Lifecycle of a Submesoscale Front Birthed from a Nearshore Internal Bore

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ABSTRACT: The ocean is home to many different submesoscale phenomena, including internal waves, fronts, and gravity currents. Each of these processes entails complex nonlinear dynamics, even in isolation. Here we present shipboard, moored, and remote observations of a submesoscale gravity current front created by a shoaling internal tidal bore in the coastal ocean. The internal bore is observed to flatten as it shoals, leaving behind a gravity current front that propagates significantly slower than the bore. We posit that the generation and separation of the front from the bore is related to particular stratification ahead of the bore, which allows the bore to reach the maximum possible internal wave speed. After the front is calved from the bore, it is observed to propagate as a gravity current for approximately 4 h, with associated elevated turbulent dissipation rates. A strong cross-shore gradient of alongshore velocity creates enhanced vertical vorticity (Rossby number $\sim 40$) that remains locked with the front. Lateral shear instabilities develop along the front and may hasten its demise.

KEYWORDS: Ocean; Continental shelf/slope; Ageostrophic circulations; Density currents; Diapycnal mixing; Frontogenesis/frontolysis; Fronts; Gravity waves; Inertia–gravity waves; Instability; Internal waves; Mixing; Nonlinear dynamics; Turbulence

1. Introduction

The inner continental shelf is home to a variety of lively phenomena, from wind-driven flows to nonlinear internal tides, to jets and fronts, to submesoscale instabilities, to surface and bottom boundary layers, to energetic turbulence (Kumar et al. 2021). Together these processes govern the distribution of heat, freshwater, momentum, pollutants, and biologically essential nutrients (Boehm et al. 2017). Most work to date has explored the dynamical underpinnings of each of these phenomena relatively independently; they are then superimposed and considered on their own. An increasingly clear picture is that internal waves and submesoscale features occupy similar length and time scales, and thus may interact in modestly or even strongly nonlinear ways (e.g., Thomas 2017).

Here we present a novel example of a near-surface submesoscale front, with some characteristics of a buoyant gravity current, that appears to be generated by a shoaling nonlinear internal bore. Before presenting our observations and discussing their interpretation, we motivate the present study by briefly reviewing the context for internal tidal bores, sharp fronts, and gravity currents.

Internal tides are found throughout the coastal oceans globally and are frequently observed propagating onshore from the shelf-break (Ramp et al. 2004; Scotti et al. 2007; Kelly and Nash 2010; Suanda and Barth 2015). Dynamically, internal waves involve interplay between baroclinic density/pressure forces, buoyancy forces in stratified water, and Coriolis, which combine to propagate a wave forward (Gill 1982). As internal tides propagate into shallower water depths, wave amplitude grows, as does the role of the quadratic advective term in the momentum equation, and the tides often develop a nonlinear character. Their nonlinear evolution can lead to various internal wave shapes, including steep bores, undular internal waves (or trains of high-frequency waves), and solitary internal waves (i.e., solitons). The details of how these internal waves evolve depend on their amplitude and waveguide factors, such as the ambient stratification, background currents, and total water depth (Vlasenko and Hutter 2002; Stastna and Lamb 2002; Scotti...
et al. 2008; McSweeney et al. 2020a). Previous analyses of the mooring data presented in this paper provide insight about the regional internal wave field (McSweeney et al. 2020a,b). Large-amplitude internal bores propagate into the region approximately every 6 h, possibly due to the presence of multiple generation sites or the formation of multiple bores within a shoaling semidiurnal internal tide (Lamb 1994; Grimshaw et al. 2014; McSweeney et al. 2020a).

Some of the internal bores observed in the region described by McSweeney et al. (2020a) become nonlinear enough that their leading isopycnals outcrop (Figs. 5, 11, and 12 in McSweeney et al. 2020a), a behavior that has also been observed for shoaling internal bores at other sites (Scotti and Pineda 2004; Thomas et al. 2016; Walter et al. 2016). The initial steep wave front is often followed by trailing high-frequency waves. The overall shape, and detailed partition into a steep bore plus high-frequency waves, evolves substantially as the waves shoal between the 100- and 10-m isobaths (McSweeney et al. 2020a,b). The specific evolution of bore shape largely depends on the stratification ahead of a bore and the vertical position of the pycnocline–water column characteristics that are equally influenced by subtidal modulation and higher-frequency variability from the frequent passage of the internal bores. The nonlinear shoaling dynamics of internal tides play an important role in providing the power for and setting the cross-shelf and vertical patterns of enhanced turbulent mixing (MacKinnon and Gregg 2003; Moum et al. 2003a; Shroyer et al. 2010; Grimshaw et al. 2010; Becherer et al. 2020).

At the same time, a parallel life cycle exists that links mesoscale (often wind-driven) large-scale currents, submesoscale instabilities at their edges, and sharp and often turbulent fronts. Near the ocean surface, submesoscale fronts are often created through confluent flow (Stone 1966; Hoskins 1974; Mahadevan and Tandon 2006; McWilliams 2016). Though secondary circulations act to steepen the front through frontogenesis, in this process rotation still plays an order one role, balancing the pressure gradient force. As horizontal scales shrink, the importance of rotation fades. Warner et al. (2018) observe fronts on the edges of tropical instability waves, created through confluence. As the fronts steepen (and in their case moves closer to the equator where Coriolis weakens), the dynamical balance switches to that of a propagating gravity current, with baroclinic pressure and nonlinear advection being the first-order terms. Similarly, Pham and Sarkar (2018) simulate a density front that initially is in thermal wind balance. The secondary circulations that develop as part of frontogenesis become strong enough to switch it into the regime of propagating gravity current. Although gravity currents are more well known from river outflows (e.g., Nash et al. 2005; Jurisa et al. 2016; Solodoch et al. 2020), these examples show that other frontogenetic processes can ultimately end with unbalanced gravity currents as well. Recent work by Barkan et al. (2019) explores the theoretical motivation by which “runaway” frontogenesis forgets the context that provided the initial instigation, with similar end-stage unbalanced situations arising from multiple initial situations.

