A Comparison of Mesoscale Eddy Heat Fluxes from Observations and a High-Resolution Ocean Model Simulation of the Kuroshio Extension

STUART P. BISHOP AND FRANK O. BRYAN
National Center for Atmospheric Research,* Boulder, Colorado

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ABSTRACT

For the first time estimates of divergent eddy heat flux (DEHF) from a high-resolution (0.1°) simulation of the Parallel Ocean Program (POP) are compared with estimates made during the Kuroshio Extension System Study (KESS). The results from POP are in good agreement with KESS observations. POP captures the lateral and vertical structure of mean-to-eddy energy conversion rates, which range from 2 to 10 cm$^2$ s$^{-3}$. The dynamical mechanism of vertical coupling between the deep and upper ocean is the process responsible for DEHFs in POP and is in accordance with baroclinic instability observed in the Gulf Stream and Kuroshio Extension. Meridional eddy heat transport values are ~14% larger in POP at its maximum value. This is likely due to the more zonal path configuration in POP. The results from this study suggest that HR POP is a useful tool for estimating eddy statistics in the Kuroshio Extension region, and thereby provide guidance in the formulation and testing of eddy mixing parameterization schemes.

1. Introduction

Mesoscale eddies with length scales $O(10–100$ km) arising from instabilities of the time mean flow are a ubiquitous feature of the ocean circulation. Motions on these scales account for the majority of the kinetic energy of the flow, with maximum eddy kinetic energy (EKE) found in the regions surrounding western boundary currents and their extensions, and the Antarctic Circumpolar Current. The eddies are more than just noise; they are integral to the dynamical balances and energy and material transport throughout the ocean. Therefore, ocean models used in climate simulation must represent the effects of eddies on the mean flow and account for their transport properties. High-resolution (HR) ocean models have begun to resolve these scales (Hecht and Hasumi 2008), and a few coupled climate simulations have been conducted with ocean models of this class (McCLean et al. 2011; Kirtman et al. 2012). To quantify the uncertainty in these simulations, it is important to establish the degree of fidelity of HR ocean models in representing eddy–mean flow interaction processes. While a number of studies have evaluated the ability of HR models to reproduce the observed geographical distribution of eddy energy or near-surface fluxes of heat or momentum (e.g., McClean et al. 2006; Lenn et al. 2011), validation of the eddy-resolving models in terms of the three-dimensional structure of eddy covariances (e.g., heat flux) is difficult because of the general lack of ocean observations at sufficient spatial resolution and the long sampling requirements for statistical convergence (Flierl and McWilliams 1977).

Observations from the Kuroshio Extension System Study (KESS) offer a unique dataset to test the validity of HR model outputs. KESS was a multi-institutional field program from 2004 to 2006, comprising an observational array of current and pressure equipped inverted echo sounders (CPIES) and eight subsurface moorings. The subsurface moorings were located between the first quasi-stationary meander crest and trough east of Japan in the region of highest EKE (Jayne et al. 2009). The geostrophic currents and temperature field derived from the CPIES observations agreed well with the subsurface moorings (Donohue et al. 2010). The CPIES data was further used to estimate eddy heat flux, and this estimate agreed with estimates at the locations of the subsurface moorings (Bishop et al. 2013).

Transient eddy heat fluxes in the ocean and atmosphere have large rotational (nondivergent) components that do not play a role in eddy–mean flow interactions and...
mask the smaller, but important, divergent component. For this reason, it is necessary to distinguish between rotational and divergent components; see Marshall and Shutts (1981), Jayne and Marotzke (2002), and Fox-Kemper et al. (2003) for further discussion. The objective of this study is to compare estimates of divergent eddy heat flux (DEHF) from KESS CPIES observations with those from an eddy-resolving integration of the Parallel Ocean Program (POP) developed at Los Alamos National Laboratory. To our knowledge, this is the first time that the magnitude and three-dimensional structure of the dynamically active divergent component of simulated eddy heat fluxes have been directly evaluated using observations. In addition, we compare mechanisms responsible for generation of the eddies that give rise to DEHF.

