Three-Dimensional Distribution of Turbulent Mixing in the South China Sea*

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ABSTRACT

A three-dimensional distribution of turbulent mixing in the South China Sea (SCS) is obtained for the first time, using the Gregg–Henyey–Polzin parameterization and hydrographic observations from 2005 to 2012. Results indicate that turbulent mixing generally increases with depth in the SCS, reaching the order of $10^{-2}$ m$^2$ s$^{-1}$ at depth. In the horizontal direction, turbulence is more active in the northern SCS than in the south and is more active in the east than the west. Two mixing “hotspots” are identified in the bottom water of the Luzon Strait and Zhongsha Island Chain area, where diapycnal diffusivity values are around $10^{-2}$ m$^2$ s$^{-1}$. Potential mechanisms responsible for these spatial patterns are discussed, which include internal tide, bottom bathymetry, and near-inertial energy.

1. Introduction

The South China Sea (SCS) is the largest marginal sea of the northwestern Pacific, with a wide range of bathymetric features and oceanographic processes. There are deep basins, steep continental slopes, and broad continental shelves in the SCS. In the deep basin, the existence of energetic internal tides, generated near the Luzon Strait, has been confirmed by both observations (Tian et al. 2009; Klymak et al. 2011) and numerical simulations (Niwa and Hibiya 2004; Jan et al. 2007). In the northern SCS, high-frequency nonlinear internal waves with large amplitude and high velocity, such as solitons, are widely spread. The SCS is considered one of the most active regions in the ocean for such waves (Zhao et al. 2004; Alford et al. 2010). When encountering prominent topography, such as steep slope and the Dongsha Island in the northern SCS, the northwestward-propagating internal tides evolved into internal solitary waves (Lien et al. 2005). Most energy of these nonlinear internal waves eventually dissipates to supply turbulent mixing over the broad shelf region in the northern SCS (Lien et al. 2005; Chang et al. 2006). Extensive research has been conducted during the Asian Sea International Acoustics Experiment (ASIAE), which has significantly improved our understanding on these waves and their associated processes (e.g., Duda et al. 2004; Ramp et al. 2004).

The SCS is considered a hotspot of turbulent mixing (St. Laurent 2008; Tian et al. 2009). Turbulent mixing in the SCS drives water exchange between the SCS and the Pacific (e.g., Qu et al. 2006; Zhou et al. 2014). However, studies of the turbulent mixing in the SCS are patchy in space due to limited data. Based on a fine-scale parameterization, Tian et al. (2009) examined turbulent mixing distribution along a section from the SCS to the Pacific and found the mixing beneath 1000 m in the SCS was two orders larger than in the Pacific. Through McLane Moored Profiler measurements at a mooring site over the northern SCS slope, Klymak...
et al. (2011) observed large overturning events exceeding 200 m in thickness, which were associated with turbulence dissipation as high as $10^{-5}$ Wkg$^{-1}$. Using the Thorpe-scale method, Alford et al. (2011) and Buijsman et al. (2012) revealed elevated diffusivity in the deep water of the Luzon Strait, which is considered as being modulated by internal tides. A few direct measurements from microstructure profiler are available. Over the shallow water in the shelf break region northeast of the Dongsha Island, St. Laurent (2008) found high dissipation as large as $10^{-6}$ Wkg$^{-1}$. Lozovatsky et al. (2013) examined the spatial structure and temporal variability of turbulent dissipation in limited areas of the northern SCS. Yang et al. (2014) suggested that the turbulence in the SCS is more energetic over the shelf, being an order larger than that over the slope. They also examined the temporal variability of turbulent mixing and found that internal tides and Kuroshio intrusion are the main factors driving the mixing variability over shelf and slope, respectively.

There is no doubt that these studies have improved our knowledge about the turbulent mixing in the northern SCS. However, these studies based on spatially patchy measurements during different periods have failed to provide a detailed picture of turbulent mixing in the whole SCS. Specifically, there is no report on mixing in the southern SCS to our knowledge. Because of the lack of understanding of the turbulent mixing variability in the whole SCS, the products from numerical simulations based on a simple parameterization of eddy diffusivity should be treated with caution.

The goal of this study is to present a three-dimensional (3D) structure of turbulent mixing in the whole SCS, based on hydrographic measurements. To our knowledge, it is the first time that such an attempt has been made. The paper is organized as follows. A brief description of the data and methods is presented in section 2. A 3D structure of turbulent mixing in the SCS is given in section 3. Associated mechanisms and a summary are provided in section 4.

2. Data and methods

a. Data

There were a total of 335 stations (477 casts) in the SCS from 2005 to 2012, which covered the whole SCS (Fig. 1). The months with data coverage in each year varied from March to December, and the specific data period for each field experiment is shown in Table 1. At each station, measurements of temperature, salinity, and pressure were obtained by the conductivity–temperature–depth (CTD) system using SBE 911plus, SBE 917plus, or SBE 25 (Sea-Bird Electronics). SBE 911/917 and SBE 25 CTD worked at frequencies of 24 and 8 Hz, respectively. With the pre- and postcruise calibrations, the accuracies of the CTD sensors are 0.001 psu for salinity and 0.001°C for temperature. In this study, only the downcast data are used, and the data shallower than 10 m are discarded because the CTD sensors were not stable before reaching 10 m. At 240 stations (319 casts), velocity profiles were simultaneously measured by a 300-KHz WorkHorse Sentinel lowered acoustic Doppler current profiler (LADCP, Teledyne RD Instruments). The vertical bin size was set to 10 m, the number of layers was set to 15, and the sampling frequency was set to 1 Hz. The LADCP collected relative velocities, namely, current velocities with respect to the instrument itself, with an estimated
uncertainty of 1 cm s\(^{-1}\) (based on the datasheet of Tel-edyne RD Instruments). The method we used to process the LADCP data is the inverse method, using the software from Andreas M. Thurnherr’s release, version IX_10 (Thurnherr 2010). Besides these finescale observations, microscale sampling was carried out at four stations using a turbulent ocean microstructure acquisition profiler (TurboMAP-L, JFE Advantech Co. Ltd.). The TurboMAP system was equipped with two shear probes, which sampled shear at 512 Hz. The noise level of TurboMAP for measuring dissipation rate is 10\(^{-10}\) W kg\(^{-1}\).