These two dynamical pathways [1) steepening internal tides and 2) submesoscale fronts and gravity currents] are generally treated separately, but here we present observations of nonlinear internal bores, fronts and gravity currents occupying the same space and time scales, which results in energy passing from one to the other. There is a limited body of previous work considering this type of interaction. White and Helfrich (2012) explore the coexistence of, and interactions between, gravity currents and internal bores, using a combination of hydraulic control theory and numerics. Their work provides a useful framework for interpreting our observations and is discussed in more detail below.

The observations presented here were collected as part of the Office of Naval Research Inner Shelf Dynamics Experiment (ISDE) (Lerczak et al. 2019; Kumar et al. 2021). The overall project was designed to explore the superposition, intersection, and interactions between a wide range of inner-shelf phenomena (Kumar et al. 2021). Here we utilize shipboard, mooring, and remote sensing data to detail the generation of a gravity current front from a shoaling internal bore and the front’s subsequent evolution and destruction.

2. Methods

The ISDE was a large, coordinated field program that collected both in situ and remote sensing observations in combination with numerical modeling over a 50-km stretch of coast in the vicinity of Point Sal, California (Lerczak et al. 2019). The experiment occurred from late August to early November 2017 (with a pilot experiment in 2015; Colosi et al. 2018) in water depths ranging from 5 to 150 m. The field campaign included moored time series measurements, ship and small boat surveys, surface drifters, and remote sensing from land, airplanes, and space [see Kumar et al. (2021) and Waterhouse et al. (2020) for more information]. The observations described herein are a subset of ISDE observations, obtained on 15 September 2017.

Shipboard observations of the front discussed here were obtained in coordinated shipboard sampling from the RVs Sally Ride, Oceanus, and Sproul from 0000 to 0600 UTC 15 September 2017. Our analysis includes data from the flow-through temperature sensors (~5 m below the surface) on each ship and a 20-m-long towed bow chain deployed on the Ride. The bow chain was designed to measure undisturbed near-surface horizontal and vertical temperature gradients, and included a combination of 16 RBR, Ltd, Solo instruments (temperature, sampling at 2 Hz) mounted every 1 m along the bow chain line, interspersed with 3 RBR Concerto instruments (temperature, pressure, and conductivity, sampling at 12 Hz) at 5, 10, and 15 m along the line. From the three pressure sensors, the shape of the bow chain catenary is calculated at each time step and is used to interpolate temperature onto constant pressure surfaces.

We also analyze in situ, profiling data from the RV Ride, which were collected via profiles from the stern of the ship that alternated between a microstructure profiler (Rockland Scientific International, Inc., VMP-250, with shear probes, Thermometrics FP07 thermistors, and a CTD), and an RBR Concerto CTD. Because of ship-wake contamination, the upper 10 m of the VMP profiles were discarded. The
turbulent dissipation rate was calculated following Lueck (2013). Turbulent heat fluxes were calculated from simultaneous turbulence and temperature profile data following standard techniques (e.g., Adams et al. 2019).

Ocean velocity during the R/V Ride surveys was measured with a hull-mounted 300-kHz ADCP and side-pole mounted 5-beam 500-kHz ADCP (with 3-m vertical bins, sampling at 1 Hz). These two ADCPs allowed for sampling of water column velocity from ~3–5 m nearly to the bottom; sidelobe reflections contaminate the bottom 15% of the water column. Acoustic backscatter was measured with a Biosonics, Inc., echosounder (with 120- and 200-kHz transducers) mounted in the hull on the R/V Ride.

A subset of the ISDE mooring array is used in this analysis, including the OC50, OC40(N.S), OC32(N.S), and OC25(SA, SB, M, NB, NA) moorings that span a depth range of 25–50 m (cyan dots in Fig. 1d; numbers in the mooring names indicate water depth). These include velocity data from a bottom-mounted ADCP [with transducer frequency of 500 kHz for OC50 and OC40(S,N) and 1000 kHz for OC25(SA, SB, M, NB, NA)], water-column temperature data every 1–3 m, and some salinity data. The 32 m moorings are the only moorings without ADCP data. Further details about these moorings can be found in McSweeney et al. (2020a) and McSweeney et al. (2020b).

A land-based radar, deployed onshore of the mooring array, complemented the in situ observations. The radar collected observations of propagating internal waves and surface fronts over a footprint of 10-km radius with a resolution of 3 m in range and 1° in azimuth. The raw image sampling rate was approximately 0.7 Hz. Two-minute “wave averaging” of the raw radar images removes the surface gravity wave signals and enhances the imaging of slower features with longer time scales. The internal waves and fronts are imaged as bright and dark bands due to changes in surface roughness in regions of surface current convergence and divergence, respectively; an example image is shown in Fig. 1d, which is one frame of the wave-averaged radar movie (which also includes shipboard data) that is provided in the online supplemental material. Further information on the radar system and deployment can be found in Haller et al. (2019).

Airborne remote sensing measurements were collected using the Modular Aerial Sensing System (MASS; Melville et al. 2016) to characterize the properties of surface and internal wave processes in the ISDE sampling region. The instrument package includes infrared, visible, and hyperspectral cameras and a high-resolution long-range scanning lidar (Lenain et al. 2019).

