1000	1051	1000	500	550

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795 Table-2 Parameters of the optimum regression model (AAM excluded, thus $a_3 = 0$) for the PiCon-
 796 trol simulation of MPI-ESM-MR; LM and OM are taken from December ($m=12$). Numbers in
 797 parenthesis denote the 95% confidence intervals. Parameters estimated from the entire 1000-year
 798 data are listed for comparison.

MPI-ESM-MR Optimum Model	b_1 (LM)	b_2 (OM)	a_1 (TM)	a_2 (AM)	a_4 (TPM)
Entire 1000 yrs	2.01 (1.19, 2.84)	-6.42 (-7.38, -5.45)	0.55 (0.50, 0.59)	-0.10 (-0.14, -0.06)	0.26 (0.21, 0.30)
First 500 yrs	1.70 (0.55, 2.84)	-6.12 (-7.49, -4.76)	0.54 (0.48, 0.61)	-0.10 (-0.17, -0.04)	0.23 (0.17, 0.30)

799

800 **Figure Legends**

801 Figure 1: (MPI-ESM-MR) a-d) The leading four IAC EOF modes of surface temperature: TM
802 (IAC1), AM(IAC2), AAM (IAC3), and TPM (IAC4) (unit: std of IAC, explained variances: 16.2%,
803 7.5%, 7.2%, 5.0%); e-h) Correlation coefficients between the corresponding principle components
804 and sea level pressure (SLP) (shadowed are significant values at 5%); i-n) Composites (color shad-
805 ing) of mass streamfunction (i, j, unit: 10^9 kg/s), surface temperature (k, l, unit: K) and velocity
806 potential at 200hPa (m, n, unit: 10^6 m²/s) for TM and TPM (positive minus negative); climatological
807 fields are contoured.

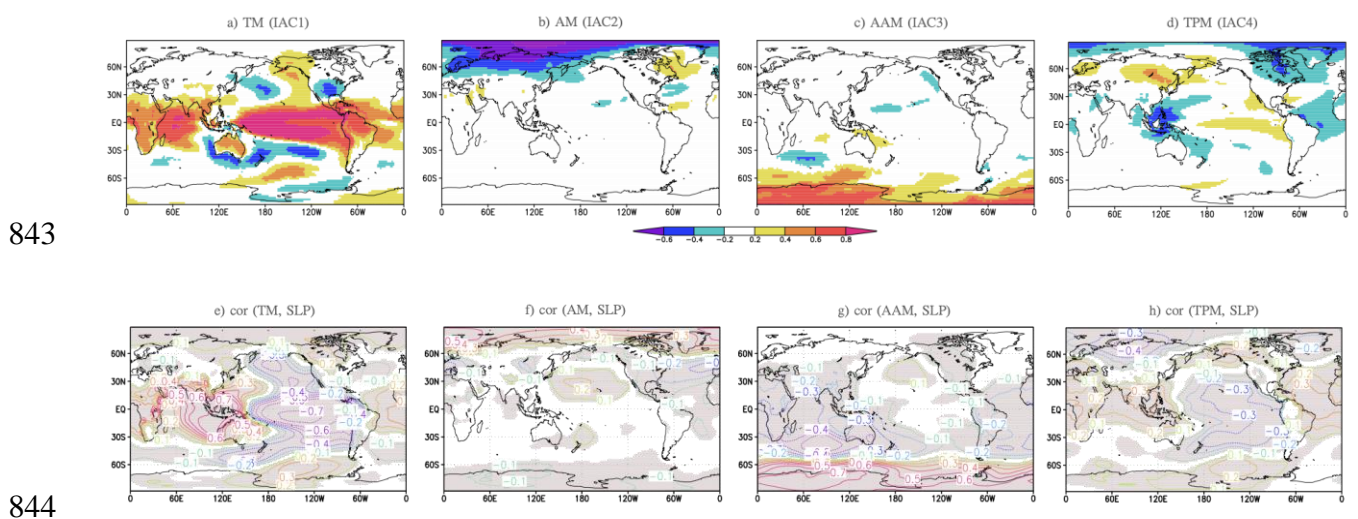
808 Figure 2: (MPI-ESM-MR) The leading two EOF modes of the seasonal component (SC) of surface
809 temperature: a) Land mode (SC-land) and b) Ocean mode (SC-ocean) (a-b, unit: std of SC, ex-
810 plained variances are 45% and 44%, respectively); c) their seasonal courses. Monthly ranges are
811 shadowed.