### b. Gregg–Henyey–Polzin parameterization

The Gregg–Henyey–Polzin (GHP) scaling based on the internal wave–wave interaction theory (Gregg et al. 2003) is employed to estimate turbulent kinetic energy dissipation rate \(\varepsilon\). This scaling can be expressed in terms of shear and/or strain as follows:

\[
\varepsilon = \varepsilon_0 N^2 \frac{\langle V_z^2 \rangle^2}{GM(V_z^2)} h_1(R_w) f(\frac{j}{N}), \quad (1)
\]

\[
\varepsilon = \varepsilon_0 N^2 \frac{\langle \xi_z^2 \rangle^2}{GM(\xi_z^2)} h_2(R_w) f(\frac{j}{N}), \quad (2)
\]

\[
h_1(R_w) = \frac{3(R_w + 1)}{2\sqrt{2R_w} \sqrt{R_w - 1}}, \quad (3)
\]

\[
h_2(R_w) = \frac{1}{6\sqrt{2}} \frac{R_w (R_w + 1)}{\sqrt{R_w - 1}} \quad \text{and} \quad (4)
\]

\[
j(f/N) = \frac{f \text{arccosh}(N/f)}{f_{30} \text{arccosh}(N/f_{30})}, \quad (5)
\]

where \(\varepsilon_0 = 6.73 \times 10^{-10}\) W kg\(^{-1}\), and \(f\) and \(N\) are the Coriolis and buoyancy frequencies, respectively (Kunze et al. 2006). The term \(R_w\) is the shear-to-strain variance ratio, defined as \(R_w = \langle V_z^2 \rangle/\langle \xi_z^2 \rangle\), where \(\langle V_z^2 \rangle\) and \(\langle \xi_z^2 \rangle\) represent the finescale internal wave shear and strain variance inferred from observations, respectively. In (1) and (2), \(GM(V_z^2)\) and \(GM(\xi_z^2)\) are the shear and strain variances inferred from the Garrett and Munk (GM) spectrum (Garrett and Munk 1972, 1975). In the GM model, an open-ocean internal wave field is constructed at a fixed buoyancy frequency of \(N_0\) (5.2 \times 10^{-3} \text{ rad s}^{-1}) at the latitude of 30\(^\circ\). Here, parameterization (1) is used for the stations where both LADCP and CTD observations are available, and parameterization (2) is used with a fixed \(R_w\) value at the other stations where only CTD observations are available. Given that \(R_w\) varies from region to region (e.g., Waterman et al. 2013), we examine its distribution at the stations where both LADCP and CTD data are available (Fig. 2). Altogether, 2987 segments were taken into consideration. The histogram indicates a peak at \(R_w = 7\), and the number of segments with \(R_w\) ranging from 5 to 12 accounts for 74% of the total number. Meanwhile, the \(h_2(R_w)\) value at \(R_w = 12\) is 5.5, about 2 times the value at \(R_w = 7\), which is 2.7. As a result, using \(R_w = 7\) will lead to uncertainty in turbulent diffusivity by a factor of 3–4, at most. Based on this, a constant value (\(R_w = 7\)) is used for simplicity when employing parameterization (2).

To quantify shear and strain variances, profiles of shear and strain with a vertical bin of 10 m were divided into half-overlapping 320-m-long segments, starting from the bottom. The term \(\langle V_z^2 \rangle\) was obtained by integrating corrected shear spectra \(S_{V_z}(k)\) from the minimum wavenumber \(k_1\) to the maximum wavenumber \(k_2\) using \(\langle V_z^2 \rangle = \int_{k_1}^{k_2} S_{V_z}(k) dk\). The shear spectral correction

\[
S_{\xi_1} = \frac{1}{\sin^4 \left(\frac{k_1 \Delta h_1}{2\pi}\right) \sin^4 \left(\frac{k_1 \Delta h_2}{2\pi}\right)}
\]

takes into account smoothing associated with range averaging, depth binning, superensemble preaveraging, and instrument tilting (Thurnherr 2012), where \(\Delta h_1\) represents the vertical bin size set for LADCP deployment, and \(\Delta h_2\) represents the vertical depth interval for the shear–strain profile. The term \(k_1\) is defined as the
reciprocal of the record length being analyzed; $k_z$ is determined as a wavenumber at which the ratio of measured shear spectrum to shear noise spectrum is 3 (Naveira Garabato et al. 2004), which mostly stays around 0.1 rad m$^{-1}$ (Fig. 3). In this study, we model the shear noise spectrum as a blue spectrum, the value of which is proportional to squared wavenumber. The root-mean-square (RMS) noise level of velocity measured by a 300-kHz LADCP is approximately 0.032 m s$^{-1}$ under optimal conditions for a large number of scatters, where $n_{\text{ping}} = 120$ is the number of pings typically averaged into each depth bin (Polzin et al. 2002). As a result, the instrument shear noise spectrum can be expressed as

