

## Salinity Determination from Use of CTD Sensors

C. E. KNOWLES

*Dept. of Geosciences, North Carolina State University, Raleigh 27607*

10 August 1973 and 4 December 1973

### ABSTRACT

To convert the specific conductance  $C(S,t,p)$  measured by an *in situ* CTD sensor to salinity in a manner consistent with the international standard expression proposed by Cox *et al.*, it is necessary to have established a means of estimating the specific conductance of seawater having a salinity of 35‰, [i.e.,  $C(35,t,0)$ ]. Third-order polynomial expressions formulated from samples having salinities near 35‰ are discussed. From the results of this study, it is recommended that an international expression for  $C(35,t,0)$  be established and that the conductivity ratio  $R_t$  calculated from this standard expression be used to obtain salinity using the UNESCO tables or the equation of Cox *et al.*

### 1. Introduction

There are many investigators who for a variety of reasons still measure specific conductance  $C(S,t,p)$  using *in situ* conductivity-temperature-depth (CTD) sensors as a means of determining the salinity of seawater. A problem arises, however, when an attempt is made to relate the  $C(S,t,p)$  measured by this sensor to its corresponding value of salinity, because the widely accepted expression of salinity as a function of conductivity proposed as the international standard by Cox *et al.* (1967) and as discussed by Wooster *et al.* (1969), Lyman (1969) and Tsurikova and Tsurikov (1971) is based upon the use of  $R_t$  [defined as the ratio of the specific conductance  $C(S,t,0)$  of a seawater sample to that of water having a salinity  $S$  of exactly 35‰, where both samples are at the same temperature  $t$ , and under a pressure of one standard atmosphere], i.e.,

$$R_t = C(S,t,0)/C(35,t,0). \quad (1)$$

The UNESCO tables and Cox *et al.*'s polynomial expression are actually for  $R_{15}$ , so they also provide a correction to  $R_t$  for temperatures different from  $t=15^\circ\text{C}$ .

For shallow waters where pressure effects are minimal,

$$C(S,t,p) \approx C(S,t,0), \quad (2)$$

and  $C(S,t,p)$  can be used directly to calculate (1), provided, of course, that  $C(35,t,0)$  is known. For depths where pressure is important, Bradshaw and Schleicher (1965), Perkin and Walker (1972) (for arctic regions) and Hassler (1971) have discussed methods that can be used to compensate for its effects.

Clearly, if one measures  $C(S,t,p)$  and wants to use Cox's standard expression, what is needed is a reliable

and standard way to approximate  $C(35,t,0)$ . Further more, since Copenhagen Normal Water is the standard used in determining salinity and specifically, since all conductivity salinometers use it to measure the reference value of  $C(35,t,0)$  and calculate  $R_t$ , the same standard should be used in providing  $C(35,t,0)$  for use with *in situ* CTD sensors. What is needed, therefore, is a complete set of conductivity measurements for Copenhagen Normal Water over a wide range of temperatures and an equation and table to approximate  $C(35,t,0)$  that fits these data.

### 2. Approximating $C(35, t, 0)$

Most of the empirical relationships formulated specifically to approximate  $C(35,t,0)$  have been published in technical reports or included in the proceedings of conferences and, therefore, have been generally unavailable for use by other investigators.

In almost every instance the formulations were based upon the experimental work of either Thomas *et al.* (1934), Brown and Allentoft (1966), or Cox *et al.* (1967). Actually, the intent of the latter two studies was to measure the conductivity ratio  $R_t$  and not the specific conductance  $C(35,t,0)$  directly, but valid approximation expressions can be derived from the data. Other studies (Weyl, 1964; Park and Burt, 1965) have discussed some of the possible errors in the data of Thomas *et al.* (1934).

One recently published paper that has had a wide distribution is that of Perkin and Walker (1972). They developed a third-order polynomial equation to estimate  $C(35,t,0)$  from the experimental data of Brown and Allentoft (1966), but their intent was to provide an approximation technique for use in the Arctic so their equation is not valid for temperatures greater than  $25^\circ\text{C}$ .