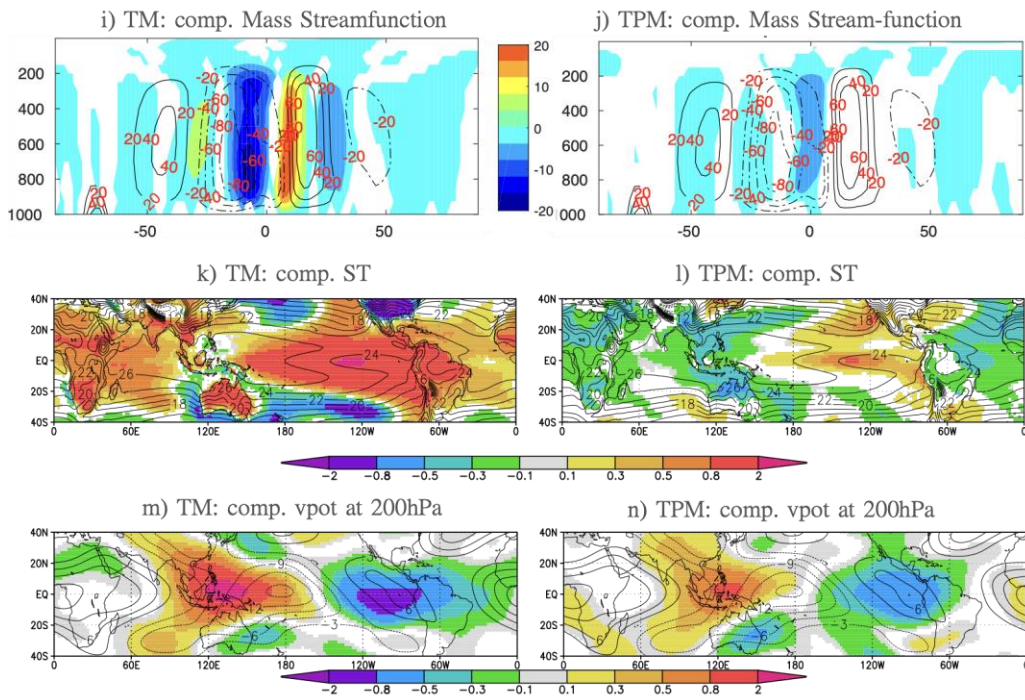
812 Figure 3 (MPI-ESM-MR) a) Q-Q plot of the TM (IAC1) principal component: (upper panel: nor-
813 mal Q-Q plot; lower panel: residual Q-Q plot); b-c) Cross-correlations between PCs of TM (IAC1)
814 and b) other IAC modes (IAC2: AM, IAC3: AAM, IAC4: TPM) and c) two seasonal modes. In b),
815 horizontal dashed lines mark the 95% confidence intervals; in c) coefficients with $P < 0.01$ are
816 marked with squares; lag = -1 corresponds to seasonal modes leading TM by 1 year; the climato-
817 logical monthly cycle of two seasonal modes (blue: LM, 'SC-land', brown: OM, 'SC-ocean') fol-
818 lows right axis.