Beyond the direct evaluation of this particular simulation, establishing the fidelity of HR models has broader implications for climate model development. Current-generation global ocean climate models do not resolve mesoscale eddies, and will not be able to do so routinely for some time. Climate models use parameterizations to include the effects of unresolved scales (e.g., Gent and McWilliams 1990, hereafter GM90) where eddy heat fluxes are represented as a flux-gradient relationship proportional to an eddy diffusivity. These parameterizations are often tested against high-resolution eddy-resolving simulations (Fox-Kemper et al. 2013). By establishing the fidelity of the eddy-resolving simulation, we can therefore provide a firmer basis for testing of a broad class of climate models.

In the next section, the model and observational datasets will be described. Additionally, the methods for estimating DEHF and a means of comparison between the two datasets will be described. The following sections will present the results of the model–observation comparison followed by a discussion and conclusions.

2. Methods

a. KESS observations

The Kuroshio Extension System Study array provided full maps twice daily of geostrophic current and temperature for 16 months from June 2004 to September 2005, after which some current and pressure equipped inverted echo sounders stopped working [the processing of the CPIES maps are documented in Donohue et al. (2010)]. Geostrophic currents determined from the CPIES separate the vertical structure into an equivalent-barotropic internal mode $u_I$ and a nearly depth-independent external mode $u_E$. The internal mode geostrophic current profiles were estimated from the mapped geopotential $\Phi$,

$$f u_I = k \times \nabla \Phi,$$

referenced to 5300 dbar where $f$ is the Coriolis parameter, $k$ is the vertical unit vector aligned with the gravitational acceleration, and $\nabla = (\partial / \partial x, \partial / \partial y)$ is the horizontal gradient operator. Measurements from the current meters and pressure gauges at the bottom provided the external mode and reference current at 5300 dbar, $u_E$, that is nearly depth independent away from steep topography (Bishop et al. 2012) to establish absolute geostrophic current profiles:

$$u = u_I + u_E.$$  

The external mode, $u_E$, may cross the front, causing the vector sum total current to veer or back with depth, which drives cross-frontal and vertical motion along sloping isopycnals (Lindstrom et al. 1997).

To match the POP model outputs described in the next section, the current and temperature maps were 5-day averaged. The cross-spectral energy of $u_E$ and $T$ at time scales less than 10 days is small (Bishop 2013, 2012), suggesting that there is little loss of energy by 5-day averaging.

b. POP model data

The model used is the Parallel Ocean Program, a general circulation model that solves the three-dimensional primitive equations. The model configuration for the simulation used in this study is the same as in Maltrud et al. (2010) and Douglass et al. (2012a,b). The model has a global tripole grid with horizontal resolution $0.1^\circ \times \cos(\text{lat})$ in both zonal and meridional directions, which is sufficient to resolve the most energetic scales of mesoscale variability. In the vertical, the model has 42 levels, with vertical spacing 10 m near the ocean surface, stretching to 250 m below 1000-m depth. The model experiment was run for 120 years with annually repeating surface atmospheric forcing, downward radiative fluxes, and precipitation from a climatology blending of the National Centers for Environmental Prediction reanalysis product and remote sensing products (Large and Yeager 2009). The outputs saved for this run were monthly-averaged potential temperature, salinity, and velocity, but 5-day-averaged variables were saved for model years 64–67. The potential temperature and horizontal velocity field from years 64–67 are used in this study because monthly outputs would underestimate a large fraction of the eddy variability observed in the 30-60-day band (Greene et al. 2012). To match the KESS observations, only the region between $32^\circ$ and $39^\circ$N, $143^\circ$ and $149^\circ$E is considered.

c. Divergent eddy heat flux

Eddy heat flux is defined as the temporal correlation between the horizontal current and temperature field,
\( \mathbf{u}^T \), where \( \mathbf{u} = (u, v) \) is the horizontal current, \( T \) is the potential temperature, a bar indicates a time mean, and primes indicate a deviation from the time mean. When studying eddy heat fluxes, it is important to distinguish between rotational (nondivergent) and divergent components (Marshall and Shutts 1981). It is the divergent component that plays a role in eddy–mean flow interactions.

