Application of Coherent ADCP for Turbulence Measurements in the Bottom Boundary Layer

ANDREAS LORKE

Applied Aquatic Ecology, EAWAG, Kastanienbaum, Switzerland, and Environmental Physics, Limnological Institute, University of Constance, Constance, Germany

ALFRED WÜEST

Applied Aquatic Ecology, EAWAG, Kastanienbaum, Switzerland

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ABSTRACT

This paper presents a novel approach for estimating the rate of turbulent kinetic energy dissipation from pulse-coherent acoustic Doppler current profiler (ADCP) measurements using the inertial dissipation method. Although the inertial dissipation technique is widely accepted and used in oceanographic and atmospheric research, its application to ADCP data is limited by the loss of directional information for high-wavenumber velocity fluctuations. However, measurements in the bottom boundary layer of a lake revealed astonishing agreement between dissipation rates estimated from temperature microstructure profiles and those estimated by applying the inertial dissipation method to data from two different brands of ADCPs.

1. Introduction

In this paper we test the applicability of the inertial dissipation method (IDM) for estimating profiles of dissipation rates $\varepsilon$ of turbulent kinetic energy from the three-dimensional current velocities measured by conventional acoustic Doppler current profilers (ADCPs) operated in pulse-coherent mode. The IDM is based on the existence of an inertial subrange in the wavenumber spectrum of velocity fluctuations and is a well-established and widely accepted method to estimate dissipation rates from measured time series of two- or three-dimensional current velocities. For technological reasons, however, applications have been restricted so far to single-point measurements or to data from instrument arrays.

ADCPs are capable of measuring profiles of the current velocity by applying run-time windowing of backscattered acoustic pings along three or four beams pointing in different directions. Whereas normal-mode ADCP measurements evaluate the Doppler frequency shift of the backscattered signal to estimate the in-beam velocity of the scattering particles, the pulse-coherent mode evaluates the phase shift between the echoes of two subsequent pings, resulting in much higher measurement accuracy but shorter profiling ranges. With the assumption that the velocity is the same within the respective depth bins of each beam, a three-dimensional velocity vector can be constructed from the measured along-beam velocities of at least three beams. A typical beam geometry is such that the beams are inclined by $20^\circ$–$30^\circ$ to the vertical and are symmetrically arranged within a horizontal plane projection (e.g., in a Janus configuration). Depending on the range from the instrument and the slant angle, the above assumption is equivalent to a velocity field that is horizontally homogenous on the scale of a few meters. For the mean velocity field this is usually an appropriate assumption for most flows in natural water bodies; however, it is not valid for turbulent velocity fluctuations, the data basis of the IDM. A detailed outline of the procedure to calculate a three-dimensional current vector based on the measured in-beam velocities of a three-beam ADCP is illustrated in Fig. 1. In analogy, for a four-beam ADCP the calculus is given, for in-
The usefulness and limits of this approach are discussed in this paper by comparing dissipation rate estimates using the IDM from two different ADCPs with simultaneously measured dissipation rates from temperature microstructure profiles. The measurements were conducted in the low-energetic environment of a bottom boundary layer in a lake in the framework of an experiment focusing on the impact of bottom boundary turbulence on the diffusive flux of oxygen at the sediment–water interface (Lorke et al. 2003).

2. Study site and instrumentation

The measurements were carried out for 25 h on 13–14 August 2002 in the bottom boundary layer of Lake Alpnach, a medium-sized subbasin of Lake Lucerne in central Switzerland. Lake Alpnach has an elliptical shape with axes lengths of 5 and 1.5 km and a maximum depth of 34 m. The strongly pronounced seiching (Münich et al. 1992; Gloor et al. 1994), resulting from daily winds along its main axis and the associated periodic nature of bottom boundary layer turbulence (Lorke et al. 2002), makes Lake Alpnach an ideal site for the present study.