819 Figure 4 (MPI-ESM-MR) Performance of candidate statistical models in terms of BIC (left axis)
820 and r-squared (right axis) assessed in two steps; the top performer at each step is marked in gray.
821 a) Three regression models: *SCs-only*, *IAC(1-4)-only*, and *SCs+IAC(1-4)* (the full model). b) Eight
822 regression models, all including both SCs and TM(IAC1) but with different combinations of the

823 other three IAC modes (IAC 2, 3, 4). The optimum regression model turns to be $SCs+IAC(1-2, 4)$.
824 All candidate models comprising both SCs show their lowest BIC in December, thus $m=12$.
825 Figure 5 (MPI-ESM-MR) Cross-validation of the optimum regression model for the PiControl sim-
826 ulation, with parameters determined from the first 500 years of TM's principle component (listed
827 in Table 2), while the rest 500-yr data serves as the target holdout data (black), with respect to
828 which predictions (red) are compared. Correlation between the holdout data and predictions is 0.74.
829 Figure 6: (Multi-models) same as Fig.3 but for NCAR-CCSM4(a-c), IPSL-CM5A-R(d-f), MRI-
830 CGCM3(g-i), and GISS-E2-R(j-l). Only residual QQ plots are shown. The null hypothesis that TM
831 follows normal distribution is rejected in a) and j) ($p<0.01$, in both AD test and JB test).
832 Figure 7 (Multi-models) same as Figure 4a but including the optimum regression model in the last
833 column (marked in gray). All regression models comprising seasonal components as explanatory
834 variables have their best performances in December ($m=12$).
835