$$S_{\text{noise}} = 0.032^2 \frac{k_z^2}{120} N_z S_{c1}.$$  

Strain is computed using $\xi_z = (\theta_z - \bar{\theta}_z) / \bar{\theta}_z$, where $\theta_z$ is the potential temperature gradient and $\bar{\theta}_z$ is its mean value based on a quadratic fit to each potential temperature gradient segment. Strain can also be estimated based on stratification, namely, $\xi_z = (N_z^2 - \bar{N}_z^2) / \bar{N}_z^2$. Here, we use the former to avoid bringing noise from the conductivity measurements into the strain derivation, although the strain results inferred from the two forms differ only slightly. The term $\langle \xi_z^2 \rangle$ is obtained by integrating corrected strain spectrum $S_{\xi_z}(k)S_{\xi_z}$ over the same wavenumber band as calculating $\langle V_z^2 \rangle$ using $\langle \xi_z^2 \rangle = \int_{k_1}^{k_2} S_{\xi_z}(k)S_{\xi_z} dk$. Here, the strain spectral correction due to first differencing inherent in the gradient is $S_{\xi_z} = 1 \times \text{sinc}^2[(k_z \Delta \theta_z) / 2\pi]$. When using parameterization (2), the upper integration limit of strain variance is determined by $\int_{k_1}^{k_2} S_{\xi_z} dk \leq 0.1$ (Kunze et al. 2006), since velocity data are not available.

The averaged shear and strain spectra are binned into four areas (the Luzon Strait, the northern, central, and southern SCS), associated with their corresponding GM spectra (Fig. 3). A striking feature is that the internal wave energy is elevated in the near-bottom layer in all four areas, which indicates enhanced turbulent mixing in the deep SCS. In the vertical direction, the

FIG. 3. Area-averaged spectra of vertical shear (thick curves) and strain (thin curves) in the (a) Luzon Strait, (b) the northern SCS, (c) the central SCS, and (d) the southern SCS, along with the GM model spectra (green curves). The four regions are indicated in Fig. 8f. The black, blue, and red indicate depth ranges of <500 m, 500–1500 m, and 500 m above the bottom, respectively.
energy level shows a clear enhancement from shallow water to the bottom in these areas, which indicates increased mixing with depth. The GHP scaling was initially developed for the open ocean, and its applicability in the marginal sea should be further examined due to its potential limitations (Polzin et al. 2014). The comparison of the two sets of results based on the GHP parameterization and microscale measurements by TurboMAP shows similar overall trends (Fig. 4). Although mostly both are in the same order of magnitude, there are quantitative differences between TurboMAP observations and results from the parameterization, by a factor of 2–4, among individual profiles at different depths. The parameterization has a slight tendency to overestimate the dissipation rate compared to the TurboMAP measurement; this tendency may be caused by applying the GHP parameterization in the SCS (as mentioned above about its applicability in the marginal sea). The fact that two different methods give similar turbulence levels suggests that the GHP parameterization results obtained in this study are reliable.

c. Thorpe-scale method

Thanks to the well-established relationship between the Ozmidov scale and the Thorpe scale ($L_T$; Dillon 1982), the dissipation rate $\varepsilon$ can be related to $L_T$ as follows:

$$\varepsilon = 0.64L_T^2N^3,$$  \hspace{1cm} (6)
where $L_T$ can be calculated as the RMS displacement of a parcel, and the buoyancy frequency $N$ is evaluated using the gradient of the reordered density profile. Here, the displacement is defined as the depth difference between a measured density profile and its reordered version (Finnigan et al. 2002). The run length and water mass tests proposed by Galbraith and Kelley (1996) are employed to reject spurious overturns (see appendix B for more detail). The disadvantage of the Thorpe-scale method is that overturns could not be easily detected in a shallow layer if there exists a strong stratification. Therefore, there may be turbulence even though no overturns are detected in the water column. In this study, we use this method to estimate diffusivity in the deeper water column only to avoid an underestimation of $\varepsilon$ due to overturns in the upper layer not being fully resolved. To derive diapycnal diffusivity $K$ from the GHP and Thorpe-scale inferred $\varepsilon$, the most common model of Osborn (1980) is employed, namely, $K = \Gamma(e/N^2)$, where mixing efficiency $\Gamma$ is set to 0.2.

3. Results

a. GHP scaling results

To show the spatial distribution more clearly, the profiles of dissipation rate and buoyancy frequency at all stations are first binned into a $1/4^\circ \times 1/4^\circ$ grid and then the averaged diffusivity profile at each bin is derived. The 3D structure of diapycnal diffusivity in the SCS is shown in Fig. 5. The zonal sections (Fig. 5a) illustrate that diffusivity decreases from the northern SCS to the southern SCS, except for some high diffusivity in the Zhongsha Island Chain area. The meridional sections (Fig. 5b) show that diffusivity weakens significantly from the eastern SCS to the western SCS. The 3D structure...
viewed from both zonal and meridional sections shows
an obvious feature that the turbulence is enhanced in the
deep SCS and in the whole water column of the Luzon
Strait. Figure 6 shows the depth-averaged diffusivity
in the upper layer (<500 m), intermediate layer (500–
1500 m), deep layer (>1500 m), and near-bottom layer
(500 m above the bottom). In the upper layer, re-
markably high diffusivity exists in the Luzon Strait,
which is as high as $10^{-2}$ m$^2$ s$^{-1}$. Another area with el-
evated mixing is at and north of 20$^\circ$N (and west of 120$^\circ$E),
where the magnitude of diffusivity is $10^{-3}$ m$^2$ s$^{-1}$. In
contrast, the diffusivity south of 20$^\circ$N reduces to
$10^{-4}$ m$^2$ s$^{-1}$ or even to $10^{-5}$ m$^2$ s$^{-1}$. A similar spatial
pattern exists in the intermediate layer. However, the
diffusivity in the intermediate layer is generally larger
than that in the upper layer. In the deep layer, diffusivity
is approximately one order larger than that in the in-
termediate layer. The Luzon Strait is characterized by
enhanced mixing, with diffusivity exceeding $10^{-2}$ m$^2$ s$^{-1}$.
The diffusivity values north of 20$^\circ$N and south of 20$^\circ$N
are almost at the same level in the deep layer, different
from the spatial patterns in the upper and intermediate
layers. In the near-bottom layer, diffusivity is signifi-
cantly elevated in the Zhongsha Island Chain area and
the Luzon Strait, with values of $10^{-2}$ m$^2$ s$^{-1}$ or larger.
The heightened mixing along 19$^\circ$N in the near-bottom
layer should be examined further because we have no
explanation for its presence.