In the Kuroshio Extension a very different picture emerges when the distinction between rotational and divergent fluxes is made (Bishop et al. 2013). For the CPIES dataset the eddy heat flux associated with \( u_i \), which does not advect the temperature field, is completely rotational and proportional to temperature variance contours (Marshall and Shutts 1981). The eddy heat flux due to \( u_E \), which can advect the temperature field, is responsible for driving DEHFs. However, \( u_E^T \) is not rotation free. The divergent component is then determined by removing the best-fit rotational component determined from objective analysis (OA) [see Bishop et al. (2013) and Watts and Tracey (2013, manuscript submitted to J. Phys. Oceanogr.) for details of this method]:

\[
\mathbf{u}^T \div = \mathbf{u}_E^T - \mathbf{u}_E^T^{OA}.
\]

For the POP data, \( u_E \) was chosen to be the velocity at 5125 m, which is close to the CPIES data (5300 dbar). The mean vertical shear along the jet path in the model data below 1500 m is \( O(10^{-5} \text{ s}^{-1}) \), which is \( \sim 1\% \) of the vertical shear within the thermocline, such that the deep currents are mostly uniform with depth. Then, \( u_E^T \) was estimated in a manner consistent with the model

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**Fig. 1.** Energy conversion rates, BC, at 400 m for (a) KESS [adapted from Bishop et al. (2013)] and (b) 0.1° POP. Superimposed are divergent eddy heat flux vectors every third grid point. Gray contours are mean temperature [contour interval (CI) = 1°C]. The thick gray contour is the 11°C isotherm and representative of the jet axis. (c) BC in (a) and (b) averaged longitudinally along mean temperature contours.

**Fig. 2.** Vertical structure of energy conversion rates, BC, for (a) KESS and (b) 0.1° POP as a function of longitude along the 11°C isotherm; (c) longitudinal average of (a) and (b).
It was confirmed that the model upper-ocean eddy heat flux due to the full velocity field, $u^0 T^0$, was mostly rotational and proportional to temperature variance contours (not shown), similar to observations (Bishop et al. 2013).

To determine the agreement of the POP model with the CPIES observations, two metrics will be compared: the mean-to-eddy energy conversion rates and meridional eddy heat transport (MEHT). The mechanism of vertical coupling between the deep and upper ocean, responsible for divergent eddy heat fluxes in the Kuroshio Extension and Gulf Stream, will also be tested in POP.

1) ENERGY CONVERSION

The mean-to-eddy energy conversion rates are estimated from

$$BC = -\frac{\alpha g \nabla_T \cdot \nabla T}{\Theta_z},$$

where $\alpha$ is the effective expansion coefficient $O(10^{-4} \text{C}^{-1})$ (Hall 1986; Cronin and Watts 1996; Phillips and Rintoul 2000), $g$ is the gravitational acceleration, and $\Theta_z$ is the regionally averaged potential temperature gradient. The baroclinic conversion (BC) (Cronin and Watts 1996), when positive, is a measure of the energy conversion from mean potential energy to eddy potential energy. Positive BC is indicative of baroclinic instability processes in the ocean and is the foundation for the GM90 parameterization.

2) MERIDIONAL EDDY HEAT TRANSPORT

Meridional eddy heat transport is estimated by vertically and zonally integrating the divergent meridional eddy heat flux:
\[ Q = \rho_0 C_p \int_0^L \int_{-H}^0 \overline{v' T'} dz dx, \]  

(5)

where \( \rho_0 \) is the regional depth-averaged density of 1027.5 kg m\(^{-3}\), \( C_p \) is the specific heat at constant pressure for seawater at \( \sim 4000 \text{ J kg}^{-1} \text{C}^{-1} \), and \( x \) and \( z \) are the zonal and vertical coordinates, respectively. Equation (5) is vertically integrated from 100- to 5000-m depth and zonally integrated from 143.5\(^\circ\)E to 148.5\(^\circ\)E.