Two ADCPs were deployed on the lake bottom, and temperature microstructure and conductivity–temperature–depth (CTD) profiles were measured on a regular time scale. All instruments were operated within a radius of about 100 m at a site close to the center of the lake at a local depth of 32.2 m.

a. ADCP measurements

A four-beam, 614-kHz RDI Workhorse ADCP (RD Instruments) was deployed directly onto the sediment facing upward. The pulse-coherent mode (RDI mode 5) with a bin size of 0.1 m was used, enabling a measurement range from 0.6 to 8.1 m above the sediment (31.6–24.1-m depth). Groups of three pings were averaged internally, and the averaged data were recorded every 2 s. In addition, a three-beam, 1.5-MHz Nortek NDP (Nortek AS, Norway) was mounted on a tripod facing downward, resolving the range from 0.05 to 2.2 m above the sediment (32.15–30-m depth) with a vertical bin size of 0.04 m. The NDP was operated in high-resolution (pulse coherent) mode and recorded the average of six individual pings every 9 s. Special data conversion software (A. Lohrmann, Nortek AS, 2002, personal communication) enabled an increase of the velocity precision by a factor of 10 for the Nortek NDP to 0.1 mm s⁻¹, as compared to the standard value of 1.0 mm s⁻¹ for both instruments.

\[
\begin{align*}
& b_1 = u_1 \sin \theta - w_1 \cos \theta \\
& b_2 = u_2 \sin \theta \cos 120° - v_1 \sin \theta \sin 120° - w_1 \cos \theta \\
& b_3 = u_3 \sin \theta \cos 240° - v_3 \sin \theta \sin 240° - w_2 \cos \theta
\end{align*}
\]

FIG. 1. Beam geometry and calculation of the horizontal and vertical velocity components \((u, v, w)\) from the measured in-beam velocities \((b_1, b_2, b_3)\) for a three-beam acoustic Doppler current profiler (such as the Nortek NDP). Whereas the derivation is exemplified for beam 1, the respective derivations for beams 2 and 3 can be obtained by rotating the coordinate system by \(120°\) and \(240°\) in the horizontal \((x-y)\) plane. An unambiguous three-dimensional velocity vector \((u, v, w)\) for each depth cell can be estimated only by assuming horizontal homogeneity of the flow field \((u_1 = u_2 = u_3, v_1 = v_2 = v_3, w_1 = w_2 = w_3)\).
b. Temperature microstructure and CTD measurements

Temperature microstructure profiles were measured with a pair of FP07 fast-response thermistors (Thermometrics) on an adapted SEABIRD SBE-9 CTD profiler (Sea-Bird Electronics, Inc.) (Kocsis et al. 1999). The probe was operated freely sinking with a speed of 8 cm s\(^{-1}\) from 20-m depth to about 0.15 m above the sediment. The sampling frequency was 96 Hz, and profiles were collected every 15 min, resulting in 96 profiles in total and leaving enough time between subsequent casts for profiler-induced turbulence to be advected away from the sampling site (Jonas et al. 2003).

A SEABIRD SBE-19 CTD was used to measure profiles of temperature, conductivity, dissolved oxygen, pH, and light transmissivity (at 660 nm) throughout the entire water column every 2 h.

3. Data processing and analysis

a. Temperature microstructure method

The temperature microstructure method (TMM) is based on the existence of a universal form of the high-frequency wavenumber spectrum of temperature or temperature gradient fluctuations in homogeneous and isotropic turbulence. The theoretical spectrum was estimated by Batchelor (1959), and its one-dimensional form has been validated by a variety of laboratory and field experiments (e.g., Grant et al. 1968). The viscous-convective and diffusive subranges of the one-dimensional temperature fluctuation spectrum \(\Phi^T\) as a function of the scalar (vertical) wavenumber \(k_3\) can be described by

\[
\Phi^T(k_3) = \sqrt{q \over 2 \nu D} x \left( e^{-(1/2x^2)} - e^{-1/2} \int_x^\infty e^{-(1/2x'^2)} dx' \right),
\]

where \(x\) denotes the dimensionless wavenumber \(x = (2q)^{1/2} k_3 / k_B\) with the Batchelor wavenumber \(k_B = \sqrt{\epsilon / \nu D}\) and the Batchelor constant \(q = \gamma(1 + \nu D)\) (\(\nu\) is the molecular diffusivity of heat and the kinematic viscosity, respectively).

The typically low dissipation rates, which are often below the detection limit of oceanographic shear probes, in conjunction with short profiling ranges, allowing for a slow profiling speed, favor the temperature microstructure or Batchelor method over the profiling shear probes in lakes. The shortcomings of this method, arising from the limited response time of the thermistor (Gregg 1999), can usually be neglected under such conditions (Kocsis et al. 1999). Fitting measured temperature spectra to Eq. (1) has become a standard method for estimating \(\epsilon\) in lakes (e.g., Dillon et al. 1981; Luketina and Imberger 2001; Jonas et al. 2003). The temperature fluctuations are usually measured using slowly sinking or upwelling profilers equipped with fast-response thermistors. Taylor’s (1938) frozen field hypothesis is used to transform the respective temperature fluctuation spectra from the frequency to the wavenumber domain using the profiling speed.

