A Global Statistical–Dynamical Tropical Cyclone Wind Radii Forecast Scheme

JOHN A. KNAAF
NOAA/Center for Satellite Application and Research, Fort Collins, Colorado

CHARLES R. SAMPSON
Naval Research Laboratory, Monterey, California

GALINA CHIROKOVA
Cooperative Institute for Research in the Atmosphere, Fort Collins, Colorado

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ABSTRACT

Forecasts of tropical cyclone (TC) surface wind structure have recently begun to show some skill, but the number of reliable forecast tools, mostly regional hurricane and select global models, remains limited. To provide additional wind structure guidance, this work presents the development of a statistical–dynamical method to predict tropical cyclone wind structure in terms of wind radii, which are defined as the maximum extent of the 34-, 50-, and 64-kt (1 kt = 0.514 m s\(^{-1}\)) winds in geographical quadrants about the center of the storm. The basis for TC size variations is developed from an infrared satellite-based record of TC size, which is homogenously calculated from a global sample. The change in TC size is predicted using a statistical–dynamical approach where predictors are based on environmental diagnostics derived from global model forecasts and observed storm conditions. Once the TC size has been predicted, the forecast intensity and track are used along with a parametric wind model to estimate the resulting wind radii. To provide additional guidance for applications and users that require forecasts of central pressure, a wind–pressure relationship that is a function of TC motion, intensity, wind radii (i.e., size), and latitude is then applied to these forecasts. This forecast method compares well with similar wind structure forecasts made by global forecast and regional hurricane models and when these forecasts are used as a member of a simple consensus; its inclusion improves the forecast performance of the consensus.

1. Introduction

The estimation and forecast of surface winds associated with tropical cyclones (TCs) is important to a variety of stakeholders and applications. Important stakeholders include state and local governments, private industry, and the U.S. military. Key applications include wind-based risks and impacts, and wave and surge forecasting. The National Hurricane Center (NHC), the Central Pacific Hurricane Center (CPHC), and the Joint Typhoon Warning Center (JTWC) provide information about TC risks and make 6-hourly forecasts of TC tracks, intensities, and wind structures for all active TCs. The initial and forecast TC surface wind structures are provided in terms of the maximum radial extent of 34-, 50- and 64-kt (1 kt = 0.514 m s\(^{-1}\)), or gale force (R34), damaging (R50) and hurricane (R64) force winds in geographic quadrants surrounding the TC. These are collectively referred to as wind radii. NHC also has been conducting postseason reanalysis or best tracking of their wind radii since 2004. The operational units for intensity are knots and for wind radii they are nautical miles (n mi, 1 n mi = 1.85 km), so these units will be used throughout this paper.

As of 2016, NHC and the JTWC forecast R64 through 36 h, and R50 and R34 wind radii through 72 h, while intensity and track are forecast through 120 h (Knaff and Sampson 2015). Recent work has shown that the current NHC forecasts are skillful to NHC’s maximum lead time of 72 h (Knaff and Sampson 2015; Cangialosi and Landsea 2016). However, because best-tracked wind radii have been considered to have large subjectively determined uncertainty (Landsea and Franklin 2013), NHC does not yet routinely verify their wind radii forecasts (Knaff and...
DeMaria et al. (2005; DeMaria 2009; DeMaria et al. 2007, 2015) and statistical–dynamical approaches (e.g., regional NWP (e.g., Bender et al. 2007; Bernardet et al. 2014). While NWP initially struggled to produce skillful wind radii forecasts (see Knaff et al. 2006), Sampson and Knaff (2015) recently showed that a consensus of NWP 34-kt wind radii forecasts provides skillful (vs DRCL) guidance through 120 h. However, individual NWP models are often biased and still struggle to show skill relative to climatology and persistence when predicting wind radii.

A similar historical analogy exists for tropical cyclone intensity forecasts. Many of the early advances in TC intensity forecast skill were due to a combination of regional NWP (e.g., Bender et al. 2007; Bernardet et al. 2015) and statistical–dynamical approaches (e.g., DeMaria et al. 2005; DeMaria 2009; DeMaria et al. 2007, 2014). The statistical–dynamical approach combines forecast information from a dynamical model within a statistical framework to make, typically more specific or smaller-scale, forecasts. A good example of this approach is the model output statistics that have long provided operational guidance on forecast wind radii (Carter et al. 1989). It has been shown that intensity forecasts made with the statistical–dynamical methods often produced the most skillful (vs climatology and persistence) individual intensity forecasts. However, it was a simple equally weighted consensus approach (Sampson et al. 2008) that ultimately proved most skillful for intensity forecasts (DeMaria et al. 2014).

At this time, there is a notable absence of models that use a statistical–dynamical approach to provide wind radii guidance in research and in operations. With this deficiency in mind, and a desire to have more relatively independent members available for consensus methods, this study will describe a statistical–dynamical approach to making wind radii forecasts in hopes that wind radii forecasts can be further improved by using the combination of NWP and statistical–dynamical approaches.