3. Results

a. Energy conversion

The DEHF vectors and energy conversion rates, Eq. (4), at midthermocline depth for the KESS and POP are shown in Figs. 1a and 1b. The cross-stream DEHF vectors are also comparable with values 5–12 cm s\(^{-1}\)C. For both KESS and POP, the DEHF is directed west and south in the area south of the meander crest and east and south in the area south of the meander trough. The DEHFs north of the jet are relatively weaker in magnitude than those to the south for both. The conversion rates are comparable and predominately positive (2–10 cm\(^2\) s\(^{-3}\)) in both datasets. In both datasets, BC has a similar spatial structure with large downgradient DEHFs concentrated near the jet mean path between a crest and trough. The mean jet path in POP is shifted \( \sim 0.5^\circ \) north, which explains why the large energy conversion rates in POP are more north than the KESS observations. It is a common problem in ocean general circulation models that western boundary current (WBC) extensions (e.g., the Gulf Stream and Kuroshio Extension) tend to take a more poleward path (Chassignet and Marshall 2008).

Since there is the offset in latitudinal dependence of the energy conversion, BC was zonally averaged along mean temperature contours (Fig. 1c). The mean
temperature contours are pseudo streamlines since the flow is approximately equivalent barotropic. BC reaches a maximum along the 11°C isotherm in both datasets (4.73 $\times$ 10^{-3} cm$^2$ s$^{-3}$ in KESS and 3.46 $\times$ 10^{-3} cm$^2$ s$^{-3}$ in POP). Thus, the maximum BC is 27% smaller in POP along the 11°C isotherm, but it has a broader latitudinal structure.

The vertical structures of the energy conversion rates are also comparable. The vertical structure of BC along the axis of the jet (defined as the 11°C isotherm at 400-m depth) is shown in Fig. 2. BC reaches a maximum near 145.5°E and 400-m depth in both KESS and POP (Figs. 2a,b). It is mainly in the upper ocean (200–500-m depth) that POP underestimates BC (Fig. 2c). The vertical structure is similar on other temperature isotherms surrounding the 11°C isotherm (not shown).

b. Vertical coupling

Vertical coupling between the deep and upper ocean is the dynamical mechanism that drives DEHFs in WBC extensions and to the subsequent release of available potential energy of the mean jet (Bishop 2013; Cronin and Watts 1996). Figure 3a shows 5-day snapshots of the vertical coupling between the deep and upper ocean in POP during the formation of a cold-core ring (CCR). As the trough steepens in the midthermocline temperature field at 381 m there are deep current vectors at 5125, $u_E$, that cross the front, exhibiting very different behavior from equivalent barotropicity. These deep currents are associated with lows and highs shown by the streamfunction, $\psi_E$. Figure 3b shows that the POP deep field is leading the midthermocline temperature field by $\sim$7 days, with joint growth in the 30–60-day band (compared with 8 days in KESS; Bishop 2013). The joint growth of the deep and thermocline fields in the 30–60-day band is consistent with the canonical view of the two-layer Phillips model of baroclinic instability and has been observed in the Gulf Stream (Cronin and Watts 1996) and Kuroshio Extension (Bishop 2013; Tracey et al. 2012). The 30–60-day band was chosen because this frequency band is associated with 25%–50% of the variance in the Kuroshio Extension (Greene et al. 2012). There is significant energy in the deep ocean within the 30–60-day band in POP, accounting for 20%–30% of the variance, agreeing with observations (Fig. 4c). Figure 4b shows that the time series of $v'_E T'$, which is mostly the divergent component (Bishop et al. 2013), is also elevated during the CCR formation event. CCRs were associated with the largest DEHF events in KESS (Bishop 2013).