The averaged diffusivity values in different layers
along zonal and meridional directions are shown in
Fig. 7. In the zonal direction, the variations in the upper
and intermediate layers have similar trends, with values
of $10^{-4}$ m$^2$ s$^{-1}$ from 110$^\circ$E to 117$^\circ$E and increasing sharply
to $10^{-2}$ m$^2$ s$^{-1}$ when reaching the Luzon Strait. The
diffusivity values in both deep and near-bottom layers
show similar variability, which increases gradually from
$10^{-5}$ to $10^{-2}$ m$^2$ s$^{-1}$ from the west to the east. The whole-
depth-averaged diffusivity mostly stays at the level of
$10^{-3}$ m$^2$ s$^{-1}$ with a rising trend toward the east, except
for some extreme values of $10^{-4}$ and $10^{-2}$ m$^2$ s$^{-1}$ at the
westernmost and easternmost ends, respectively. Just as
the variability in the zonal direction, the variations in
the upper and intermediate layers, or those in the deep
and near-bottom layers, are similar in the meridional

![Fig. 6. Maps of depth-averaged diffusivity (m$^2$ s$^{-1}$; logarithmic scale) for the (a) upper layer (0-500 m), (b) intermediate layer (500-1500 m), (c) deep layer (>1500 m), and (d) near-bottom layer (500 m above the bottom).]
direction. The diffusivity in the upper and intermediate layers is weakened by one order from $10^{-3}$ m$^2$ s$^{-1}$ in the north to $10^{-4}$ m$^2$ s$^{-1}$ in the south. In the deep and near-bottom layers, significantly intensified turbulence activity exists between 13$^\circ$ and 17$^\circ$N, with enhanced diffusivity exceeding $10^{-2}$ m$^2$ s$^{-1}$ in the near-bottom layer. When averaged in the whole water column, diffusivity displays a decreasing trend from the north to the south. Four regions, namely, the Luzon Strait and the northern, central, and southern SCS, are selected to further examine vertical distributions of area-averaged dissipation, buoyancy frequency, and diffusivity derived from these two mean variables in the SCS (Fig. 8). A common feature of the four regions is that diffusivity increases with depth. A striking diffusivity profile is found in the Luzon Strait, with values ranging from $5 \times 10^{-3}$ to $4 \times 10^{-2}$ m$^2$ s$^{-1}$, much larger than those in the other three areas. Such large diffusivity in the Luzon Strait was reported before. For example, Alford et al. (2011) showed diffusivity as large as $3 \times 10^{-2}$ m$^2$ s$^{-1}$ around 2000-m depth in the Luzon Strait, comparable with our value of $1 \times 10^{-2}$ m$^2$ s$^{-1}$ at the same depth. However, our estimated diffusivity in the upper layer is higher than that of Alford et al. (2011), which may be caused by seasonal variability because the observations of Alford et al. (2011) were from summer, while our measurements include two winters. The associated dissipation rate is about $2 \times 10^{-8}$ W kg$^{-1}$ below 2000 m in the Luzon Strait, also exceeding the levels in the other regions. Among the other three regions, diffusivity at a depth shallower than 2500 m is the strongest in the northern SCS and is the weakest in the southern SCS until reaching 3100 m. Deeper than 2500 m, diffusivity in the central SCS becomes the largest; below 3100 m, the values in the northern SCS become the smallest. The dissipation rates below 2000 m mostly stay around $10^{-9}$ W kg$^{-1}$. The basin-averaged diffusivity profile reveals that the mixing level is larger than $10^{-3}$ m$^2$ s$^{-1}$ below 1400 m and even reaches $10^{-2}$ m$^2$ s$^{-1}$ below 3300 m. This suggests enhanced turbulent mixing in the deep SCS, which supports the finding of Tian et al. (2009).

b. Thorpe-scale results

An example of overturn with a depth range from 790 to 890 m is identified at 21.11$^\circ$N, 117.84$^\circ$E in the northern SCS, where the water depth is 1000 m; 12 profiles of LADCP/CTD were collected during 34 h (Figs. 9a,b). Potential temperature and salinity in the water column.
FIG. 8. (a)–(d) Area-averaged profiles of dissipation rate $\varepsilon$ (W kg$^{-1}$), buoyancy frequency $N^2$ (s$^{-2}$) and diffusivity $K$ (m$^2$ s$^{-1}$) in the four regions as indicated in (f). Note the colors in (a)–(d) are the same as the colors used for boxes in (f). (e) The averaged profiles over the whole SCS. We use the logarithmic scale for the $x$ axis in (a)–(e), with error bars to indicate the uncertainty of standard deviation. In (a)–(e) the top $x$-axis is for $K$ and the bottom $x$-axis is for $\varepsilon$ and $N^2$. 
were nearly uniform in the vertical. The original and sorted potential density profiles show a remarkable overturn with denser water overlying lighter water. At a similar location, Klymak et al. (2011) found even larger overturning events with a thickness exceeding 200 m, twice that shown in Figs. 9a and 9b. The time series of inferred diffusivity at this location are further examined (Figs. 9c–e) using Thorpe-scale estimates as well as zonal and meridional velocities. The frequency of the signals was predominantly diurnal. Turbulent mixing was elevated when the tidal current reached its maximum, and a correlation coefficient between them is 0.73.
Similar results were reported by Alford and Pinkel (2000) and by Levine and Boyd (2006) near California and Hawaii, respectively.