3. Results

A sharp temperature front was observed off the California coast through multiple ship crossings and remote sensing. Figure 1 shows a sea surface temperature front (warm
Fig. 2. (a) Radar space–time diagram extracted along the northern (offshore) R/V Sally Ride transit (shown in Fig. 1). The R/V Ride front crossings are indicated as open cyan circles. The analyzed front is marked with white asterisks; note that there is a similar front approximately 6 h earlier. (b) As in (a), but extracted along the southern (offshore) transit. R/V Ride front crossings are indicated as open purple circles. The analyzed front is marked with white crosses; the earlier, similar front is also visible. In (a) and (b), the R/V Ride's signature in the radar is visible as linear white streaks. Transects are labeled A–E corresponding to the transects in Fig. 5, below. (c) Estimates of the front's cross-shore speed from the radar front tracking in (a) and (b), shown as gray and black lines, respectively. Theoretical estimates of gravity current speed computed from the R/V Ride frontal data are shown as dashed lines.

Figure 2 and 3 show space–time diagrams of radar intensity extracted along the cross-shore transects indicated by white lines in Fig. 1d, and in the video in the online supplemental material, which align with the northern offshore (Figs. 2a, 3a) and southern offshore (Figs. 2b, 3b) transits of the R/V Ride. Figure 3 is a zoomed-in and annotated version of the data in Fig. 2 to highlight the stages of the front’s evolution. The signature of the R/V Ride picked up by the radar is visible as white streaks with ship transits labeled A–E in Fig. 2; gaps in the streaks indicate times in which the ship veers off the transect line, potentially due to surface velocity gradients.

The dominant feature is the cross-shore propagation of nonlinear internal waves, visible as yellow-orange, nearly linear, negatively sloping streaks that indicate their shoreward propagation. It is especially evident in Fig. 2 that the internal waves tend to arrive in packets, with the leading internal tidal bore arriving first followed by a quiet (dark) period and then a high-frequency packet of internal waves. These propagating waves all have a similar cross-shore speed, consistent with nonlinear internal wave propagation (McSweeney et al. 2020a).

The event of interest here is a slower feature that peels off of the middle group of waves, which we are referring to as a detached front. This feature is crossed multiple times by the R/V Ride ship track, with the intersections denoted by cyan circles (offshore crossings) and purple circles (onshore crossings) in Fig. 2. The front begins to detach after the ship crossings labeled “A” and “B” in Figs. 2a and 2b, and is fully detached by crossings “C” and “D.” Detailed labels of this life cycle are given in Fig. 3. As apparent by its shallower slope in the space–time diagram, this detached front feature propagates appreciably more slowly than the internal wave speed exhibited by the vast majority of wave packet members, and instead propagates at close to the speed expected offshore and cool onshore; labeled “front” in Fig. 1d) along with multiple ship tracks. This front is aligned roughly alongshore (north/south) and is propagating shoreward. Note that the temperature contrails represent 1.75 h of data whereas the radar image is a snapshot. Hence, the temperature transitions observed earlier in the ship tracks may no longer line up with the features observed in the radar. The front in the radar image is visible over a distance of ~8 km in the alongshore direction. This snapshot is one frame of the movie that is included in the online supplemental material.

Aerial infrared imagery (Fig. 1a) gives another view of the same front but at an earlier time. The sharpest temperature gradient is centered near 120.722°W in the infrared data. Sea surface temperature (SST) collected from the MASS (Fig. 1a) highlights the sharpness of the front and the presence of high-frequency trailing waves behind the main front. Surface gravity wave steepness $S = \left[\left(\frac{\partial h}{\partial x}\right)^2 + \left(\frac{\partial h}{\partial y}\right)^2\right]^{1/2}$ computed from the MASS-derived surface topography $\eta(x, y)$ shows the energetic surface wave–current interaction that occurs as the front propagates onshore (Fig. 1b). We find an unmodulated surface wave field on the cold, shoreward side of the front, and modulation of the wave steepness by the front on the offshore side. The surface waves and front propagating in the same direction lead to surface smoothing (lower steepness), whereas localized roughening is associated with the presence of trailing waves where current and surface gravity are opposed (locally) and cause the rapid steepening of surface waves [see Lenain and Pizzo (2021) for details].

### a. Cross-shore propagation

To understand the nature of this feature, we first look at the evolution in time and space from the land-based radar observations. A convenient method for observing the propagation of sharp near-surface features is a space–time (Hovmöller) diagram.
for gravity currents (section 3c). The detached front also has a jagged shape, more notable in Fig. 3, which is likely related to southward-propagating alongfront instabilities (section 4c). Figure 2 also shows that a similar feature appears during the previous nonlinear wave packet arrival approximately 6 h earlier (~0200 UTC); it is not analyzed here.

b. Anatomy of a front

The subsurface structure of this sharp, surface intensified front and trailing turbulent filaments is shown in Fig. 4. This ship crossing (A in Fig. 2) was made shortly before the front detaches from the internal bore in the radar image. The data have been placed into a cross shelf coordinate system (rotated 11° south of due east), centered at the peak horizontal temperature gradient. On the offshore side (left; negative cross-front distance values), the warm water exhibits a series of filamentous structures, while on the onshore (right) side, the near-surface water is of a more uniform temperature. Lateral temperature gradients (Fig. 4b) reveal this structure in more detail. At the front there is a sharp horizontal temperature gradient (~0.1°C m⁻¹) throughout the 15-m depth range pictured. The temperature gradient of this front observed by the R/V Sproul bow chain (not shown) is of similar magnitude. The trailing filaments show up as bright features in the temperature gradient. Turbulence in the front and trailing filaments are visible through acoustic backscatter (Fig. 4c); here sound is likely directly scattering off the turbulent billows (e.g., Moum et al. 2003b). Average microstructure profiles of turbulent dissipation (Fig. 4d) ahead of (green) and within/trailing the front (blue) reveal a 10-fold increase in turbulence from 10- to 30-m depth.