2. Data and methodology
   a. The dependent variable

To build a statistical model designed to predict TC structure changes, some thought was needed concerning the dependent variable $Y = f(x)$, where $x$’s are the independent variables or predictors. For wind radii the following considerations were important. The variable $Y$ must provide information about the primary vortex size, be available for all intensity ranges, be valid over landmasses, and be consistent in all ocean basins—citing that operational procedures (Knaff et al. 2003; Rappaport et al. 2009) and the quality of the wind radii have been shown to vary over time and by basin (K07). In addition, it also is desirable to estimate a single homogeneously developed $Y$, rather than build a model for several instances of $Y$ (e.g., one for each radii, each quadrant, MSLP, etc.) or $Y$’s that were estimated in different ways and/or have variable quality. It also quickly becomes rather cumbersome to maintain and occasionally update 3–12 regressions at 20 lead times, as was the case for the McAdie wind radii climatology and persistence model (MRCL) discussed in K07. Our choice of homogeneously calculated $Y$ for this work is the temporal change from the initial time of a normalized infrared (IR) satellite-based TC size estimate $R_5$, developed in Knaff et al. (2014b, hereafter K14). We will refer to this $Y$, whose development is described next, as $\Delta F_{R5}$.

The first step in creating $\Delta F_{R5}$ is to account for the variations of $R_5$ with TC intensity and create the normalized TC size variable $F_{R5}$. This is done by dividing $R_5$ by an intensity-based climatology $R_5^c$ (see Knaff et al. 2014a), where $VM$ is the intensity in knots, as shown in Fig. 1:

$$R_5^c = 7.653 + \frac{VM}{11.651} - \left(\frac{VM}{59.067}\right)^2,$$  \hspace{1cm} (1)

where $R_5^c$ has units of degrees latitude, increasing from about 9° latitude (999 km) at 20-kt intensities to 13° latitude (1443 km) at 90 kt. At intensities greater than 90 kt, $R_5^c$ eventually maximizes at 14° latitude (1554 km),

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1 We define $R_5$ as the radius at which the TC wind field is indistinguishable from the background flow in a climatological environment (K14) and has units of degrees latitude. $R_5$ is calculated from estimates of the tangential wind at 500-km radius ($V_{500}$) that are based on the principle components of the azimuthally averaged storm-centered IR brightness temperatures and the sine of the absolute value of latitude, which follows similar approaches used by Mueller et al. (2006) and Kossin et al. (2007). Full details can be found in Knaff et al. (2014b).
actually decreasing a tiny bit for the most intense storms. A similar pattern of behavior was noted for 34-kt wind radii observed in the western North Pacific (Wu et al. 2015), where the 34-kt wind radii leveled off at approximately 775 km. The normalization procedure is

\[ F_{R5} = \frac{R5}{R5_c} . \]  

To provide the reader a visual example of what a time series of R5 and \( F_{R5} \) would look like for a hurricane, Fig. 2 shows the R5 and \( F_{R5} \) time series for east Pacific Hurricane Amanda (2014). Amanda was a relatively short-lived major TC with a life cycle of just 7½ days. During that time, it reached a peak intensity of 135 kt, making it the strongest east Pacific hurricane to occur in the month of May (Stewart 2014). To accompany these time series, IR images of the storm are shown at 24-h intervals starting at 0000 UTC 23 May. These results show the changes in TC structure that accompany the variations of R5 and \( F_{R5} \). Having estimated \( F_{R5} \) for all the cases available, the last step is to create our dependent variable, \( \Delta F_{R5} \), as a function of forecast lead time.

To form \( \Delta F_{R5}(t) \), the initial value of \( F_{R5}(t = 0) \) is subtracted from the value of \( F_{R5} \) for each 6-hourly lead time from 6 to 120 h. The \( \Delta F_{R5}(t) \) values were then created for the following global tropical cyclone basins: the North Atlantic (NATL), the eastern and central North Pacific (EPAC), the western North Pacific and north Indian Ocean (WPAC), and the Southern Hemisphere (SHEM). The north Indian Ocean has too few cases to develop this capability, and we could have combined that basin with the WPAC, but that was not done in this study. The years 1996–2012 were used in the NATL and EPAC and years 2001–12 were used in the WPAC and SHEM. The availability of IR imagery in the WPAC and SHEM limited the starting year. The resulting numbers of cases available for model development are similar for all these basins, as shown in Table 1.

b. Fitting the statistical–dynamical model

Statistical–dynamical model development follows past work with intensity forecasting, where the change in intensity from the initial time is used as the dependent variable and independent variables or predictors are
TABLE 1. Number of cases available for multiple linear regression development in the NATL, EPAC, WPAC, and SHEM basins.