The number of profiles used in averaging, overturn number, and the maximum thickness of the overturns at each grid in the near-bottom layer of the SCS are given in Figs. 10a, 10b, and 10c, respectively. The overturn number varied spatially, mostly ranging from 10 to 40. A large number of overturns occurred in the Luzon Strait and its adjacent northern SCS, as well as in the Zhongsha Island Chain, with the number exceeding 15. The maximum thickness of the detected overturns was mostly between 20 and 180 m. There were remarkable overturns with thicknesses between 140 and 180 m in the Luzon Strait, where Alford et al. (2011) reported a striking overturn with thickness larger than 500 m. Some large overturns with thicknesses of 80 m or larger exist in the northern SCS, and in the Zhongsha Island Chain as well. Compared with the neighboring area of the Pacific, where the thickness of the largest overturn was mostly smaller than 20 m (Yang et al. 2014), the overturns in the SCS were rather energetic. These results support the conclusion of Tian et al. (2009) that the turbulent mixing in the SCS is much stronger than that in the Pacific. The spatial pattern of diffusivity in the near-bottom layer is reconstructed from Thorpe-scale estimates (Fig. 10d). The result is the averaged diffusivity based on many overturns (Fig. 10b) with substantial size (Fig. 10c), not just from one individual profile. It shows enhanced mixing in the SCS deep basin. Two areas with significantly elevated diffusivity are the Luzon Strait and the Zhongsha Island Chain, with maximum values of $10^{-2} \text{m}^2\text{s}^{-1}$ or larger. This structure agrees well with the GHP scaling results; however, there is a discrepancy in magnitude by a factor of 2–3 between these two methods (Fig. 11). Examining variations of the two results with buoyancy frequency, the correlation between them reaches 0.72. The discrepancies mainly occurred in the low stratification regions, where both GHP parameterization and Thorpe-scale method have relatively high noise. Nevertheless, the diffusivity estimates based on GHP scaling and Thorpe-scale estimates yield similar spatial patterns, which add to our confidence in the diffusivity map obtained in this study.

Fig. 10. Maps of (a) the number of profiles used in averaging, (b) mean number of overturns, (c) the maximum overturn thickness (m), and (d) the depth-averaged diffusivity inferred from the Thorpe-scale estimate ($\text{m}^2\text{s}^{-1}$) for the near-bottom layer. A logarithmic scale is used for diffusivity in (d).
4. Discussion and summary

a. The Luzon Strait

The Luzon Strait is an area with vigorous turbulence in almost the entire water column. Prominent topographic features include two parallel north–south-oriented ridges, interacting effectively with normally incident barotropic tides. This promotes energy conversion from barotropic tides to internal tides. Niwa and Hibiya (2004) revealed that 14-GW M2 barotropic energy flux (one-quarter of the total) is converted to M2 internal tides, and about half, or 6.6 GW, is dissipated to furnish local turbulent dissipation before radiating away from the Luzon Strait. Buijsman et al. (2012) suggested high-mode turbulent lee waves account for the elevated dissipation in the deep water of the Luzon Strait; they also pointed out the key role of the double ridges in lee-wave generation. Yang et al. (2014) noted that the shear instability associated with Kuroshio intrusion plays a nonnegligible role in strengthening the turbulent mixing in the Luzon Strait. These factors may lead to the remarkably high diffusivity in the Luzon Strait inferred in this study.

b. The northern South China Sea

There are some potential candidates in the northern SCS that can contribute to the turbulent mixing in the region, such as internal solitary waves, internal tides, and near-inertial internal waves. The northern SCS has a high occurrence area of internal solitary waves, which mainly exist north of 20°N, especially around the Dongsha Island (Zhao et al. 2004). The solitary waves in the deep basin are associated with relatively small shear and exhibit weak turbulence (e.g., Klymak et al. 2006). They can, however, trigger mixing events on the base of preexisting background shears (Pinkel 2000). When propagating west to the shelf and slope of the northern SCS, solitary waves become dissipative, exhibit strong shears, and generate turbulence due to shear instability (e.g., Xu et al. 2012). This is consistent with the diffusivity pattern in Fig. 6a, in which the values around the Dongsha Island are 3–4 times larger than those east of the island in the upper layer. Based on the mooring observations in this area, Lien et al. (2005, 2014) revealed a dissipation rate as high as $1.5 \times 10^{-4}$ W kg$^{-1}$ caused by solitary waves. Compared to propagating solitary waves, the contribution of locally generated internal waves is small. For example, Klymak et al. (2011) found that the generation of local internal waves is less than one-tenth of the incoming waves.