Expanding our view to the entire water column (Fig. 5, leftmost column), the full-depth transects of temperature, velocity and turbulent dissipation rate from this first ship crossing demonstrate that the feature shown in Fig. 4 has elements of both a sharp front and an onshore propagating internal bore. The sharp surface front is coincident with a depression bore of the type discussed in detail by McSweeney et al. (2020a,b). In the depression, the thermocline (yellow to blue transition color in the temperature panel) descends from 12 to 29 m deep from about 200 to ~200 m (and 400 m in the offshore direction).

Cross-shore velocity shows surface convergence near the surface at the bore front, and divergences at depth, as is typical of bores in this region (McSweeney et al. 2020a). The alongshore flow has a sharp cross-shore gradient, yielding a very large vertical vorticity ~du/dz of ~O(100) f. The vertical vorticity is aligned with the surface front but extends through nearly the entire water column. An analysis (not shown) of the alongshore currents ahead of all the bores identified in McSweeney et al. (2020a) revealed no consistent patterns in the cross-shore gradient of the alongshore currents, and we note that the strong cross-shore gradient in these observations is neither “unique” nor “typical.”

c. Evolution of the detaching front

The subsurface evolution of the front and the bore ahead of it can be seen in both a series of ship crossings and in multiple time series from several nearby moorings. Over the five ship-crossings shown in Fig. 5, the near-surface temperature anomaly both weakened and shoaled in depth range. The first crossing (A) has the deepest and strongest temperature anomaly and clearest
cross-front convergence and took place when the front was still coincident with the onshore propagating bore in the radar image (Fig. 2). A strong cross-shore gradient in alongshore velocity (third row) is coincident with both the temperature front and gradients in cross-shore velocity. Turbulent kinetic energy dissipation rate and turbulent heat flux (bottom two panels) is enhanced at the front and behind it, visually roughly aligned with the vertical shear in cross-shore velocity. For the second crossing (B), the front is just starting to detach from the faster propagating bore as apparent in the radar image. In the subsurface view (Fig. 5, second column), both the deepening of the thermocline and the cross-front convergence of cross-front velocity have advanced several hundred meters ahead of the sharpest near-surface temperature front (the x axis is still centered at the surface temperature front). The cross-shore gradients in alongshore velocity stay most closely aligned with the front. Turbulence is still elevated at and trailing the front, in the region of high vertical shear.

By the third and fourth crossings (C and D), the radar image suggests the leading edge of the internal tide bore is approximately 1 km ahead of the front, out of the field of view of the ship survey. The front that is still visible by the ship (Fig. 5, third and fourth columns) is weaker and shallower. Cross-shore gradients in alongshore velocity (positive vertical vorticity) remains coincident with the front. In crossing C the turbulence takes on a strikingly different character, and is elevated at and beneath the front, throughout the entire water column; we briefly speculate about the source of this turbulence at the end of section 4c. In the fourth crossing (D), a series of high-frequency waves can be seen catching up with the front, visible in isotherm displacement (black contour), alongshore and cross-shore velocity. The arrival of this internal wave packet can be seen in the radar image for crossing D. By the final crossing (E), the near-surface temperature front is no longer visible. Cross-shore velocities are weaker, and there are no strong cross-shore gradients in alongshore velocity. Elevated turbulence appears coincident with the arriving high-frequency wave packet.

Mooring records showcase a different perspective of the detaching front, and also provides a sense of spatial variability of its position relative to the bore (Fig. 6). Offshore, the outcropping isotherm that defines the front and plunging thermocline at the leading edge of the bore arrive at OC50 simultaneously. As they move onshore past OC40S and OC32S, the near-surface front increasingly lags behind the bore. While the bore is evident in all but the OC25NA mooring, the front is most apparent along the southern mooring line and completely disappears inshore of the 32-m isobath. Note that as the bore moves onshore, the deepened thermocline becomes rarefied and appears flattened. The mooring array also gives a broader view of the full bore structure, including high-frequency internal waves that chase (and eventually catch as seen in the radar data) the front. The same high-frequency internal waves appear as bright bands in the radar data (Fig. 2) and are visible in transect D of the R/V Ride crossings (Fig. 5).

The cross-shore velocity data from the moorings echo what is seen from the ship, that is, strong surface convergence and deep divergence offshore that weakens as the bore moves onshore (Fig. 7). While offshore the surface convergence aligns with the surface front, at OC40S the convergence zone has moved somewhat ahead of the surface front. The cross-shore
gradient in alongshore velocity (vertical vorticity), however, appears to be more tightly bound to the surface front than to the bore. This is also evident in the shipboard data (Fig. 5). As with the temperature features of the front, the convergence and vorticity that are evident offshore have vanished by the 25-m isobath.

The radar data allow the slowing speed of the detaching front seen in both ship-based and mooring observations to be quantified. The slopes of features in the space–time diagrams (Fig. 2) indicate their cross-shore propagation speed (note both total water depth and cross-front distance are marked on the ordinate axes). For the front of interest, the trajectories are manually identified and the estimated speeds along the northern and southern transits are shown as gray and black lines in Fig. 2c. It appears that the front is birthed from an internal bore traveling at \( \sim 0.18 \text{ m s}^{-1} \) and then falls behind the bore, sharply decreasing in speed to \( \sim 0.05 \text{ m s}^{-1} \) over a shoreward propagation distance of about 1.5 km.

The first clue that this front is propagating as a gravity current comes from analysis of its speed. The associated expected gravity current speed, \( C_{GC} \approx (g' H_{Total})^{1/2} \), is estimated at the locations of the R/V Ride front crossings indicated by open cyan and purple circles. To compute \( g' \), we use the lateral density difference across the front using the temperature and salinity measured at roughly 2-m depth on the R/V Ride bow chain. These theoretical speeds are indicated by cyan and purple circles in Fig. 2c and are connected with a dashed line. The front is initially faster than gravity current theory would suggest but slows down to a speed that is comparable to theory by the time it becomes barely visible in the radar image. Note that this slowing to the gravity current speed is an interesting contrast to the front turned gravity current observed by Warner et al. (2018), which speeds up as it transitions from balanced to unbalanced, propagating dynamics.