<table>
<thead>
<tr>
<th>Lead time (h)</th>
<th>NATL</th>
<th>EPAC</th>
<th>WPAC</th>
<th>SHEM</th>
</tr>
</thead>
<tbody>
<tr>
<td>6</td>
<td>5915</td>
<td>4613</td>
<td>5168</td>
<td>4554</td>
</tr>
<tr>
<td>12</td>
<td>5724</td>
<td>4453</td>
<td>4986</td>
<td>4390</td>
</tr>
<tr>
<td>18</td>
<td>5498</td>
<td>4265</td>
<td>4777</td>
<td>4204</td>
</tr>
<tr>
<td>24</td>
<td>5448</td>
<td>4055</td>
<td>4563</td>
<td>4010</td>
</tr>
<tr>
<td>30</td>
<td>4993</td>
<td>3824</td>
<td>4347</td>
<td>3815</td>
</tr>
<tr>
<td>36</td>
<td>4743</td>
<td>3594</td>
<td>4136</td>
<td>3618</td>
</tr>
<tr>
<td>42</td>
<td>4499</td>
<td>3367</td>
<td>3927</td>
<td>3424</td>
</tr>
<tr>
<td>48</td>
<td>4262</td>
<td>3145</td>
<td>3723</td>
<td>3237</td>
</tr>
<tr>
<td>54</td>
<td>4041</td>
<td>2933</td>
<td>3527</td>
<td>3052</td>
</tr>
<tr>
<td>60</td>
<td>3827</td>
<td>2726</td>
<td>3337</td>
<td>2873</td>
</tr>
<tr>
<td>66</td>
<td>3621</td>
<td>2524</td>
<td>3151</td>
<td>2699</td>
</tr>
<tr>
<td>72</td>
<td>3425</td>
<td>2329</td>
<td>2967</td>
<td>2531</td>
</tr>
<tr>
<td>78</td>
<td>3238</td>
<td>2145</td>
<td>2988</td>
<td>2369</td>
</tr>
<tr>
<td>84</td>
<td>3058</td>
<td>1972</td>
<td>2610</td>
<td>2217</td>
</tr>
<tr>
<td>90</td>
<td>2891</td>
<td>1808</td>
<td>2438</td>
<td>2068</td>
</tr>
<tr>
<td>96</td>
<td>2731</td>
<td>1656</td>
<td>2268</td>
<td>1922</td>
</tr>
<tr>
<td>102</td>
<td>2577</td>
<td>1514</td>
<td>2105</td>
<td>1787</td>
</tr>
<tr>
<td>108</td>
<td>2429</td>
<td>1377</td>
<td>1946</td>
<td>1659</td>
</tr>
<tr>
<td>114</td>
<td>2289</td>
<td>1245</td>
<td>1792</td>
<td>1539</td>
</tr>
<tr>
<td>120</td>
<td>2161</td>
<td>1121</td>
<td>1644</td>
<td>1424</td>
</tr>
</tbody>
</table>

Based on time-averaged (initial time until the forecast time) large-scale diagnostics derived from global model analyses and static predictors derived from current storm conditions (e.g., DeMaria and Kaplan 1994a; DeMaria et al. 2005; Knaff et al. 2005). Best-track locations and intensities along with global analyses were used to create the developmental datasets, and these are referred to as the SHIPS developmental dataset hereafter. These data are described in CIRA (2016a).

A number of potential predictors were selected based on past research, as shown in Table 2. These include $F_{R5}$ (SIZE), current intensity (VM), and 12-h intensity changes (PER). These three predictors are based solely on initial conditions and are referred to as static predictors. It is also known that storms tend to grow in terms of R5 as they intensify (K14). To better capture the potential intensification, potential intensity (PI) is included as a predictor. PI is defined by the SST-based empirical relationships of DeMaria and Kaplan (1994b) and Whitney and Hobgood (1997) in both the Atlantic and the Southern Hemisphere, and the East/central Pacific, respectively. PI in the WPAC is formulated as in the NATL, but the coefficients are $A = 19.7$ kt, $B = 88.0$ kt, and $C = 0.1909$. Relative humidity in the middle layers of the atmosphere (RH) is also purported to influence TC structure and size variations (e.g., Hill and Lackmann 2009; Xu and Wang 2010). Maclay et al. (2008) also showed how low-level temperature advection (TADV) and temperature gradients (TGR); vertical wind shear (VWS); trough interactions, which are related to relative eddy flux convergence (REFC); divergence at 200 hPa (D200); and sea surface temperature (SST) may play a role in TC in increasing the TC wind field (i.e., kinetic energy). Lee et al. (2010) showed how initial size (radial extent of 17 m s$^{-1}$ wind speeds) and environmental relative vorticity (Z850) may also play a role in future size evolution (i.e., the idea of TC pedigree). Finally, it has long been known that latitude plays a role in TC size variations (Merrill 1984). This predictor set is similar to those used by Kozar and Misra (2014) to predict TC kinetic energy in the NATL.