The measured temperature microstructure profiles were segmented using fixed and overlapping segmentation lengths of 512 data points, corresponding to \(~45\) cm long profile sections. Within these segments the profiler drop rate was sufficiently steady, and the respective fluctuation spectra in the wavenumber domain were fitted to Eq. (1) with \(\epsilon\) and \(\chi\) as the fitting parameters. The probe, the data acquisition, and the data processing procedure have been described in detail in Kocsis et al. (1999) and Jonas et al. (2003).

b. Inertial dissipation method

Similar to the TMM, the inertial dissipation method (IDM) is based on fitting measured fluctuation spectra to their respective theoretical and universal forms, however, not within the high-frequency dissipation range but within the inertial subrange of the wavenumber spectrum. There, the spectra often show the characteristic \(k^{-5/3}\) slope as a function of the wavenumber \(k\) (Tennekes and Lumley 1973). Although it was shown that fluctuation spectra of scalar properties like temperature, suspended solid, or chlorophyll concentrations follow this characteristic slope (Soulsby et al. 1984; McPhee 1994; Lee et al. 2003), the lack of universal scaling constants constrained the application of this method to measured spectra of the three-dimensional velocity fluctuations. In homogeneous turbulent flow and with the assumption of isotropy, the diagonal components \(\Phi^i_i\) \((i = 1, \ldots, 3)\) of the associated spectrum tensor can be separated:

\[
\Phi^i_i = \alpha_i \nu^{(2/3)} k_i^{-(5/3)},
\]

The index \(i\) refers to the along-stream \((i = 1)\) and cross-stream \((i = 2, 3)\) components of the spectrum tensor, and \(\alpha_i\) refers to the one-dimensional Kolmogorov constant \(\alpha_k\) \((\alpha_1 = \alpha_2 = \alpha_3 = 4/3\alpha_k)\). By applying Taylor’s hypothesis \(\Phi^i_i\) is calculated from measured time series of the three-dimensional velocity, and thus \(\epsilon\) is estimated by spectral fitting (e.g., Gross and Nowell 1985; Dewey and Crawford 1988; McPhee 1998; Bertuccoli et al. 1999).

Since ADCPs do not resolve the directions of the
turbulent velocity fluctuations, along-stream and cross-stream velocity spectra cannot be separated. Thus the isotropy constant $\alpha_i$ in Eq. (2) remains undetermined within the range $\alpha_K \leq \alpha_i \leq 4/3\alpha_K$. Using spectral fitting [Eq. (2)] leads to an uncertainty for the dissipation rate estimation of up to a factor of $(4/3)^{-3/2} \approx 0.65$, which is well within the range of uncertainties of conventional methods (e.g., Peters and Gregg 1988; Yamazaki and Osborn 1990).

Segments of the measured time series of the velocities at all depths were first analyzed for the mean current direction and speed. Wavenumber spectra were calculated from the measured in-beam velocities and averaged over the three and four beams of the Nortek NDP and RDI ADCP, respectively. Segment sizes were 128 samples (19.2 min) for the Nortek and 512 samples (17 min) for the RDI. If the spectra exhibited an inertial subrange slope, a straight line representing a $-5/3$ slope was fitted to a double logarithmic spectrum plot, and $\varepsilon$ was estimated by rearranging Eq. (2), using a Kolmogorov constant $\alpha_K = 1.56 \times 18/55$ for the streamwise spectral component (Wolk et al. 2002; Jonas et al. 2003). The particular choice of the isotropy constant results in the estimation of an upper limit for $\varepsilon$ due to the unknown orientation of the spectrum with respect to the mean flow. Sample spectra from both ADCPs are shown in Fig. 2. The wavenumber range used for the fitting procedure was adjusted manually for each spectrum according to the existence of an inertial subrange.

Alternatively, an automated procedure was employed to perform the spectral fitting. This procedure, which was applied to fixed frequency ranges (from $9 \times 10^{-4}$ to $3 \times 10^{-2}$ Hz for the Nortek and from $1 \times 10^{-3}$ to $4 \times 10^{-2}$ Hz for the RDI), estimated $\varepsilon$ based on Eq. (2) by

$$\varepsilon = \exp \left( \ln \left( \frac{\Phi^K}{\alpha_K (\omega/U)^{5/3}} \right)^{3/2} \right),$$

with $\omega$ and $U$ being frequency and mean current speed and $\langle \cdot \rangle$ denoting averaging over different frequencies in the logarithmic domain. A fixed frequency limit was chosen in favor of an upper wavenumber limit, since it was assumed that instrument noise is the most relevant process limiting the high-wavenumber resolution of the measurements and that this noise can be described more appropriately in the frequency domain.