4. Discussion

The observations described above illustrate the life cycle of a sharp, surface-intensified front birthed from an internal tidal...
bore. The front is initially coincident with the bore, but is then left behind, propagating onshore as a gravity current, more slowly than both the bore and the high-frequency internal waves (e.g., Fig. 2). It has an evolving structure, visible both subsurface (Figs. 5–7) and from above (Figs. 1–3), schematically portrayed in Fig. 8. After separation from the bore, the front is visible for about 4 h and 2 km of propagation distance and then disappears from view. Here we discuss these
observations in light of potential mechanisms for front generation, evolution, and destruction.

a. Generation and evolution of the front

The generation and evolution of shoaling internal tidal bores are active research topics (Lamb 1994; Holloway et al. 1997; Scotti et al. 2007), and, to our knowledge, the data presented here represent the first observational evidence of a shoaling internal bore generating a gravity current front. The instrumentation was concentrated on the inner shelf, so the formation of the internal tidal bore farther offshore was not captured; we only observe how the internal bore evolves across the inner shelf. One question that emerges is how this particular bore’s evolution gives rise to the formation of the front and why the front detaches and subsequently propagates so slowly relative to the bore’s speed. Given the range of shoaling bore dynamics that have previously been described from the 2-month mooring dataset (McSweeney et al. 2020a,b), we suggest that the stratification and current shear ahead of the bore (i.e., the upstream waveguide) are relevant to both the bore’s cross-shore evolution and to the evolution of the high-frequency waves that trail behind the bore. We observe that this bore encounters a pycnocline that is about middepth in the water column, consistent with observations of α, the quadratic nonlinearity coefficient in the Korteweg–de Vries equation, being near zero (McSweeney et al. 2020a).

It is likely that the bore also transits through the critical depth, where α changes sign from positive to negative (Helfrich et al. 1984; Vlasenko and Stashchuk 2007; Shroyer et al. 2009), which would entail the high-frequency internal waves switching polarity from depression to elevation waves. These waveguide conditions do not appear to necessitate the formation of a secondary front, but we do note that other gravity current fronts were observed during similar waveguide conditions throughout the record (such as that observed behind the earlier internal tide in Fig. 2 at 26-m depth at 0200 UTC).

The bore and gravity current are first observed at OC50, where they are still coincident (Figs. 6 and 7, left-most panel in each). Near the 40-m isobath, the two features have begun to separate. By this we mean that the thermocline depression (bore) is beginning to leave the near vertical outcropping isopycnals (gravity current front) behind. With this sort of separation, the ensuing flattened wave that connects the two separated features is often referred to as a rarefaction (e.g., Melville and Helfrich 1987). McSweeney et al. (2020a) demonstrate that these rarefactions occur in this region when the pycnocline depth exceeds one-half of the total water depth, a condition not often observed this far offshore.

The phenomenology and dynamical properties of nonlinear internal waves and gravity currents have been linked through a series of previous analyses (e.g., Benjamin 1968; Rottman and Simpson 1989; Lamb and Wilkie 2004; Nash and Moum 2005; White and Helfrich 2008; Kilcher and Nash 2010; White and Helfrich 2012). Most previous work involves causality in the opposite direction from what was observed here, i.e., internal waves spawned from a gravity current propagating into stratified fluid. For the present analysis, the crucial insight is to recognize the equivalence between (i) a buoyancy-driven gravity current with large enough amplitude to water depth ratio to approach the critical Froude number and (ii) a particular limiting case sometimes experienced by shoaling internal bores. In this limiting bore case, the increasing amplitude does not lead to wave breaking but instead a horizontally elongated “flat-bottomed” bore, in which the growing horizontal extent conserves energy and the
upstream undisturbed stratification is linked to the adjusted downstream isopycnal locations through a dissipation-less jump (White and Helfrich 2008). This latter situation is often dubbed the conjugate state, in light of the conjoined but complementary upstream and downstream thermocline conditions (Benjamin 1966). In idealized conditions, this conjugate state bore/gravity current occupies half the water depth, and is the fastest internal wave allowed.

Observations from the farthest-offshore moorings are consistent with this state, with a bore-like depression making up half the water column (Figs. 6 and 7, left-most panels in each). At this point it is reasonable to interpret the situation as a conjugate style bore, or a gravity current; the equivalency described above argues that either or both are appropriate, both solutions can be considered superimposed at this time. Here we argue that as this feature continues to shoal into shallower water, that equivalency allows it to separate into a propagating rarefied internal wave and a slower moving surface-intensified gravity current.

The nature of that subsequent separation is well described by the theory and simulations of White and Helfrich (2012). They approach the situation from a different starting point, that of a gravity current propagating into a stratified fluid. An observational example of getting to the equivalence point is shown in Solodoch et al. (2020). For two-dimensional gravity currents, Benjamin (1965) used the Bernoulli equation to show that the depth of the gravity current $H_{GC}$ will not exceed one-half of the total depth $H_{Total}$, if it is energy conserving. Furthermore, he showed that for $0.2 < H_{GC}/H_{Total} < 0.5$ the speed of the gravity current front is relatively constant, $C_{GC} = (g' H_{Total})^{1/2}/2$.