As in the development of other statistical–dynamical models, we use a stepwise variable selection procedure where the 1% probabilities (based on an F test) were used for adding and removing variables at each step (see Wilks 2006, p. 210). Once the variables are selected for all lead times, a forward model is created that makes use of the complete set of those variables, mirroring the successful methodology used in SHIPS. All of the SHIPS developmental data were used to train regressions for our four separate TC basins. The regression equations will later be used to make a number of independent forecasts that will be discussed in the results section.

As a real-time application, these regression equations will predict $\Delta F_{R5}(t)$. Adding the initial $F_{R5}$ (i.e., SIZE) to the forecast changes provides a forecast of $F_{R5}(t)$. To create forecasts of the TC size or R5(t), one multiplies $F_{R5}(t)$ by the intensity-based climatology of R5 (i.e., R5) using the forecast value of intensity at that time VM(t). For this study, VM(t)$^4$ comes from the decay-SHIPS forecast, which empirically decays the TC when it encounters land using the relationships described in DeMaria et al. (2006) and has implications for the predictive skill that will be discussed in the results section.

Summarizing, using the regression-based forecast of $\Delta F_{R5}(t)$ based on current conditions and forecast SHIPS diagnostics, as well as intensity forecasts VM(t), forecasts of the normalized TC size $F_{R5}(t)$, and more importantly TC size R5(t), are made. Recent work has shown how R5 and VM along with a storm motion vector can be used to estimate wind radii (Knaff et al. 2016, hereafter K16) using a vortex

\[ \text{PI(kt)} = A + Be^{C(30.0 - \text{SST})} \]

\[ \text{PI(kt)} = D + E(\text{SST}) \]
model. This approach is also used here and is described next.

c. Wind radii via a vortex model

Given forecasts of $R_5(t)$, wind radii are then estimated using a vortex modeling approach, which was designed primarily for and is most valid for the purely tropical cyclone vortex (i.e., the vast majority of forecast cases). This procedure is illustrated in Fig. 3 using the observed $R_5$ and best-track conditions for Hurricane Amanda at 0000 UTC 25 May. This is done by using a parametric model, namely the modified Rankine vortex (MRV), for each wind radii threshold (i.e., 34, 50, and 64 kt), where the azimuthally averaged wind field is a function of the intensity $V_M$, radius $r$, and a shape parameter $x$. The MRV was chosen for its simplicity and its proven stability in the operational setting, its use in previous work (cf. Demuth et al. 2006, K07, and K16), and its ability to incorporate azimuthal wavenumber-1 asymmetries. To account for these asymmetries as a function of azimuth in terms of the angle measured from a direction $90^\circ$ to the right (Northern Hemisphere) of the storm heading $u$, parameters $\theta_\alpha$, the degree of rotation of the asymmetry from the direction $90^\circ$ to the right of the storm motion vector, and the variable $a$.

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**TABLE 2.** Potential independent variables or predictors tested for their ability to predict the changes of the normalized TC size from the initial forecast time $\Delta F_{R5}(t)$. The basins where these predictors were selected are also provided.

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
<th>Averaging area</th>
<th>Basin selected</th>
</tr>
</thead>
<tbody>
<tr>
<td>SIZE</td>
<td>Initial normalized $F_{R5}$</td>
<td></td>
<td>All</td>
</tr>
<tr>
<td>VM</td>
<td>Current intensity</td>
<td></td>
<td>All</td>
</tr>
<tr>
<td>PER</td>
<td>12-h intensity trend</td>
<td></td>
<td>All</td>
</tr>
<tr>
<td>PI</td>
<td>Potential intensity</td>
<td>Same as SST</td>
<td>All</td>
</tr>
<tr>
<td>RH</td>
<td>Relative humidity (700–500 hPa)</td>
<td>200–800 km</td>
<td>All</td>
</tr>
<tr>
<td>TGR</td>
<td>Temp gradient (850–700 hPa) (from south to north)</td>
<td>0–500 km</td>
<td>All</td>
</tr>
<tr>
<td>D200</td>
<td>200-hPa divergence</td>
<td>0–1000 km</td>
<td>All</td>
</tr>
<tr>
<td>LAT</td>
<td>Sine of latitude</td>
<td></td>
<td>All</td>
</tr>
<tr>
<td>SST</td>
<td>Sea surface temp</td>
<td>At the TC center</td>
<td>All</td>
</tr>
<tr>
<td>REFC</td>
<td>Relative eddy flux convergence (Northern Hemisphere convention)</td>
<td>100–600 km</td>
<td>NATL, WPAC, SHEM</td>
</tr>
<tr>
<td>TADV</td>
<td>Temperature advection (850–700 hPa) (veering/backing Northern Hemisphere convention)</td>
<td>0–500 km</td>
<td>NATL, WPAC, SHEM</td>
</tr>
<tr>
<td>VWS</td>
<td>Vertical wind shear (200–850 hPa)</td>
<td>0–500 km</td>
<td>EPAC, WPAC, SHEM</td>
</tr>
<tr>
<td>Z850</td>
<td>Vorticity at 850 hPa</td>
<td>0–1000 km</td>
<td>WPAC, SHEM</td>
</tr>
</tbody>
</table>