Besides instrumental noise, the high-wavenumber response of the ADCP is limited by the system spatial resolution (Zedel and Hay 1999). The maximum wavenumber resolved by the instrument is $2\pi/(2d)$, with $d$ being the width of the acoustic beam in the particular depth bin. Given the transducer diameters of 0.043 and 0.078 m for the RDI and Nortek, respectively, and assuming a beam-spreading angle of 1.5°, the corresponding wavenumbers are 43–11 rad m$^{-1}$ for the RDI and 78–30 rad m$^{-1}$ for the Nortek, depending on distance from the instrument. Whenever the wavenumber of the noise-limiting frequency exceeded the wavenumber of the system spatial resolution, the latter was used during the automated fitting procedure.

4. Results

The averaged current speeds and directions measured by both ADCPs are shown in Fig. 3. During the 25-h observation the speeds varied between 1 and 30 mm s$^{-1}$ and covered a bit more than one complete cycle of internal seiching with a period of about 18 h. The regular seiching pattern was slightly disturbed by a moderate wind event at the end of the measurements. The main current directions (northeast and southwest, respectively) correspond to the alignment of the main axes of the lake. Although the current directions measured by both instruments agreed almost perfectly, systematic differences were found in the current speeds. As shown in Fig. 3, the differences in the measured current speeds depended on the current direction. Whereas during the northeast currents [1800–0600 local time (LT)] the speeds measured by both instruments agreed reasonably well, systematic differences of ~4 mm s$^{-1}$ (up to 60%) were detected at the beginning and at the end of the 25-h observation (southwest current

Fig. 2. Wavenumber spectra of the in-beam velocities measured simultaneously by the RDI ADCP and the Nortek NDP. The spectra were calculated over time periods of 19 (RDI) and 17 (Nortek) min, respectively, and averaged over all beams at a height of 1 m above the sediment. The straight line shows a $k^{-5/3}$ inertial subrange slope.
direction). The higher velocities were measured by the Nortek. Since the form of the current profiles also differed significantly during these periods (not shown), it cannot be excluded that the measured differences were real and could be attributed to topography-induced variations of the local flow field.

A comparison of the TMM-based dissipation rates with the IDM estimates from the two ADCPs is shown in Fig. 4. In general, the turbulence followed the same dynamics as the current velocity, resulting in a periodic structure. However, as shown by Lorke et al. (2003) and discussed in more detail in Lorke et al. (2002), the turbulent dissipation at some distance from the sediment lags behind the current velocity due to the seiching-induced periodicity of the flow. The estimated time lag at a height of 1 m above the sediment was between 1.5 and 2 h (Lorke et al. 2002).

The TMM-based dissipation estimates at a height of 1 m above the sediment varied over three orders of magnitude between $10^{-11}$ and $2 \times 10^{-8} \text{ W kg}^{-1}$ throughout the seiching period. The IDM-based $\varepsilon$ values from the two ADCPs followed the same dynamics as the TMM-based dissipation estimates, and the correspondence between both methods was excellent (Fig. 4). An inertial subrange was observed in the velocity spectra almost throughout the entire measurement period, although it was less pronounced at the rising flanks of the current speed (Fig. 4). A major discrepancy between the TMM- and IDM-based dissipation estimates was found on the morning of 14 August (0600–0800 LT), when high dissipation rates were measured by both ADCPs, whereas the TMM-based dissipation rate remained low.

The vertical structure of the dissipation rate is exemplified in Fig. 5, which shows dissipation profiles from all three instruments for periods of “strong” (Fig. 5a) and “weak” (Fig. 5b) turbulence, respectively. In contrast to the dissipation time series shown in Fig. 4, the IDM-based dissipation rates were estimated using an automated procedure by fitting a $k^{-5/3}$ slope to the spectra, regardless of whether or not they matched the Kolmogorov form.

The “strong” turbulence profile showed a pronounced bottom boundary layer within the lowest 2 m above the sediment, with turbulent dissipation rates increasing by more than two orders of magnitude. The bulk dissipation above, measured by the TMM, did not show much dynamics, with very weak dissipation rates between $10^{-11}$ and $10^{-10} \text{ W kg}^{-1}$.