TABLE 1. Comparison of results of four equations for approximating the conductivity of seawater that has a salinity of 35‰.

| <i>T</i><br>(°C)  | Conductances<br>(mΩ <sup>-1</sup> cm <sup>-1</sup> ) |          |                 |                 | Differences<br>(×10 <sup>-2</sup> mΩ <sup>-1</sup> cm <sup>-1</sup> ) |  |                    |                    |                     |                     |
|---|--|----------|-----------------|-----------------|---|--|--------------------|--------------------|---------------------|---------------------|
|   | KR   | PW       | KN <sub>1</sub> | KN <sub>2</sub> | KR-PW   | KN <sub>1</sub> -KN <sub>2</sub>                             | KR-KN <sub>1</sub> | KR-KN <sub>2</sub> | KN <sub>1</sub> -PW | KN <sub>2</sub> -PW |
| 35  | 63.7274  | 63.7927* | 63.7374         | 63.7508         | -6.53*  | -1.34  | -1.00              | -2.34              | -5.53*              | -4.19*              |
| 30  | 58.3324  | 58.3740* | 58.3399         | 58.3493         | -4.16*  | -0.94  | -0.75              | -1.67              | -3.41*              | -2.47*              |
| 25  | 53.0499  | 53.0779  | 53.0555         | 53.0637         | -2.80   | -0.82  | -0.56              | -1.38              | -2.24               | -1.42               |
| 20  | 47.9003  | 47.9216  | 47.9044         | 47.9133         | -2.13   | -0.89  | -0.41              | -1.30              | -1.72               | -1.83               |
| 15  | 42.9040  | 42.9225  | 42.9069         | 42.9170         | -1.85   | -1.01  | -0.29              | -1.30              | -1.56               | -0.55               |
| 10  | 38.0814  | 38.0975  | 38.0833         | 38.0941         | -1.61   | -1.08  | -0.19              | -1.27              | -1.42               | -0.34               |
| 5   | 33.4529  | 33.4640  | 33.4538         | 33.4635         | -1.11   | -0.97  | -0.09              | -1.06              | -1.02               | -0.05               |
| 0   | 29.0390  | 29.0392  | 29.0386         | 29.0443         | -0.02   | -0.57  | +0.04              | -0.53              | -0.06               | -0.51               |
| Symbol  | Data source  |          |                 |                 | Range of fit<br>(°C)  | rms deviation of fit<br>(mΩ <sup>-1</sup> cm <sup>-1</sup> ) |                    | chlorinity<br>(‰)  |                     |                     |
| KR  | Reeburgh—Red Sea                                     |          |                 |                 | 0 ≤ <i>t</i> ≤ 35   | 0.00013  |                    | 19.374             |                     |                     |
| KN <sub>1</sub>   | Reeburgh—Normal Water                                |          |                 |                 | -1 ≤ <i>t</i> ≤ 35  | 0.00100  |                    | 19.369             |                     |                     |
| KN <sub>2</sub>   | Reeburgh—Normal Water                                |          |                 |                 | -1 ≤ <i>t</i> ≤ 35  | 0.00212  |                    | 19.372             |                     |                     |
| PW  | Perkin and Walker<br>(Brown and Allentoft)           |          |                 |                 | 0 ≤ <i>t</i> ≤ 25   |  |                    | 19.373             |                     |                     |
| $KN_1 = 29.04433 + 0.86141t + 0.46109 \times 10^{-2} t^2 - 0.2545 \times 10^{-4} t^3$ |  |          |                 |                 |   |  |                    |                    |                     |                     |

\* Beyond range of fit.

Needing an interim expression to approximate  $C(35, t, 0)$  for temperatures greater than 25°C, Knowles (1973a) formulated a third-order polynomial equation from Reeburgh's (1965) Red Sea data (interpolated to  $Cl = 19.374‰$ ).

In the present analysis the results of this expression are compared with similar expressions formulated by Knowles (1973b) from Reeburgh's (1965) Normal Sea Water data ( $Cl = 19.369‰$  and  $Cl = 19.372‰$ ), and that formulated earlier by Perkin and Walker (1972). The results are included in Table 1.

TABLE 2. Comparison of empirical relationships for estimating  $C(35, t, 0)$  at  $t = 15°C$ .\*

| Author and source of data   | $C(35, 15, 0)$<br>(mΩ <sup>-1</sup> cm <sup>-1</sup> ) |
|---|--|
| Knowles (1973a, b)  |  |
| KR (Reeburgh Red Sea)   | 42.904   |
| KN <sub>1</sub> (Reeburgh Normal Water)                                     | 42.907   |
| KN <sub>2</sub> (Reeburgh Normal Water)                                     | 42.917   |
| Perkin and Walker (1972)<br>(Brown and Allentoft)                           | 42.923   |
| Rohde (quoted by Keyte, 1970)<br>(Thomas <i>et al.</i> )                    | 42.899   |
| Ribe and Howe (1967)<br>(Cox <i>et al.</i> and Brown and Allentoft)         | 42.917   |
| Bennett (quoted by Greenburg, 1972)   | 42.929   |
| ZDLP (Zaburdaev <i>et al.</i> , 1969)<br>(Cox <i>et al.</i> )               | 42.896   |
| Accerboni and Mosetti (1967)<br>(Cox <i>et al.</i> and Brown and Allentoft) | 42.902   |
| Daniel and Collias (1971)<br>(Thomas <i>et al.</i> )                        | 42.698   |

\* Includes results from Walker and Chapman (1973).