The energy of internal tides generated from the Luzon Strait and entering the northern SCS is also an important source to sustain the high mixing away from the shelf. The slope in the northern SCS is supercritical with respect to both diurnal and semidiurnal tides, although the supercritical region for the semidiurnal tides is narrower than that for the diurnal tides (Fig. 12). Here, the slope criticality $S/\alpha$ is defined as the ratio of local topographic slope, to the energy propagation slope of a radiated tidal beam $\alpha = \sqrt{(\omega^2 - f^2)/(N^2 - \omega^2)}$. In this calculation, the bathymetry data are from the Smith–Sandwell database (Smith and Sandwell 1997), and stratification is calculated using the annual temperature and salinity data of the WOA13.
The stratification data are obtained from the climatological dataset of the World Ocean Atlas 2013 (WOA13; available online at https://www.nodc.noaa.gov/cgi-bin/OC5/woa13/woa13.pl); \( \omega \) and \( f \) are tidal frequency and Coriolis frequency, respectively. Because of this kind of criticality, the slope in the northern SCS acts as a barrier, that is, most incoming energy is reflected back, with the higher vertical modes becoming gradually dominant. As a result, the energy is trapped in the deep basin of the northern SCS and eventually dissipates to furnish the mixing there. Klymak et al. (2011) estimated that one-third of the incoming diurnal tidal energy is reflected into the SCS basin and used to facilitate turbulent mixing. Consistent with the above-mentioned processes, Tian et al. (2009) made an estimate based on the assumption that 8-GW internal tide energy are dissipated in the SCS and deduced a diffusivity value of \( 10^{-3} \text{m}^2\text{s}^{-1} \) in the deep water of the SCS.

The ocean can obtain energy from wind by generating near-inertial internal waves, which enter the surface mixed layer, propagate downward, and dissipate in the interior eventually, as noted by Alford et al. (2012). Comparison between the climatological near-inertial energy level (Fig. 13a) and the diffusivity in the upper layer (Fig. 13b) shows similar patterns. The near-inertial energy in the northern SCS, say at 20\(^\circ\)N, is notably higher than that in the southern SCS, say at 14\(^\circ\)N. The energy difference between the two latitudes is almost one order in magnitude. This agrees well with the diffusivity map in the upper layer, that is, the higher the near-inertial energy, the higher the diffusivity, implying the contribution from wind to the diffusivity in the upper layer. In summary, these three kinds of internal waves (internal solitary waves, internal tides, and near-inertial internal waves) are important factors driving the high-level mixing in the northern SCS.

c. The Zhongsha Island Chain

Figure 14 compares zonally averaged diffusivity, bottom roughness, shear variance, and strain variance in the near-bottom layer of the central SCS. Bottom roughness is defined as the bathymetry variance calculated in bins of \( \frac{1}{8}^\circ \times \frac{1}{8}^\circ \), which is considered a suitable spatial scale for internal tide generation by St. Laurent and Garrett (2002). The zonally averaged diffusivity peaks at about \( 5 \times 10^{-2} \text{m}^2\text{s}^{-1} \) around 15.5\(^\circ\)N, where a series of small ridges are present along the east–west direction. Bathymetry roughness reaches its maximum of \( 5 \times 10^5 \text{m}^2 \) across the ridges, where \( V_z^2 \) and \( N^2 \xi_z^2 \) are simultaneously elevated to \( 2.5 \times 10^{-5} \) and \( 3.5 \times 10^{-5} \text{s}^{-2} \), respectively. This structure is similar to that over the Hawaiian Ridge reported by Rudnick et al. (2003); however, their measured diffusivity was \( 3 \times 10^{-4} \text{m}^2\text{s}^{-1} \) across the ridge, about two orders smaller than that in our study. It is reasonable to ask what kind of energy source could support such elevated turbulent mixing in the central SCS. Zhao (2014) examined the internal tide behavior in the SCS based on multiple satellite observations. His results suggested that \( K_1 \) and \( O_1 \) internal tides generated in the Luzon Strait could propagate to the Zhongsha Island Chain area (one of the high mixing areas in our study) along the central SCS deep basin, but their magnitudes in the central SCS are clearly weaker than those near the generation site. The \( M_2 \) internal tides propagate over a shorter distance compared to the diurnal tides and are hardly detected in the Zhongsha Island Chain area. As a result, the total

\[ V_z^2 \]
internal tide energy flux in the Zhongsha Island Chain area is significantly weaker than that near the Luzon Strait. The diffusivity values in these two areas, however, are comparable in magnitude. One likely explanation is that the internal tides generated in the Zhongsha Island Chain area are dissipated locally.

Let us take two boxes, which represent the Luzon Strait and Zhongsha Island Chain area, respectively, to analyze their bathymetries and barotropic tides (Fig. 15a). Slope spectra are computed along zonal and meridional directions in the Luzon Strait and Zhongsha Island Chain area, respectively, since the major axes of the tidal ellipse are almost in the zonal and meridional directions in these two areas (Figs. 15b,c). The slope spectra in these two regions are distinctly different. In the Luzon Strait, the mean slope spectrum has a high level at small wavenumbers ($<1 \times 10^{-4}\text{rad m}^{-1}$). In contrast, the mean slope spectrum in the Zhongsha Island Chain area peaks around the wavenumber of $2 \times 10^{-4}\text{rad m}^{-1}$ and tapers off at lower and higher wavenumbers. This implies the internal tides with low vertical modes prevail in the Luzon Strait, which is supported by field measurements (e.g., Alford et al. 2011) and numerical simulations (e.g., Jan et al. 2008). In the Zhongsha Island Chain area, however, the internal tides with high vertical modes would prevail. Here, the equivalent mode number is toward the diurnal internal tide, which is determined by the modal dispersion relation given by $k_j = [(j\pi)H][\{(\alpha^2 - f^2)/(N^2 - \omega^2)\}]^{1/2}$, where $j$ is the mode number; $k_j$ is the corresponding horizontal wavenumber; $H$ and $f$ are the mean water depth and Coriolis frequency in the selected region, respectively; and $\omega$ is the diurnal frequency. The equivalent mode numbers for the diurnal tide are indicated at the top of Figs. 15b and 15c. The buoyancy frequency used is the averaged value from our measurements. We also examined the barotropic tidal information from the Oregon State University Tidal Data Inversion (Egbert and Ray 2003; http://volkov.oce.orst.edu/tides/). The results show that the diurnal tides prevail in the Zhongsha Island Chain area, and the major axes are a quarter to a third of their counterparts in the Luzon Strait (Fig. 15d). However, the generated internal tides available for local turbulent dissipation are possibly comparable in these two areas, since part of the generated lower-mode internal tides in the Luzon Strait radiates away and enters the northern SCS (Niwa and Hibiya 2004); therefore, this part does not contribute crucially to the local mixing in the Luzon Strait. In contrast, most higher-mode internal tides generated in the Zhongsha Island Chain area are likely dissipated locally to furnish mixing. Clearly, this inference needs to be confirmed when time series observations over a longer period in the Zhongsha Island Chain area become available.