By comparing the two profiles, it becomes obvious that in this example the noise level or the detection limit of the automated estimation procedure for the RDI-based dissipation rate was about $4 \times 10^{-10} \text{ W kg}^{-1}$.
5. Discussion

The comparison of the dissipation rate estimates in the bottom boundary layer using the two different measurement techniques and three different instruments was limited by two general constraints. (i) For technological reasons the application of the IDM to ADCP data holds the lack of a properly defined isotropy constant $\alpha$ in Eq. (2). (ii) Both methods, the TMM and the IDM, rely on the conditions of homogeneous and isotropic turbulence, which are not necessarily fulfilled for periodically forced bottom boundary layers. Further, considering the highly intermittent turbulence in natural waters (e.g., Baker and Gibson 1987), the correspondence of the dissipation rate estimates, using the two different techniques and three different instruments, was excellent. It is important to note that the two techniques differ fundamentally, not only in measurement principle (direct measurement of the velocity fluctuations versus associated temperature fluctuations) but also in wavenumber range under consideration. Whereas the TMM is most sensitive to the diffusive cutoff in the temperature fluctuation spectrum at the highest wavenumbers ($k > 10^3 \text{rad m}^{-1}$), the IDM relies on the existence of an inertial subrange at wavenumbers that are at least one order of magnitude smaller.

As explained in the introduction, the application of the IDM to ADCP data has the uncertainty of the undefined isotropy constant $\alpha$ in Eq. (2) resulting from the unresolved directional information of the velocity fluctuations. The use of $\alpha$ for the streamwise fluctuation spectrum would result in the estimate of an upper limit for the dissipation rate $\varepsilon_*$ with the “true” dissipation rate $\varepsilon$ between

$$\left(\frac{4}{3}\right)^{-3/2} \varepsilon_* \leq \varepsilon \leq \varepsilon_*.$$  \hspace{1cm} (4)

This range results from the difference between the isotropy constants $\alpha$ for the streamwise ($\alpha = \alpha_k$) and cross-stream-wise ($\alpha = 4/3\alpha_k$) wavenumber spectra [Eq. (2)]. The actual factor within this given range, however, is not completely random but is biased by the orientation of the ADCP toward the mean flow. Figure 6 shows a direct comparison of $\varepsilon_*$ estimated from the Nortek NDP with the TMM-based dissipation rate (the figure reproduces the corresponding data from Fig. 4). Although the two independent estimates are linearly correlated over the entire range of the measurements, the
large scatter does not allow the estimation of a bias, and $e_{\infty} \approx e$ seems to be the best first-order approximation. A linear regression of the logarithmic dissipation rates results in a slope of 0.99. The range of uncertainty encompassed by Eq. (4) is shown in Fig. 6. This range is small compared to the overall uncertainty of the dissipation estimates resulting from the intrinsic intermittency in natural waters ($\alpha_{\text{int}} \approx 0.5 \ldots 2$; Baker and Gibson 1987), which is usually expressed as an uncertainty factor of 2 (Kocsis et al. 1999).

6. Conclusions

The application of the inertial dissipation method (IDM) to ADCP velocity data is not a straightforward approach due to the missing directional information of the measured fluctuation spectra. However, a comparison of dissipation rates measured simultaneously by the conventional “profiling technique” (temperature microstructure) and by two different ADCPs revealed good agreement between both methods. The discrepancies are reasonable and similar to those found in other experiments that compare estimates of dissipation rates using two or more different techniques (e.g., Moum et al. 1995; Kocsis et al. 1999; Gregg 1999).

The measurements were conducted in the relatively low energetic bottom boundary layer of a lake. There was strong evidence that the dissipation rate estimates, at least from the RDI ADCP, were limited by instrument resolution. Hence it can be expected and should be proven in future experiments that the method performs at least as robustly in more energetic environments such as the coastal ocean or estuaries. A prerequisite, however, is the use of the pulse-to-pulse coherent operation mode of the ADCP, which enables higher-accuracy velocity measurements although restricting the measurement range to a few meters, depending on the acoustic frequency.

Because of its limited profiling range and accuracy, the described method cannot replace conventional turbulence measurements using vertical profiling techniques. However, as a supplementary method, the IDM offers the great advantage of potential long-term and autonomous operation. Furthermore, this method provides a remote sensing approach for simultaneously measuring dissipation and vertical current shear, the driving force of turbulence. Considering the future development of appropriate fitting procedures, as proposed for Batchelor curve fitting (e.g., Ruddick et al. 2000), the relatively simple algorithm of the inertial dissipation method promises great potential for fully automated data processing routines.

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REFERENCES