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**Fig. 3.** (left) The inputs needed, values calculated, and resulting wind radii estimates based on the best track of Hurricane Amanda (2014) at 0000 UTC 25 May and (right) the corresponding IR image with the wind radii estimates overlaid.
defined as the magnitude of the asymmetry, are also required. The MRV equations used for this study are provided below. The MRV parameters are estimated from a combination of regression and climatology and closely follow the methodology discussed in K16. To further aid the reader, descriptions of the vortex model variables are also provided in Table 3:

Table 3. Variables used in the construction of the parametric vortex model presented in section 2c along with a brief description and physical interpretation (when needed).

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
<th>Physical interpretation</th>
</tr>
</thead>
<tbody>
<tr>
<td>( r )</td>
<td>Radius</td>
<td>Accounts for storm heading by placing the largest asymmetry to the right of motion (Northern Hemisphere)</td>
</tr>
<tr>
<td>( \theta )</td>
<td>Azimuth, 90° to the right (Northern Hemisphere) of heading</td>
<td></td>
</tr>
<tr>
<td>( \theta_o )</td>
<td>Degree of azimuthal rotation with respect to ( \theta )</td>
<td>Allows the asymmetry to move relative to its position determined by ( \theta )</td>
</tr>
<tr>
<td>( a )</td>
<td>Magnitude of the wavenumber-1 asymmetry</td>
<td>Determines the size of the wavenumber-1 asymmetry</td>
</tr>
<tr>
<td>VM</td>
<td>Max wind</td>
<td>Peak wind in the vortex</td>
</tr>
<tr>
<td>( R_m )</td>
<td>Radius of max winds</td>
<td>Location of max wind</td>
</tr>
<tr>
<td>( R_{th} )</td>
<td>Radius of a given threshold ( th )</td>
<td>Azimuthally averaged wind radii</td>
</tr>
<tr>
<td>( B )</td>
<td>Bias correction for the azimuthally averaged wind radii</td>
<td>Accounts for the use of nonzero wind radii to create azimuthally averaged ( R_{th} )'s</td>
</tr>
<tr>
<td>( x )</td>
<td>Rankine vortex shape parameter</td>
<td>Determines the vortex shape or decay rate of the winds outside the radius of maximum winds</td>
</tr>
<tr>
<td>( c )</td>
<td>Vortex translations speed</td>
<td>Scalar of vortex motion</td>
</tr>
<tr>
<td>( \gamma )</td>
<td>Vortex latitude</td>
<td></td>
</tr>
<tr>
<td>( V(r, \theta) )</td>
<td>Wind speed as a function of radius and azimuth in terms of ( \theta )</td>
<td>Note that for this application ( V ) is calculated for each available wind threshold ( th )</td>
</tr>
</tbody>
</table>

for the use of nonzero azimuthal averages in these regression equations, an additional empirically derived bias correction \( B \) is applied to each regression result as a function of distance between \( R_m \) and \( R_{th} \) and is given by

\[
B = 0.0607 \ln(R_{th} - R_m) + 0.6395, \quad (R_{th} - R_m) > 0. \tag{4}
\]

The \( x_{th} \) values are then estimated [see Eq. (5) below]. Note that for this algorithm \( x_{th} \) are also constrained to fall between 0.1 and 1.0, where the latter value implies the vortex wind profile conserves angular momentum:

\[
x_{th} = \log \left[ \frac{\text{th}}{VM} \right] / \left( \frac{R_m}{R_{th}} \right). \tag{5}
\]

To account for the asymmetries as a function of azimuth \( \theta \), the degree of rotation of the asymmetry from the direction of 90° to the right of the storm motion vector \( \theta_o \), and the magnitude of the asymmetry \( a \), are required. To calculate \( a \) and \( \theta_o \), the climatological relationships developed for the North Atlantic version of DRCL (i.e., Table 1 in K07) are used. These relationships represent the best fit that minimized the mean square differences between the observed wind radii and those calculated from the parametric model for a large sample of cases found in the extended best track (Demuth et al. 2004) during 1988–2003 (see K07). The use of these climatological asymmetries as a function of...
motion is justified by the results of both Uhlhorn et al. (2014) and Klotz and Jiang (2016), who showed that surface azimuthal wind asymmetries are to first order as a result of translation. The storm motion vector is calculated from the track forecasts associated with the decay-SHIPS intensity forecast. In this formulation,

\[ a = 1.06 + 0.28c - 0.0026c^2 - 0.08(|\gamma| - 25) \]  
\[ \theta_o = 17.0 + 0.08(|\gamma| - 25) - 1.05c, \]

where \( c \) is the storm speed (kt) and \( \gamma \) is the latitude. The same values of \( a \) and \( \theta_o \) are used for each wind speed threshold. Note that for SHEM TCs the asymmetries are a mirror image of those of the Northern Hemisphere.