836 Figure 1: (MPI-ESM-MR) a-d) The leading four IAC EOF modes of surface temperature: TM
 837 (IAC1), AM(IAC2), AAM (IAC3), and TPM (IAC4) (unit: std of IAC (Figure S3-b), explained
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 839 principle components and sea level pressure (SLP) (shadowed are significant values at 5%); i-n)
 840 Composites (color shading) of mass streamfunction (i, j, unit: 10^9 kg/s), surface temperature (k, l,
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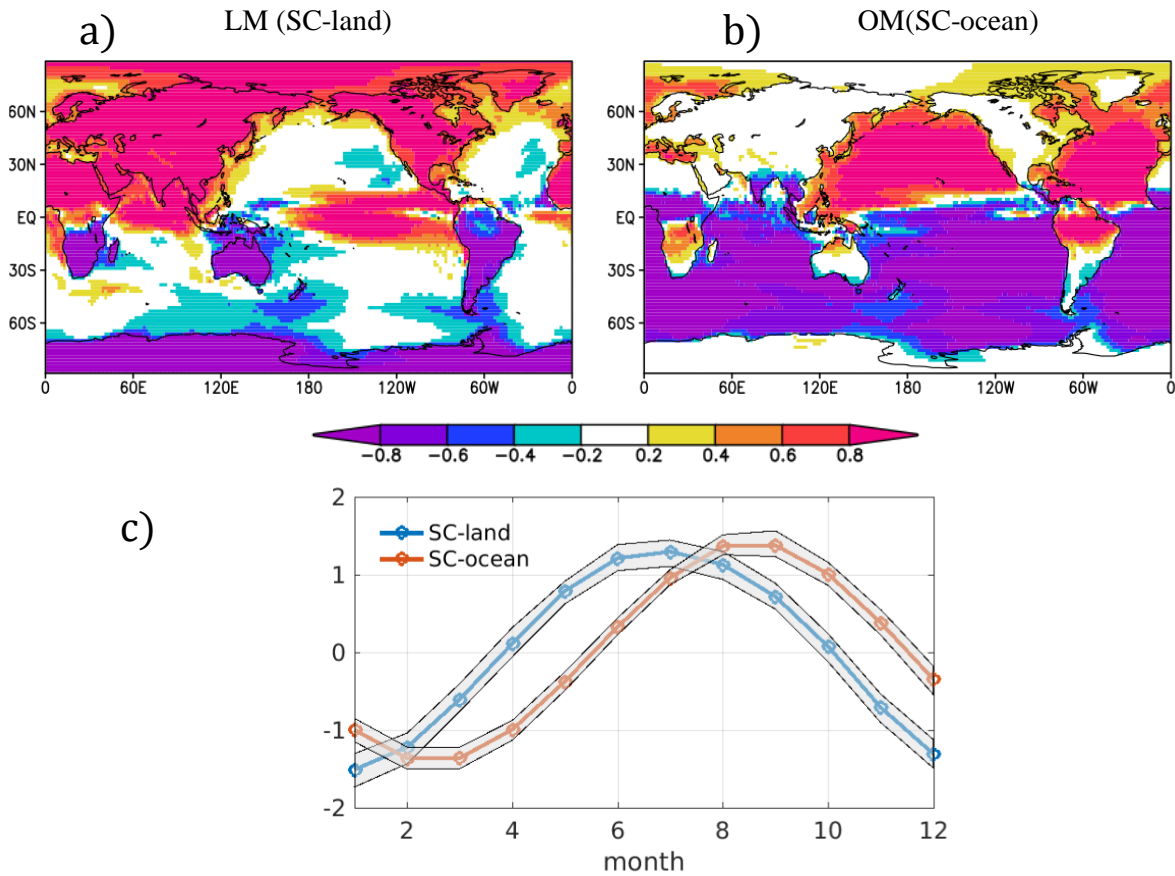
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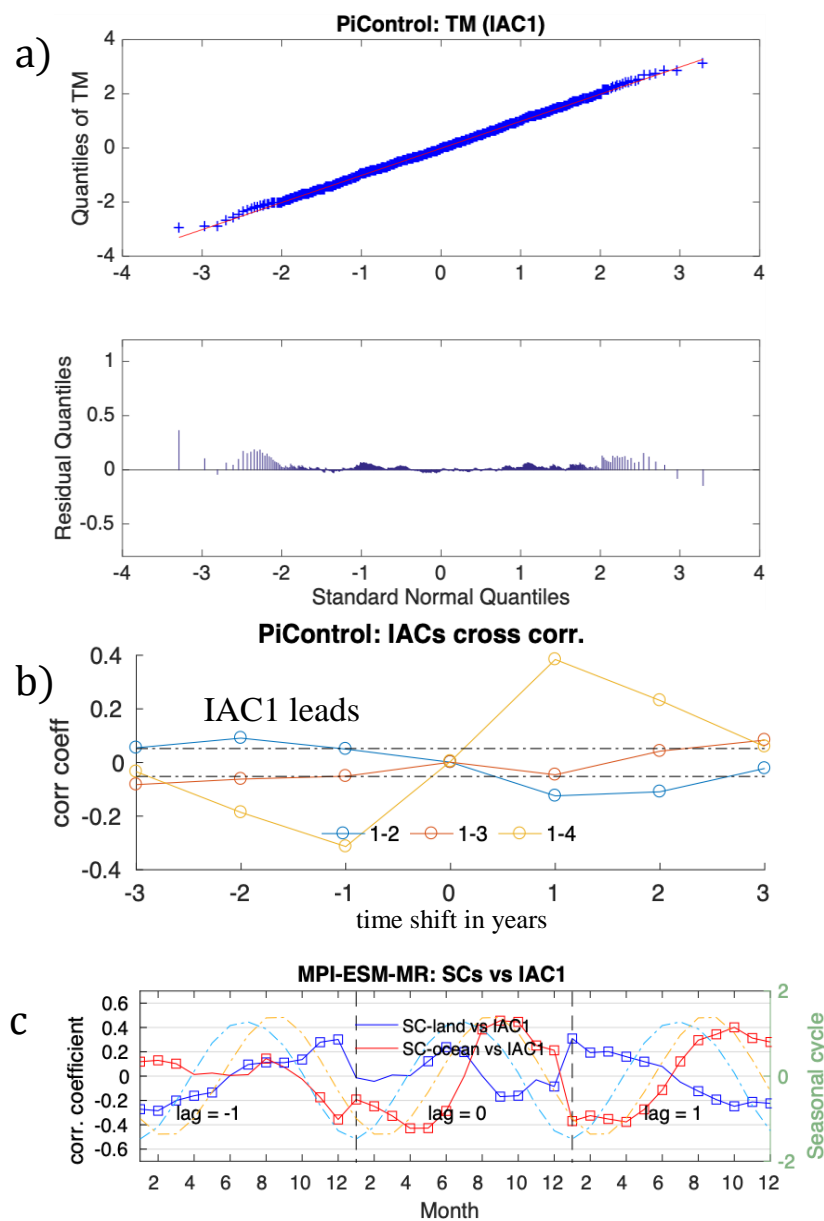
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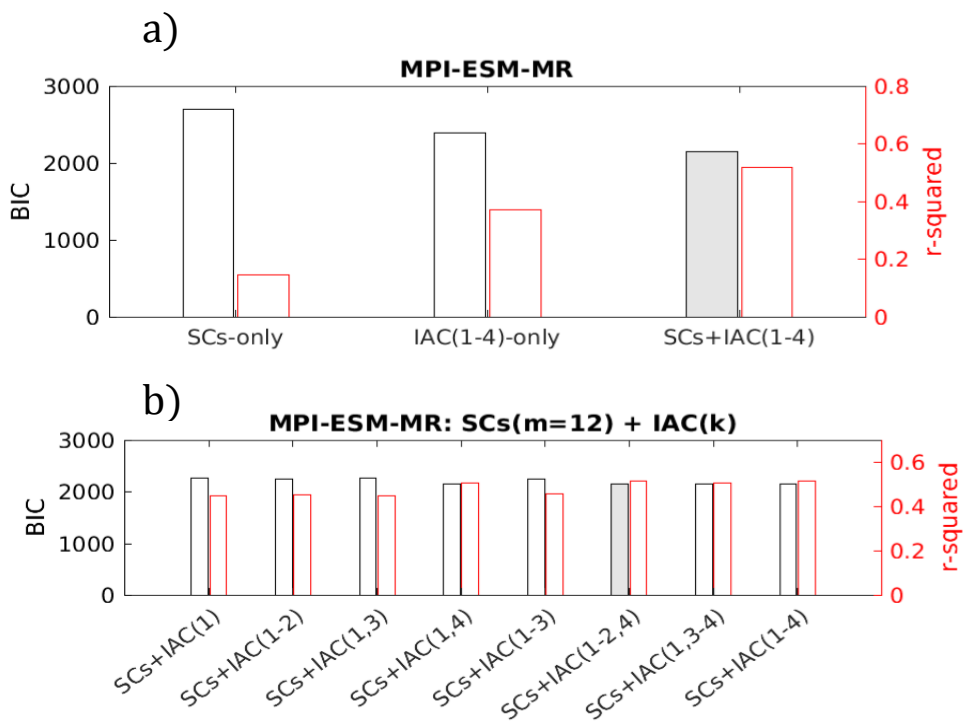
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856 Figure 3 (MPI-ESM-MR) a) Q-Q plot of the TM (IAC1) principal component: (upper panel: nor-
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 858 and b) other IAC modes (IAC2: AM, IAC3: AAM, IAC4: TPM) and c) two seasonal modes. In b),
 859 horizontal dashed lines mark the 95% confidence intervals; in c) coefficients with $P < 0.01$ are
 860 marked with squares; lag = -1 corresponds to seasonal modes leading TM by 1 year; the climato-
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 862 follows right axis.