Perkin and Walker's specific conductance values are under the heading PW; KR, KN<sub>1</sub> and KN<sub>2</sub> come from Knowles polynomial using the coefficients computed from Reeburgh's Red Sea data and his Normal Sea Water data ( $Cl = 19.369‰$  and  $Cl = 19.372‰$ ), respectively. Those values marked with an asterisk are for temperatures beyond the range of fit of the equation and show the danger of extrapolation beyond that range.

Since the equation developed by Perkin and Walker (PW) also used Reeburgh's Red Sea data for  $t = 0°C$ , it is not surprising that the least difference with KR occurs at this temperature. A systematic increase in the differences is evident for  $t > 0°C$ , which is probably a function of the different set of data used in each case.

A comparison of the Normal Water values of KN<sub>1</sub> minus KN<sub>2</sub> indicates a non-systematic fluctuation in differences, which may, in part, be because only one set of conductivity measurements was made as a function of temperature for each Normal Water sample. Indeed, if the rms deviation of fit for each of these two data sets (as shown in Table 1) is examined, there is a strong indication that the measurements of KN<sub>2</sub> may not have been as precise as those of KN<sub>1</sub>. The differences, however, when rounded to the nearest hundredth of a millimho per centimeter (mΩ<sup>-1</sup> cm<sup>-1</sup>) are all 0.01 mΩ<sup>-1</sup> cm<sup>-1</sup> greater for KN<sub>2</sub> than for KN<sub>1</sub>, which is consistent with the fact that the salinity of KN<sub>2</sub> is 0.006‰ greater than KN<sub>1</sub>. This difference of 0.01 mΩ<sup>-1</sup> cm<sup>-1</sup> is probably significant only for the best CTD units that have an accuracy greater than ±0.01 mΩ<sup>-1</sup> cm<sup>-1</sup>.

A comparison of KR and PW with the two Normal Water samples KN<sub>1</sub> and KN<sub>2</sub> show differences that range from as small as 0.0004 mΩ<sup>-1</sup> cm<sup>-1</sup> (for KR-KN<sub>1</sub>

at  $t=0\text{C}$ ) to as large as  $-0.0224\text{ m}\Omega^{-1}\text{ cm}^{-1}$  (for  $\text{KN}_1\text{--PW}$  at  $t=25\text{C}$ ) and  $-0.0234\text{ m}\Omega^{-1}\text{ cm}^{-1}$  (for  $\text{KR--KN}_2$  at  $t=35\text{C}$ ), the latter two differences being significantly large. Generally  $\text{KR--KN}_1$  was markedly less than  $\text{KN}_1\text{--KN}_2$  and  $\text{KR--KN}_2$  was just slightly larger in magnitude, indicating that though Red Sea Water cannot be considered characteristic of normal oceanic water and the results must be used with extreme caution, diluted to 35‰ salinity it is not significantly unlike it in terms of specific conductance.

A study with a wider ranging comparison of salinity-conductivity formulas was made by Walker and Chapman (1973). Some of their results are included in Table 2, which presents values of  $C(35,15,0)$  obtained from the various  $C(35,t,0)$  formulas for  $t=15\text{C}$ . An examination of the table indicates differences even for formulas derived from the same data source. All but one of the values lie within the range  $42.896\text{ m}\Omega^{-1}\text{ cm}^{-1} \leq C(35,15,0) \leq 42.929\text{ m}\Omega^{-1}\text{ cm}^{-1}$  which indicates also the variability in salinity ( $\sim 0.03\%$ ) that could result from the use of these different formulas.

### 3. Conclusions

The results of this study re-emphasize the conclusion made earlier (Knowles, 1973a), i.e., that there is a need to have established a standard expression for the estimation of  $C(35,t,0)$  for use with CTD sensors. To make it most consistent with current salinity analysis techniques using conductive salinometers and applicable at any latitude, this expression should be derived from a series of measurements made on samples of Copenhagen Normal Water with a chlorinity near 19.374‰ over the temperature range  $-1$  to  $40\text{C}$ . To establish it as an international standard, the measurements should be under the supervision of the appropriate UNESCO committee.

It is also recommended that the conductivity ratio  $R_t$  calculated from this standard expression be used to obtain salinity using the UNESCO tables or the equation of Cox *et al.* (1967). Instrument differences and measurements made in non-standard composition seawater will still introduce errors as is the case for other techniques, but with a standard expression for  $C(35,t,0)$  at least one more variable will have been minimized.