Figure 9 is a modified version of Fig. 4 from White and Helfrich (2012), showing five regimes that they delineate for gravity current evolution, as a function of gravity current height normalized by the distance from ocean surface to the thermocline ($x$ axis) and gravity current speed relative to the mode-1 linear wave speed ($y$ axis). The conceptually simplest cases that they consider are either purely subcritical (type I) or purely supercritical (types IV and V), the latter happening for $c_{GC}/c_{0} > 1$ where $c_{GC}$ is the gravity current speed and $c_{0}$ is the linear mode-1 internal wave speed in the undisturbed upstream stratification. The more interesting situations are transcritical regimes II and III, in which different types of upstream propagating features are allowed, generated by quasi-resonant interaction between gravity current speed and linear wave speeds, using both the pure undisturbed upstream stratification and that influenced by the gravity current isopycnal deflections. In regime II, undular bores or solitary waves propagate ahead of a gravity current. Regime II conditions are encountered several days earlier in our observations, with commensurate observations of leading solitons (Figs. 9a,b,d,e).

The boundary between transcritical regimes II and III occurs at the conjugate state described above. Past this point,
instead of a train of waves, theory predicts a monotonic upstream bore connected to the gravity current front by an expanding rarefaction. Though the situation depicted in our observations starts with a tidal bore and not a gravity current, we posit that at the 50-m isobath the system is on that dividing line between regimes II and III and can be thought of equivalently as either a conjugate state bore or a gravity current. As the feature continues to shoal, it takes a larger percentage of the water column, pushing the state to the right in the phase diagram (Fig. 9c; into regime III). In this regime a single rarefied wave propagates ahead, leaving a gravity current with associated leading front behind. The evolution of this process is evident in Fig. 6, particularly along the southern mooring line. As the bore shoals between the 50- and 40-m isobaths, the thermocline depression deepens and now occupies more than half of the water depth at OC40S. At this point the gravity current and bore become decoupled. Farther onshore, mooring (Fig. 6; OC32S) and shipboard observations (Fig. 5; transect C) show a thermocline depression moving ahead of a sharp surface front. The front continues to propagate onshore but more slowly; front propagation speeds observed in the radar near the 32-m isobath (Fig. 2c) match those predicted for a gravity current by Benjamin (1968).

b. Relationship to the broader category of frontogenesis

This example of front formation through evolution of, and subsequently detachment from, a nonlinear tidal bore is to our knowledge a new (observational) contribution to the increasingly diverse array of frontogenetic processes in the ocean (Mahadevan and Tandon 2006; McWilliams 2021). The classic view of frontogenesis in the ocean (Hoskins and Bretherton 1972) is instigated by a sharpening of preexisting lateral density gradients through confluence of mesoscale currents. As a front sharpens through confluence, frontal sharpening is accelerated through a secondary circulation, which enhances the local convergence rate to create a runaway affect.

More recent work by Barkan et al. (2019) highlights that an analogous run-away frontogenesis process can be produced from a wide variety of initial forcing conditions. Once it gets going, there is often an interplay between growing convergence at the front, vertical velocity, growing vorticity, and sharpening buoyancy gradients. Crucially, they argue that once the lateral convergence rate becomes strong (relative to the inertial frequency), the processes play out in a similar manner regardless of the initial instigation; the system has “forgotten” how it got started on the route to frontogenesis (e.g., Wang et al. 2021). Though the instigating convergence here comes from an internal tide instead of a mesoscale process, the evolution of this front bears some similarity to the situation described in Barkan et al. (2019). Both the observed frontal convergence rate and positive (cyclonic) vorticity at the front (onshore gradient of alongshore velocity) are of order ~30–50°f at this lateral resolution. We suspect that similar run-away frontogenesis effects may act to sharpen the front observed here. Finally, for steep enough fronts initially created through any mechanism, the dominant momentum balance may shift from a roughly balanced one (through inviscid or turbulent thermal wind) to that of a propagating gravity current (Warner et al. 2018; Pham and Sarkar 2018).

c. Destruction

The sections above discuss potential processes creating the formation and sharpening of the front shown here, which propagates shoreward as a gravity current. The observations also show the front to diminish in both strength and vertical extent over roughly 4 h, eventually disappearing from view in the remote and subsurface data. Here we discuss several processes that may contribute to the front’s destruction. While each of these mechanisms likely plays a role in the frontal evolution, southward advection of the entire feature (visible in the movie in the online supplemental material) may dominate the disappearance of this feature from the shipboard and moored data at this latitude.

The first possibility is that some of the heat may be turbulently mixed downward. Microstructure profiles show that turbulence is elevated on average on the warm side relative to the cool side of the front (Fig. 4, right). Comparison of turbulence from multiple ship passes (Fig. 5, fourth row) reveals a complex structure that is often intensified right at the front (crossings 1 and 2) but sometimes has more of a full depth structure (crossing 3). Zooming in on the first crossing in detail, the rich structure in both lateral temperature gradients (Fig. 4b) and acoustic backscatter (Fig. 4c) are consistent with a series of turbulent billows trailing the front. The billows are visually suggestive of a shear instability process (Smyth and Moum 2012; Geyer et al. 2010). The mooring records confirm that a Richardson number criterion for shear instability is frequently met during and following front passage (Fig. 7), especially along the interface of the front.

Downward turbulent heat fluxes are shown in the bottom row of Fig. 5. Downward turbulent heat fluxes at the leading edge of the front and beneath the warmest water are of order ~100–300 W m$^{-2}$. Upward heat loss to the atmosphere during this time was ~90 W m$^{-2}$, as calculated from shipboard meteorological sensors using standard bulk formula (Fairall et al. 2003). These heat fluxes can be compared with the observed loss of heat on the warm side of the front throughout the night. Figure 10 shows the decrease in the temperature jump moving from the cooler (onshore) to the warmer (offshore) side of the front, from three different ships. If this pattern were to be caused by downward turbulent heat fluxes from the warm side of the front only, the observed level of cooling would require approximately ~4000 W m$^{-2}$ of heat loss, assuming a 15-m warm-layer depth (Fig. 10, right). Although the observed turbulent heat fluxes are substantial, they are not sufficient to fully explain the observed rapid loss in heat.