c. Meridional eddy heat transport

The MEHT [Eq. (5)] is shown in Fig. 5 for KESS and POP. MEHT reaches a maximum value of 0.048 PW at 35.2°N and 0.055 PW at 35.5°N for KESS and POP, respectively (1 PW = 10^{15} watts). At their respective maximum values, MEHT from POP is 14% larger than KESS. The POP maximum MEHT is shifted poleward of the KESS observations by 0.3° latitude owing to the more northerly path of the Kuroshio Extension, as mentioned earlier. This can be seen in Fig. 4a where the maximum fluxes are confined between the crest and trough at $\sim$35.5°N. The larger MEHT in POP is partly a manifestation of zonally integrating over a less steep mean trough in POP (Fig. 1). The mean trough in the path of the Kuroshio Extension has a steeper north–south extent in the KESS observations, resulting in a smaller projection of the dominantly cross-stream DEHF vectors onto the meridional direction.

4. Discussion and conclusions

The Kuroshio Extension jet axis in the 3 years of POP stayed in a more zonal path configuration within the first 1000 km east of Japan than is typically observed with satellite altimetry (seen from weekly contours of the Kuroshio Extension path, not shown). Qiu and Chen (2005) observed, from satellite altimetry, decadal variability in the path of the Kuroshio Extension axis with transitions from high (unstable) to low (stable) variability linked to external forcing owing to variations in the Pacific decadal oscillation (PDO). Despite that POP is forced with annually repeating winds, there is intrinsic interannual and decadal variability (Fig. 6) not associated
with PDO forcing. Douglass et al. (2012a) also pointed out that there is decadal variability in the formation of the large meander south of Japan. While the dynamics of these state transitions are beyond the scope of this study, the eddy statistics must be interpreted in the context of the mean flow state.

The KESS observations captured a transition from a stable to unstable path configuration in late 2004. The variability in KESS reflects the unstable period (Bishop 2013, 2012) with enhanced cold-core ring formation and ring–jet interaction. The first year of the POP output (year 64) has a CCR that forms (Fig. 3). Figure 6 shows the time series of the area average over the KESS region of vertically integrated EKE \( \int \nabla \cdot (\mathbf{u}^2 + \mathbf{v}^2) \, dz \, dA \), where \( A \) is the area]. EKE was elevated during the first year of the comparison period (model years 64–67) with the jet transitioning to a weaker meander phase thereafter, by coincidence, almost mirroring the KESS observations. See Fig. 3 in Qiu and Chen (2010) for a comparison of EKE variability from observations with Fig. 6, especially the transition from a low to high EKE state during KESS (June 2004–June 2006).

Even with these caveats, the 3 years of HR POP model data captures mean-to-eddy energy conversion rates and meridional eddy heat transport similar to observations during KESS. The horizontal and vertical structures from POP have a pleasing similarity to the KESS observations. There is crest–trough asymmetry in the baroclinic conversion along the mean path in both KESS and POP. There is strong BC upstream of the mean trough with values that agree quantitatively to within 25% with observations. The largest values are near the mean jet axis and peak in the horizontal along the 11°C isotherm and in the vertical near 400-m depth. The mechanism of vertical coupling, responsible for DEHFs in observations, is also shown to be present in POP. MEHT is comparable between KESS and POP with the peak in MEHT shifted northward in POP by \(-0.3^\circ\) latitude, which is due to the more northerly path of the Kuroshio Extension jet. MEHT from POP is also higher by \(-14\%\).

For the first time observations of divergent eddy heat fluxes with sufficient mesoscale resolution have been compared to a high-resolution ocean model simulation. The level of agreement lends confidence to climate simulations using HR POP and suggests that HR POP can be used as a tool to validate parameterizations for mesoscale eddy processes within the Kuroshio Extension region. Other similar studies would need to be done to determine the utility of the model in other dynamically important regions. However, this study lends confidence to using POP to test parameterization schemes for mesoscale eddies used in non-eddy-resolving global climate models.

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