Using the parameters \( VM, R_m, a, \theta_o, \) and \( \theta \) (i.e., perpendicular to the provided motion vector); \( x_{34}, x_{50}, \) and \( x_{64} \); and the MRV equations [Eqs. (3a) and (3b)], complete vortices for each wind threshold (i.e., \( V_{34}, V_{50}, \) and \( V_{64} \)) are constructed for each forecast time. The value of \( VM(t) \) determines which vortex equations are used. For instance, if \( VM(t) = 60 \) kt at \( t = 48 \) h, only \( V_{34} \) and \( V_{50} \) are constructed at the 48-h forecast time. By searching through each azimuth (16 azimuthal directions in this case), the maximum extent of each wind threshold in each earth-relative quadrant is found. In this manner the traditional wind radii can be estimated. Again, Fig. 3 illustrates the steps taken to estimate wind radii given inputs based on the best track and satellite imagery, and Table 3 provides the variables used along with their description. While this description seems complicated, it is generally less involved, especially in terms of programming and maintenance, than trying to predict wind radii in individual quadrants. This vortex model approach also ensures results that are consistent with the intensity forecast \( VM(t) \).

d. Validating wind radii

Forecast values of 34-, 50-, and 64-kt wind radii in each quadrant and at each forecast lead time are compared with the final best-track values in the NATL and EPAC to validate forecasts. At present, the WPAC and SHEM wind radii are not best tracked following the season, and forecasts in those basins will not be validated. The occurrence of zero-valued wind radii introduces an added complication when verifying wind radii. The zero-valued wind radii typically occur when storms are near the wind radii threshold intensity or when storms are translating rapidly. For this study, the verification strategy follows that of Sampson and Knaff (2015), as follows. If any of the quadrants in the best track have nonzero wind radii, all quadrants for that case are tested. This strategy allows the individual quadrant statistics to be combined to form a single measurement of mean absolute error and bias for each forecast lead time.

For comparison, the validation of the vortex model presented in section 2c, with the bias correction, produced 34-kt wind radii mean absolute errors of 25 and 33 n mi and biases of 11 and \(-11 \) n mi, based on 2 yr (2014–15) of scatterometry imagery in the NATL and EPAC (243 cases) and a wind radii best track for the WPAC (3138 cases), as reported in Sampson et al. (2017). These validations were performed for all cases, including TCs transitioning to an extratropical structure or those that had an extratropical structure that were contained in the best track. Our results are based the same approach.

3. Results

a. Selected variables and interpretation

The stepwise multiple regression procedure selected 11, 10, 13, and 12 predictors for the NATL, EPAC, WPAC, and SHEM basins from the list of potential predictors in Table 2. In the NATL, the predictors \( Z_{850} \) and VWS were not selected in the procedure. In the EPAC, on the other hand, the TADV, REFC, and \( Z_{850} \) predictors were not selected. In the SHEM, only the PI predictor was not selected and in the WPAC all the potential predictors were selected. To help the reader, Table 2 also lists the basins in which each potential predictor is used. The lack of statistical importance of \( Z_{850} \) as a predictor in the NATL and EPAC likely indicates that most TCs are moving in a trade wind environment for most of their life cycles in those basins. In a similar manner, the statistical unimportance of TADV and REFC in the EPAC may also reflect the infrequent encounters of TCs with strong atmospheric temperature gradients and troughs.

The normalized regression coefficients for the PI, SST, and VM terms are large and sometimes indicate relationships that are opposite of physical reasoning. Such behavior in multiple regressions often signals that the linear model is trying to accommodate a nonlinear behavior. To examine the underlying relationships, \( \Delta F_{R5} \) as a function of SST and VM at a lead time of 48 h is plotted, while holding the other variables fixed (Fig. 4). TC growth in each basin behaves quite differently in the SST and VM parameter space. The NATL panel indicates that all TCs in the NATL tend to grow over the entire SST and VM space, with the largest
growth occurring for TCs in very warm SST environments. In the EPAC, growth again generally occurs in the warmest SSTs (i.e., >28.5°C), but below that SST TCs tend to shrink. In contrast, the WPAC TCs seem to grow only slightly in a relatively narrow range of moderate SSTs and only at the highest intensities. This may indicate growth during rather intense TC weakening as they encounter progressively cooler SST conditions. In the SHEM, weaker TCs appear to prefer growth over quite warm SSTs (>29°C), but TCs generally shrink in cooler SST conditions. Plots from other lead times are similar to those shown in Fig. 4.

To examine the strength and signs of the remaining relationships in the multiple regression equations, Fig. 5 shows the normalized regression coefficients for the remaining predictor set at 24, 48, 72, 96, and 120 h and in
The strongest and most consistent relationships are between the SIZE, LAT, D200, and RH. The signs of these relationships suggest that storms that are large (small) relative to the mean SIZE tend to shrink (grow). The regressions also suggest that greater than average D200 and RH also promote growth of TCs. The latter (higher RH promotes growth) is consistent with previous modeling results, such as those of Hill and Lackmann (2009) and Xu and Wang (2010). Less interesting is the finding that higher LAT is also related to TC growth, which has long been known (i.e., Merrill 1984).