In addition to turbulent mixing, there is also an indication in the radar image sequences that the front develops lateral shear instabilities as it propagates toward shore. For example, Fig. 11 shows three radar snapshots (Figs. 11a–c) over the span of 3.5 h, each synchronous with a R/V Ride front crossing. In Fig. 11a, the front is observed in ~36-m water depth, with some weakly visible alongfront structure. In Fig. 11b, the
The front is observed 35 min later but the water depth is only slightly less, ~35 m, with more noticeable alongshore wave-like structure. As the front continues to propagate to shore, this alongshore structure appears to lengthen as seen in Fig. 11c at the time of R/V Ride front crossing D in ~26-m water depth.

Lateral shear instabilities on gravity currents are not well understood. White and Helfrich (2013) numerically simulated shear instabilities due to across-front shear in the alongfront velocities of an idealized gravity current system. They associate the existence of these instabilities with O(1) values of a nondimensional parameter $\gamma$ that is the ratio of the representative time scales for growth of horizontal shear instability $\tau_y$ versus that of gravitational adjustment $\tau_{gc}$. This ratio is defined as

$$\gamma = \frac{\tau_y}{\tau_{gc}} = \frac{10l_y}{9(\gamma' H_{Total})^{1/2}} = \frac{10H_{Total}}{3\Delta V H_{Total}} C_{GC}, \quad (1)$$

where $H_{Total}$ represents the total water depth, $l_y$ is the half-width of the horizontal shear layer, and $\Delta V$ is the difference in alongfront velocity across the front. The propagation speed of the gravity current $C_{GC}$ is taken here as $(\gamma' H_{Total})^{1/2}$. Values of $\gamma \leq O(1)$ support the existence of shear instabilities, while larger values would suggest that gravitational adjustment occurs at much faster time scales.

Each of the terms in $\gamma$ can be roughly estimated at the different cross-shore locations and depths corresponding to the R/V Ride crossings of the front and are listed in Table 1. The across-front change in velocity $\Delta V$ is taken as the difference in velocities averaged from 100 to 400 m on either side of the front. These velocities were measured from the R/V Ride near-surface side-mounted ADCP at 5.7-m depth. A 20-s moving average is applied to the 1-Hz measurements to filter out surface wave orbital velocities. This 20-s filtering corresponds to 20-m filtering in space (1 m s$^{-1}$ ship velocity), which limits the possibility of estimating the shear layer half-width $l_y$ from the velocity data. In essence, because of the necessary averaging, an $l_y$ of less than 20 m cannot be resolved by the side-mounted ADCP. Thus, $l_y$ is instead estimated using the sharp change in $\gamma'$ (equivalently temperature). For this, $l_y$ is the distance at which $\gamma'$ reaches 50% of the average $\gamma'$ values between 20 and 60 m on either side of the front. This method yields $l_y$ values of 2–10 m, consistent with that observed in Fig. 4.

The final parameter needed to compute $\gamma$ is the gravity current speed $C_{GC}$, which we take directly from the radar space–time plots at the locations of R/V Ride frontal crossings shown in Fig. 2 and discussed in section 3b. Estimated values of $\gamma$ reported in Table 1 are clearly $O(1)$. This indicates the potential for horizontal shear instability in this gravity current. It is also evident that $\gamma$ decreases as the crossings get closer to shore, which only further supports the potential for shear instability as the front propagates onshore.

Linear shear instability theory (Michalke 1964) would suggest that the most unstable wavenumber is $k \approx 0.45/l_y$. According to this, the $l_y$ values estimated from $\gamma'$ would yield...
wavelengths of 30–140 m. However, manual measurements of
the instability wavelengths in the radar imagery (Fig. 11)
indicate observed wavelengths of 550–700 m, larger than
the linear theory would suggest. Note that, at the offshore
distance of the instabilities, the azimuthal resolution of the
radar is approximately 70 m, thus limiting the lower bound of
observable wavelengths. Additionally, values of $l_y$ determine
via momentum may not be equal to that via temperature, as we
have assumed here. It is possible that nonlinearity contributes
to the longer wavelength of the observed instabilities as com-
pared with linear theory. Baroclinic instability can be ruled out
as the cause by using the scales for buoyancy frequency, water
depth, and Coriolis parameter at the study site in an Eady-type
model (Chen et al. 2020). From these, we calculate a length
scale for the fastest growing baroclinic instability as $O(10 \text{ km})$,
which is an order-of-magnitude longer than the observed
instabilities.

This sort of lateral shear instability may conspire with ver-
tical instabilities to enhance turbulent mixing in ways not fully
captured by these measurements, nor well understood. It is,
however, intriguing to note that near the time lateral instabil-
ities are observed developing in the radar, turbulence in tran-
sect C is elevated throughout the entire water column (Fig. 5).
The lateral shear instability is drawing energy from alongshore
currents, which also extend throughout nearly the entire
water column.

Some part of the observed evolution between ship transects
observed in Fig. 5 may reflect southward advection of a warm
filament with finite alongshore extent. In an animated version
of the radar images (included in the online supplemental ma-
terial) the warmest water appears to be propagating south-
ward, out of the field of view of these measurements. This
alongshore temperature gradient and southward advection
likely explains the order of magnitude difference.

5. Conclusions

Here we have described the life cycle of a submesoscale
front that decouples from a shoaling internal bore, through
the lenses of shipboard, in situ, and remote measurements.

Table 1. Estimated $\gamma$ values and parameters used for calculation. Each of the four $\gamma$ values corresponds in space and time to a front
crossing (A–D) by the R/V Sally Ride.