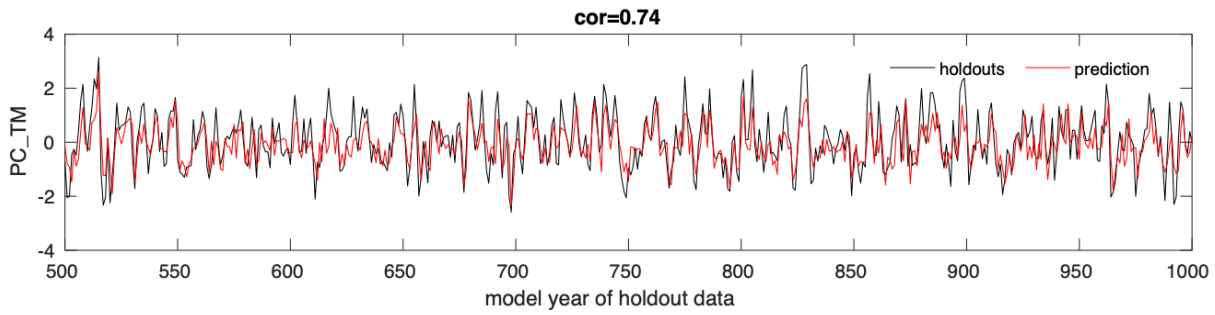


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886 which predictions (red) are compared. Correlation between the holdout data and predictions is 0.74.