Predictors with less pronounced forecast influence include PER, TGR, REFC, TADV, VWS, and Z850. Intensification (i.e., positive PER) promotes the slight shrinking of TCs in all basins. Similarly, positive (Northern Hemisphere) REFC, as it promotes vortex intensification when other factors are held constant or favorable (e.g., Molinari and Vollaro 1989, 1990; DeMaria et al. 1993; Leroux et al. 2016, and additional references therein), also promotes a reduction in storm sizes. Positive Z850 (Northern Hemisphere) appears to be related to TC growth in the SHEM and WPAC where TCs often form in monsoon trough environments (equatorial westerlies converging with poleward easterlies). This is likely due to imports of low-level angular momentum in monsoon trough environments consistent with the findings of Chan and Chan (2013, 2015). Positive TADV
(Northern Hemisphere convention) is generally associated with TC growth and is consistent with the findings of Maclay et al. (2008). The remaining terms TGR and VWS seem to have more variable interpretations. Alone, increased VWS and TGR are related to growth, but the increased TGR is also related to zonal wind shear, which complicates the interpretation.

b. Independent performance

To assess the performance of these wind radii forecasts, the 2014 and 2015 seasons are reforecast in the NATL and EPAC. Reforecasts are based on real-time NHC advisories, decay-SHIPS intensity, track, and large-scale diagnostics. These diagnostics were created in real time at NHC and are based on the available real-time Global Forecast System (GFS) forecasts. IR-based TC size estimates were calculated after the fact, but using the real-time advisory information. Thus, the reforecasts simulate nearly identically a system that was run in real time, save for small (0.5 h) differences in IR image availability. These decay-SHIPS-based wind radii (DSWR) forecasts are also independent of the developmental dataset.

Figures 6 and 7 shows the mean absolute error (MAE) and bias statistics in the NATL and EPAC. For simplicity, a single measure for the MAE/bias is shown where the performance of the geographic quadrants is combined. The EPAC is further broken down to storms forming in the central Pacific (140°W–180°) and east Pacific (east of 140°W), as different organizations construct the best tracks of these storms. The statistical significance of these results versus other forecasts or a baseline is difficult to assess because of the numbers of cases (Table 4) and the strong serial correlations.
between adjacent times. Results indicate that MAEs are typically less than 30, 20, and 10 n mi for the 34-, 50-, and 64-kt wind radii forecasts, respectively. These are rather respectable results given the vortex model’s capabilities discussed in section 3d. The biases are negative in the EPAC basins and straddle zero in the NATL. The biases appear to be somewhat related to decay-SHIPS intensity errors that were slightly negative to near zero in the Atlantic and slightly negative to distinctly negative (less than −5 kt) in the east Pacific, with negative biases in the central Pacific during these two seasons (Cangialosi and Franklin 2015, 2016). Note the vortex model’s positive biases in these basins versus scatterometry fixes.

Overall, our results suggest that these forecasts are competitive with forecasts made by regional hurricane forecast models and the DRCL (K07) used for skill analysis (see Figs. 4 and 5 in Sampson and Knaff 2015). One benefit of the DSWR is that its forecasts are relatively independent of other forecasts7 and that adding them to a wind radii forecast consensus (cf. Sampson and Knaff 2015) generally reduces the consensus 34-, 50-, and 64-kt wind radii forecast errors. In fact, these decay-SHIPS-based forecasts result in no degradation or reductions of consensus errors (on the order of 0–1 n mi) and reduction of negative biases based on a 2014–15 EPAC and NATL sample. For instance, 34-kt wind radii forecasts are improved by 1, 1, 0, 1, and 0 n mi with bias reductions of 1, 1, 1, 1, and 1 n mi at 12-, 24-, 36-, 48-, and 72-h lead times. These reductions of about 1 n mi are also found for 50- and 64-kt wind radii forecasts.

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7 This concept of consensus member independence and consensus improvement is described in the appendixes in Sampson et al. (2008).
thresholds, with the majority of the error reduction coming from improved biases.

c. Example forecasts

Two forecasts are now presented to give the reader an idea of what representative forecasts look like and how they compare to the corresponding best tracks. We have purposely chosen cases in which track and intensity forecasts were close, yet not identical, to the verification so that we could more confidently discuss predicted changes in the wind radii unrelated to those predictors while still highlighting the dependencies of wind radii on the forecast track and intensity.