*Acknowledgments.* Support for this study was provided by the North Carolina State University Center for Marine and Coastal Studies and by the Office of Sea Grant, NOAA, under Grants 2-35178 and 04-3-158-40, and the State of North Carolina. Thanks go, also, to Dr. John Lyman for providing additional references and critical comments pertinent to this

study and to the Department of Geosciences for encouragement and financial support.

### REFERENCES

- Accerboni, E., and F. Mosetti, 1967: A physical relationship among salinity temperature and electrical conductivity of seawater. *Boll. Geofis. Teor. Appl.*, **9**, No. 34, 87-96.
- Bradshaw, A., and K. E. Schleicher, 1965: The effect of pressure on the electrical conductance of seawater. *Deep Sea Res.*, **12**, 151-162.
- Brown, N. L., and B. Allentoft, 1966: Salinity, conductivity and temperature relationship of seawater and over the range 0-50 PPT. Final Report, ONR Contract NONr 4290 (00) M.J.O. No. 2003, Bissett-Berman, San Diego, Calif.
- Cox, R. A., F. Culkin and J. P. Riley, 1967: The electrical conductivity/chlorinity relationship in natural seawater. *Deep Sea Res.*, **14**, 203-220.
- Daniel, R. A., and E. E. Collias, 1971: Inductive conductivity probe calibration. *Proc. IEEE Intern. Conf. Engineering in the Oceanic Environment*, San Diego, Calif., 21-23 September, 16-18.
- Greenberg, D. A., 1972: Comparisons of salinity formulae used in Canada. Canada Oceanic Data Centre, M.S.B., Dept. of Environment, 25 pp.
- Hassler, B. V., 1971: The temperature-pressure dependence of ionic conductivity in sea water at temperatures in the oceanic range. M.S. thesis, U.S. Naval Postgraduate School.
- Keyte, F. K., 1970: Processing of STD magnetic tapes. B.I. Computer Note 1970-9-C, Bedford Institute Atlantic Oceanographic Lab., Dartmouth, N.S., Canada.
- Knowles, C. E., 1973a: Salinity determination for use with CTD sensors (abstract). *Trans. Amer. Geophys. Union*, **54**, 300.
- , 1973b: CTD sensors, specific conductance and the determination of salinity. Rept. No. 73-3, NCSU Center for Marine and Coastal Studies; also Office of Sea Grant, Rept. No. UNC-SG-73-16, 15 pp.
- Lyman, John, 1969: Redefinition of salinity and chlorinity. *Limnol. Oceanogr.*, **14**, 928-929.
- Park, K., and W. V. Burt, 1965: Electrolytic conductance of seawater and the salinometer. *J. Ocean. Soc. Japan*, Part 1, **21**, No. 2, 69-80; Part 2, **21**, No. 3, 124-132.
- Perkin, R. G., and E. R. Walker, 1972: Salinity calculations from *in situ* measurements. *J. Geophys. Res.*, **77**, 6618-6621.
- Reeburgh, W. S., 1965: Measurements of electrical conductivity of seawater. *J. Marine Res.*, **23**, 187-199.
- Ribe, R. L., and J. G. Howe, 1967: An empirical equation relating seawater salinity, temperature, pressure and electrical conductivity. Unpublished report, Oceanographic Instrumentation Center, Naval Oceanographic Office, Washington, D.C.
- Thomas, B. D., T. G. Thompson and C. L. Utterback, 1934: The electrical conductivity of seawater. *J. Cons. Perman. Intern. Explor. Mer*, **9**, 28-35.
- Tsurikova, A. P., and V. L. Tsurikov, 1971: On the concept of "salinity." *Oceanology*, **12**, 282-286.
- Walker, E. R., and K. D. Chapman, 1973: Salinity-conductivity formulae compared. Rept. No. 73-5, Pacific Marine Science Environment Canada, 52 pp.
- Weyl, P. K., 1964: On the change in electrical conductance of seawater with temperature. *Limnol. Oceanogr.*, **9**, 75-78.
- Wooster, W. S., A. J. Lee and G. Dietrich, 1969: Redefinition of salinity. *Deep Sea Res.*, **16**, 321-322.
- Zaburdaev, V. I., L. M. Dobruskina, E. F. Lyashenko and M. G. Poplavskaya, 1969: A method of determination of salinity from specific conductivity, temperature and pressure of seawater. *Oceanic Hydrol. Invest. Rept.*, No. 1(43), *Akad. Nauk Ukrainian S.S.R.*, Sevastopol, 5 pp.