d. Vertical velocity

Based on the diffusivity results inferred from the GHP parameterization, vertical velocity $w_e$ can be obtained from a vertical advective–diffusive balance model (Munk 1966; Munk and Wunsch 1998). This model is expressed as $w_e(\partial \rho/\partial z) = \partial \rho \partial z[K(\partial \rho/\partial z)]$, and we used its incarnation of $w_e = (0.2/\langle N^2 \rangle)(\partial \rho / \partial z)$. Here, the cubic fits to logarithmic stratification and dissipation rate profiles are used to calculate $w_e$. First, the averaged dissipation and buoyancy frequency profiles yield one vertical velocity profile on the same grid as diffusivity shown in Fig. 6. Then, $w_e$ at a specific depth is obtained by averaging all the vertical velocity values at that depth over the whole SCS. The errors of derived $w_e$ are given by the uncertainty of standard deviation. Note that this velocity does not take into account any upward flows driven by wind stress curl and others, only those resulting from turbulent mixing. A persistent upwelling exists in the deep water of the SCS, which exceeds $30\text{cm day}^{-1}$ below $2700\text{m}$, and becomes weaker at shallower depth.
(Fig. 16). Maximum diapycnal upwelling of 46 cm day\(^{-1}\) is found around 3300 m. This upwelling is consistent with the deep-water exchange in the SCS reported by Tian et al. (2006) and Zhou et al. (2014) based on observations. These two studies noted the deep water of the SCS comes from the Pacific via the Luzon Strait due to density difference and moves upward by the heightened mixing in the deep SCS.

We also obtained the vertical motion \(w_{\text{ECCO}}\) from a dynamically and kinematically consistent ocean state estimate system [Estimating the Circulation and Climate of the Ocean (ECCO) version 4, release 1; available at http://www.ecco-group.org/index.htm]. The ECCO product is the result of least squares fitting the Massachusetts Institute of Technology General Circulation Model (MITgcm; Marshall et al. 1997) to a huge collection of global-scale observations (about \(2 \times 10^9\) observational points). The vertical velocity is an output in the ECCO product, so we directly average it in the same way as we treated the balance model inferred \(w_{\beta}\) and compare the two. The vertical profile of \(w_{\text{ECCO}}\) shares a similar trend as that of \(w_{\beta}\), and their discrepancies are generally less than 10 cm day\(^{-1}\). On average, the upwelling speeds in the SCS deep water are 32 ± 5 cm day\(^{-1}\) and 28 cm day\(^{-1}\) based on \(w_{\beta}\) and \(w_{\text{ECCO}}\), respectively. Tian et al. (2006) and Yang et al. (2010) measured the Luzon Strait transport and found the Pacific water consistently entering the SCS below 1500 m, with a transport \(Q\) of 2.0 Sv. Let \(A\) be the area of the SCS at 1500 m, which is estimated to be \(8.3 \times 10^{11}\) m\(^2\). An
estimate of the average upwelling velocity of the deep water in the SCS can then be made using \( w = \frac{Q}{A} = 21 \text{ cm day}^{-1} \). Qu et al. (2006) applied a hydraulic theory to estimate \( Q \) and gave a rough estimate of upwelling speed at 24 cm day\(^{-1}\). These estimates are all comparable, which suggests that the deep water in the SCS moves upward much faster than the deep water in the open ocean (on the order of 0.1 cm day\(^{-1}\); e.g., Kunze et al. 2006) due to enhanced mixing in the deep SCS.

**e. Summary**

The turbulent mixing in the SCS was examined based on the GHP finescale parameterization, and a 3D structure of diapycnal diffusivity was obtained for the first time. The results suggest that the mixing level in the SCS generally increases with depth, reaching the order of \( 10^{-2} \text{ m}^2\text{s}^{-1} \) at depth. On average, the turbulence in the SCS becomes more active from south to north and from west to the east. In addition, two mixing “hotspots” were identified in the bottom water in the Luzon Strait and the Zhongsha Island Chain area, where diapycnal diffusivity is around \( 3 \times 10^{-2} \text{ m}^2\text{s}^{-1} \).

Potential mechanisms responsible for these spatial patterns were discussed, such as internal tides, bottom bathymetry, and near-inertial energy.

Using the hydrographic measurements over 8 yr, the spatial structure of the diffusivity in the SCS was investigated. Note that the results presented here did not take into account temporal variability at both seasonal and annual time scales. This may bias these spatial patterns. Fortunately, the results at most grids were obtained by averaging several observations from different cruises, which may reduce this bias. Moreover, the GHP parameterization may induce errors to the inferred diffusivity values, since the parameterization may not be completely appropriate for the SCS due to its potential limitations (Polzin et al. 2014). For example, Klymak et al. (2008) reported that the diffusivity predicted by the parameterization was smaller than that directly observed near the topography. We are, however, confident that the order of magnitude of the estimates and the 3D spatial pattern of turbulent mixing in the SCS reported here are robust and reliable, as the diffusivity results were confirmed by other independent methods (sections 2b and 3b; Fig. S1 in the online supplemental information). We hope the mixing patterns unveiled in this study will be helpful for improving mixing configuration in the numerical model used for simulating a realistic ocean state in the SCS. Research on temporal variability of turbulent mixing in the SCS needs to be carried out when more data become available.