Figure 8 shows the DSWR forecasts of Hurricanes Edouard (al062014) and Linda (ep152015) and the corresponding best tracks. To improve readability, only the 34- and 64-kt wind radii are shown for these cases. The 0000 UTC 12 September DSWR forecast and corresponding best track are shown for Edouard (Fig. 8, top two panels). During the 5-day forecast, Edouard intensified and recurved. During the intensification period, the wind radii expanded. A similar pattern of behavior is seen in the DSWR forecast, but the wind radii are handicapped by the underforecast of intensity and a track forecast that does not indicate recurvature. Similarly, early in the Edouard forecast the intensity forecasts were too high, leading to slightly larger 34-kt wind radii in the northeast quadrants. The bottom two panels in Fig. 8 show the 0000 UTC 8 September forecast for Linda and the corresponding best track. During the 5-day forecast, Linda intensified and recurved. During the intensification period, the wind radii expanded. A similar pattern of behavior is seen in the DSWR forecast, but the wind radii are handicapped by the underforecast of intensity and a track forecast that does not indicate recurvature. Similarly, early in the Linda forecast the intensity forecasts were too high, leading to slightly larger 34-kt wind radii in the northeast quadrants.

4. Summary, discussion, and future work

This paper has detailed a statistical–dynamical method for forecasting wind radii using decay-SHIPS intensity and track forecasts, associated large-scale GFS-forecast-based diagnostic files, and information derived from current IR imagery and TC advisories. The independent variable predicted is the change from t = 0 of the normalized (by intensity) IR-based TC size or R5 (see K14). The estimation of the wind radii is done parametrically using the method of K16 and utilizing the decay-SHIPS track and intensity forecast along with the predicted changes in the IR-based TC size R5. The method produces stable forecasts of wind radii that are competitive with the current operational methods. Furthermore, the addition of these independent forecasts into wind radii consensus forecasts (Sampson and Knaff 2015) suggests that the forecasts provide independent information that reduces forecast errors and bias among the consensus forecasts at most forecast lead times and all wind radii.

This model has been developed for the majority of tropical cyclone basins. Here, we compare to the NHC-based best tracks of wind radii in the NATL and EPAC, as such validation datasets do not yet exist in the WPAC or SHEM. The model is currently running and making forecasts for all of these basins at the Cooperative Institute for Research in the Atmosphere. The forecasts in the NATL and EPAC are also being tested by the Joint Hurricane Testbed and should be soon incorporated.
into the real-time experimental processing in the operational computing environment at NHC. In the very near future, these methods should also be transitioned to the Automated Tropical Cyclone Forecast System (ATCF; Sampson and Schrader 2000) and operations at the JTWC, where they will become part of the wind radii consensus forecast. It is here that this capability may be most important as it is expected that this consensus capability should dramatically improve JTWC’s wind radii estimates and forecasts, which will provide improved input to several operational products including wind speed probabilities (DeMaria et al. 2009, 2013), wave forecasts (Sampson et al. 2010, 2013, 2016), model initialization (e.g., Trahan and Sparling 2012), and improved objectively determined Department of Defense TC conditions of readiness (Sampson et al. 2012).

Since all the information needed to estimate the minimum sea level pressure (MSLP) using the wind–pressure relationship (WPR) of Courtney and Knaff (2009) is available, forecast values of MSLP($t$) that are consistent with decay-SHIPS intensity, track, and wind radii forecasts are created and provided with the wind radii forecasts. This WPR explicitly accounts for MSLP variations as a function of VM, storm latitude, 34-kt wind radii, and storm translation speed, and should produce physically consistent MSLP forecasts. This WPR is also used at NHC, JTWC, and the Australian tropical cyclone warning centers (Perth, Western Australia; Darwin, Northern Territory; and Brisbane, Queensland) to determine MSLPs operationally. The addition of MSLP estimates is provided and will be validated/evaluated in the future. It is also recognized that MSLP is not forecast by NHC nor JTWC. However, some WMO regional meteorological specialized centers make MSLP forecasts, noting that many of the regional specialized meteorological centers (RSMCs) routinely

*Fig. 8. (left) DSWR forecasts for Hurricanes (top) Edouard (0000 UTC 12 Sep 2014) and (bottom) Linda (0000 UTC 8 Sep 2015) with (right) corresponding best tracks. To improve the esthetics and readability of the figures, only the 34- and 64-kt wind radii are shown, the latter being shown as inner concentric rings when the intensity exceeds 64 kt. Note how intensity biases affect the forecast of wind radii with under- (over-) forecasts of intensity corresponding to slightly smaller (larger) 34-kt wind radii.*
receive JTWC’s guidance products. MSLP estimates are also useful for other TC risk applications like storm surge and risk models that use pressure-based vortex parameterizations [e.g., the Holland (1980) model]. Before being employed in operations, the coefficients will be updated to use a longer developmental dataset, noting that we left out 2yr here to test the scheme with independent data. Finally, the vortex model used in this work uses climatological motion-relative asymmetries. These asymmetries can likely be improved by 1) incorporating known causes of convective and wind field asymmetries into this methodology and 2) specifically addressing the extratropical transitioning and extratropical stages of TCs. That work will be the focus of future studies.

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