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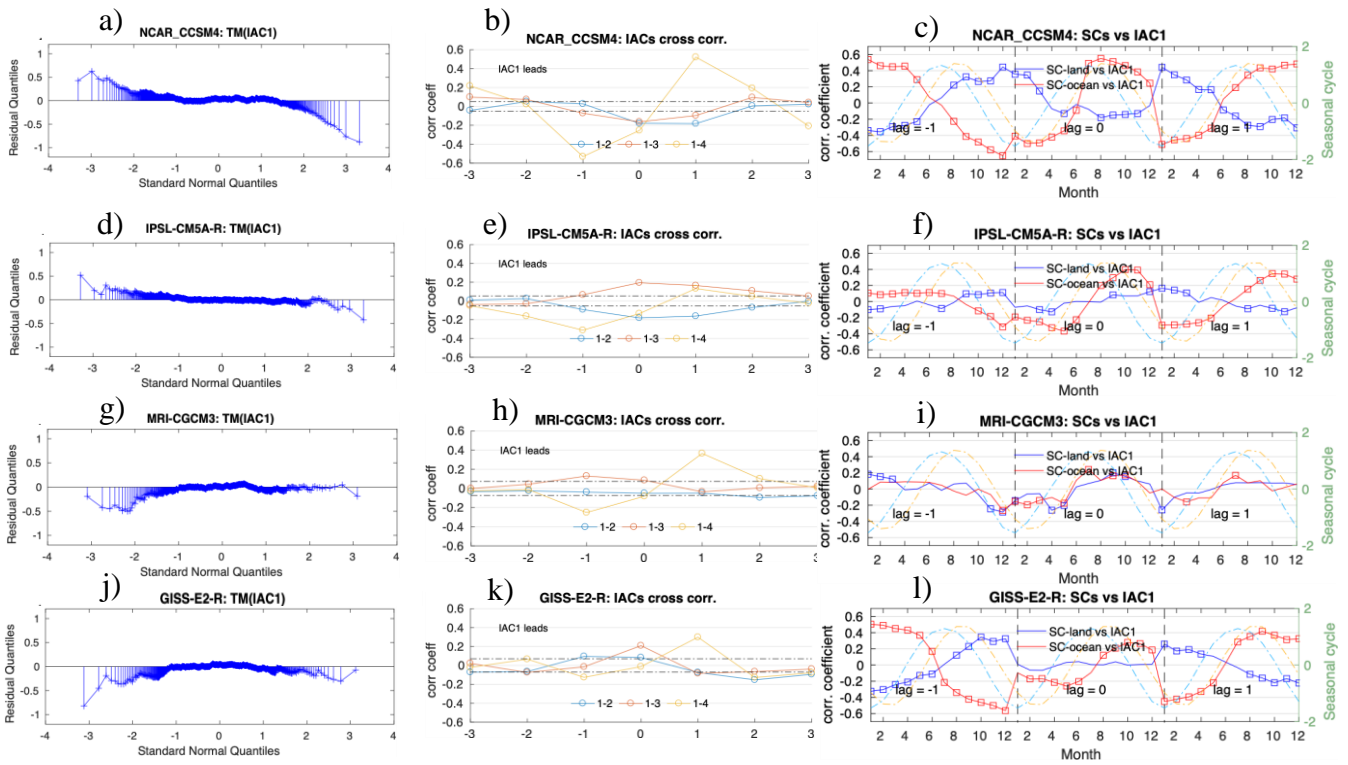
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892 Figure 6: (Multi-models) same as Fig.3 but for NCAR-CCSM4(a-c), IPSL-CM5A-R(d-f), MRI-
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 894 follows normal distribution is rejected in a) and j) ($p < 0.01$, in both AD test and JB test).

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898 Figure 7 (Multi-models) same as Figure 4a but including the optimum regression model in the last
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