<table>
<thead>
<tr>
<th>R/V Sally Ride transit</th>
<th>$H_{Total}$</th>
<th>$\Delta V$</th>
<th>$l_c$</th>
<th>$C_{GC}$</th>
<th>$\gamma$</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>36.6 m</td>
<td>0.23 m s$^{-1}$</td>
<td>10.2 m</td>
<td>0.171 m s$^{-1}$</td>
<td>2.1</td>
</tr>
<tr>
<td>B</td>
<td>35.1 m</td>
<td>0.13 m s$^{-1}$</td>
<td>3 m</td>
<td>0.166 m s$^{-1}$</td>
<td>1.1</td>
</tr>
<tr>
<td>C</td>
<td>30.3 m</td>
<td>0.23 m s$^{-1}$</td>
<td>5 m</td>
<td>0.088 m s$^{-1}$</td>
<td>0.6</td>
</tr>
<tr>
<td>D</td>
<td>26.5 m</td>
<td>0.26 m s$^{-1}$</td>
<td>2.6 m</td>
<td>0.072 m s$^{-1}$</td>
<td>0.3</td>
</tr>
</tbody>
</table>
As the bore propagates onshore, it steepens and grows to occupy more than half the water column. Its amplitude and speed put it in a near-critical state, in comparison with the internal wave phase speed appropriate for the upstream water into which it is propagating. In this state it can be described as either a particular solution to the nonlinear internal wave equation, known as a conjugate state wave, or equivalently as a critical gravity current; those two phenomena are in some sense thus superimposed (White and Helfrich 2012). As the feature moves further onshore, continued shoaling breaks the symmetry, and the feature decomposes into a faster-moving rarefied wave and a trailing gravity current front. The type of rarefaction behavior of the internal bore seen here is neither common nor rare, but rather one of at least a handful of personalities these shoaling bores may assume depending on their amplitude and the stratification ahead of them. In fact, the bore immediately preceding the one discussed here displayed the same rarefaction behavior. Given the generality of the conditions, this type of relationship between internal bores and gravity current fronts may be not uncommon in other places where internal waves shoal.

After calving from the bore, the gravity current and associated sharp front are encompassed by turbulence that grows from both the lateral and vertical shear. At the frontal interface and in the wake of the front, the Richardson number dips below 0.25, implying the potential for vertical shear instability. The measured dissipation rate at and below the front exceeds that of the surroundings by orders of magnitude, with downward turbulent heat fluxes of 200–300 W m$^{-2}$. The cross-shore shear of the alongshore velocity at the front is also very high ($\text{Ro} \sim 40$), suggesting that lateral shear instability plays a role in modulating the gravity current front. To test this we compared the lateral shear instability time scale with the gravity current propagation time scale as defined by White and Helfrich (2013). As the gravity current slows to its theoretical speed $[\text{CGC} = (g' H_{\text{total}})^{1/2}/2]$, lateral shear instabilities likely contribute to its destruction. Southward advection of the entire feature outside of our observational region prevents closure of an energy or heat budget.

While there remain many unanswered issues, we choose to highlight three that we find to be particularly intriguing. First, sharp cross-shore gradients in strong alongshore flow create a large vertical vorticity. The southward flow is initially coincident with the steepening tidal bore. It may reflect a combination of wave origin and initial cross-shore orientation, the influence of rotation, or preexisting wind-driven alongshore currents. An analysis of the full range of bores described in McSweeney et al. (2020a,b) (not shown here) reveals no consistent patterns for the direction or strength of alongshore currents associated with onshore-propagating bores. Interestingly, when the front separates and lags behind the bore propagating onshore, the sharpest vertical vorticity stays locked with the front, perhaps reflecting the types of frontogenesis processes described by Barkan et al. (2019). Second, with a wide range of scales linking the linear internal tide, nonlinear bores and solitons that develop at its leading edge, and this type of sharp near-surface front spawned by a steepening bore, the distribution of energy between these features is unclear. Energy and momentum appear to be exchanged between these features in inhomogeneous and anisotropic ways; thus, fully understanding coastal energy or momentum budgets requires knowledge of both processes and how they operate together. Third, while we show evidence of both vertical and lateral shear instabilities developing at this front, there is a suggestive hint of interplay between them that cannot be fully assessed with these data. Future observational analysis or targeted numerical simulations may help disentangle some of these complexities.

The coexistence and intermingling of these two distinct features remind us that as students of turbulent flows we cannot restrict ourselves to the study of a single scale or type of ocean dynamics. This may be only one of many cases of intersections and interactions between nominally distinct phenomena that are yet to be appreciated.

6. Dedication

We dedicate this paper to our friend and colleague Sean Haney, who led this interdisciplinary collaboration (Fig. 12). Sean passed away in January of 2021, following several years of serious illness. Sean was a physical oceanographer at the Scripps Institution of Oceanography, where he was highly regarded both for his scientific insight and adventurous spirit. He completed his Ph.D. at University of Colorado Boulder in 2015 and made substantial contributions to our understanding of upper-ocean processes. He was extremely thoughtful and inquisitive, remembered by his colleagues as the person with whom to talk through challenging problems. Sean was a rare breed of oceanographer who was easily able to integrate complicated physical observations into equally complex theoretical frameworks. He was also a beloved shipmate, who brought a keen sensibility and a joyful, playful spirit to field work. Outside of work, Sean embraced every opportunity to explore and was often found surfing, mountain biking, climbing, skydiving, or camping. He was an avid participant in game nights, incredibly witty, and frequently the MVP of the trivia team. His kindness, brilliance, and spunk will forever be remembered. We miss you, Sean.

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Data availability statement. The complete dataset from the Inner Shelf Dynamics Experiment, including the raw mooring, shipboard, and radar data required to reproduce the
results in this paper, is archived online (https://doi.org/10.6075/J0WD3Z3Q).

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