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APPENDIX A

Velocity Derived from LADCP Observations

The LADCP used in the field experiment is WorkHorse Sentinel, manufactured by Teledyne RD Instruments. Its transducer frequency is 300 kHz. The datasheet of Teledyne RD Instruments states that the velocity accuracy is “0.5% of the water velocity relative to ADCP ±0.5 cm s^{-1}.” However, this uncertainty is for the relative water velocity with respect to the ADCP itself, not the absolute water velocity with respect to a fixed point on Earth. The uncertainty of absolute velocity is difficult to estimate accurately due to many factors, such as tilt, tilt difference, and processing method, among others (Firing 1998; Visbeck 2002). Both Firing (1998) and King et al. (2001) reported that the accuracy was a few centimeters per second except when backscattering was very low. A value of ∼3 cm s^{-1} was given for the accuracy by Thurnherr (2010). Our diffusivity results, however, are not sensitive to the accuracy of absolute velocity, since the shear involved in the diffusivity calculation can be obtained from the relative velocity profile, which has a higher accuracy.

The method we used to process the LADCP data is the inverse method. The software is from Andreas M. Thurnherr’s release, version IX_10. Some key parameters we used to conduct data quality control when using this software are given below. First, we discarded the data when the tilt and the tilt difference between the adjacent pings exceed 22° and 4°, respectively. Second, the limits of LADCP internal error velocity, horizontal velocity, and the vertical velocity deviation from the median of all bins in each ensemble were set to 0.5, 2.5, and 0.2 m s^{-1}, respectively. The LADCP measurement was discarded if any of these limits were not met. Finally, side-lobe contaminated data near seabed and surface were not used in the calculation. As an example, one measurement is shown in Fig. A1; there are 6400 effective ensembles in all, and 1011 of them are discarded after quality control. Figure A2 shows the final velocity profile and the comparison with shipboard ADCP in the upper 600 m. The results suggest that the velocity profiles after quality control are more consistent with the shipboard ADCP observation than before quality control. For most of a water column (300–1300 m), biases exist between the two velocity profiles, but these biases

![Fig. A2. (a) Zonal u and (b) meridional v components of absolute velocity. The blue curves are the velocity measurements from shipboard ADCP, which is WorkHorse Long Ranger 75 kHz manufactured by Teledyne RD Instruments. The red and magenta curves are the derived velocity profiles from LADCP with and without quality control, respectively.](unnamed)
do not affect the shear significantly since they change little with depth.

APPENDIX B

Diffusivity Estimation from CTD Observations

The essence of diffusivity estimation from CTD measurements is to search for a reliable depth inversion from the original and sorted density profiles. One needs to first remove spurious pressure fluctuations in the CTD record due to cable shaking or ship movement. To remove these spikes, especially those in salinity, we did time averaging for the observed temperature and salinity. The CTD systems we used are SBE 911plus, SBE 917plus, and SBE 25, manufactured by Sea-Bird Electronics. SBE 911/917plus have a sampling rate of 24 Hz, and SBE 25 has a sampling rate of 8 Hz. As a result, we constructed a temporal average of 0.25 s for the measurements from SBE 911/917 and of 0.5 s for the measurements from SBE 25. The normal descending velocity of CTD is about 1 m s\(^{-1}\), which implies that the vertical resolution of the averaged record is about 0.25 m for SBE 911/917 and about 0.5 m for SBE 25.

An overturn can be found by comparing the original density profile (with depth \(z_o\)) and the sorted one (with depth of \(z_s\)). The associated Thorpe scale is calculated based on the difference between \(z_o\) and \(z_s\), using \(L_T = \sqrt{(z_o - z_s)^2}\). The next step is to remove spurious overturns using two tests, following Galbraith and Kelley (1996). The first is the run length test, which is useful in detecting spurious density inversion caused by random noises. To increase the sample size and hence to

![Fig. B1. Examples of the (top) run length test and (bottom) water mass test. (left) \(T-S\) diagrams are shown, with the thin curves indicating failed tests. (right) The corresponding potential density profiles and the rejected overturns based on the tests are shown, where the black and red curves are original and sorted potential density profiles, respectively.](image-url)
improve the accuracy of the cutoff of the run length in statistics, we conducted this test for all CTD casts used in this study. Here, the cutoff of the run length is set to seven. Besides the random noise, the systematic noise, such as that resulting from mismatches in time responses of temperature and conductivity probes, could cause density inversion, which is not a true mixing event (Galbraith and Kelley 1996). The second test, namely, the water mass test, was conducted to resolve this issue. A parameter $\xi$ was employed during the test, which is the maximum of nondimensional deviations of $\xi_S$ and $\xi_T$, where $\xi_S$ indicates the salinity-induced density deviation between observed and linearly fitted values, and $\xi_T$ is the temperature-induced density deviation. A critical value of $\xi = 0.6$ is used in this study. Examples of these two tests are shown in Fig. B1.

A few factors, such as instrument accuracy level, local stratification, and vertical size of the overturn, could influence the accuracy of the Thorpe scale–derived diffusivity, as noted by Frants et al. (2013). They used the following approach to assess the reliability of the Thorpe-scale inferred diffusivity, that is, to examine the difference between the minimum resolvable overturn size and the dominated overturn size. The comparison performed in the near-bottom layer of the Luzon Strait is shown in Fig. B2, which suggests there was a significant difference of 50 m, implying that the Thorpe scale–derived diffusivity in our study is reliable.

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