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## Supplemental Material

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1 **Supplemental Material for:**

2 **Using climate model simulations to constrain observations**

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## 19 **1. Statistical analysis**

20 The statistical analysis presented in this section closely follows Santer et al. (2011), with only  
21 minor modifications to the notation and text.

### 22 *a. Notation*

23 This section introduces the statistical notation used for comparing atmospheric temperature  
24 changes in models, reanalysis, and satellite data in Fig. 8. These comparisons involve least-  
25 squares linear trends and regression coefficients, referred to collectively as “metrics”. Metrics are  
26 calculated for overlapping  $L$ -month analysis periods. We consider four specific values of  $L$  here:  
27 120, 240, 360, and 480 months. We do not explicitly include the timescale  $L$  in our notation.

#### *Abbreviations*

MMA	Multi-model average
MMSD	Multi-model sampling distribution of metric
SMSD	Single-model sampling distribution of metric

#### *Subscripts*

$o$	Subscript denoting observationally based data (satellite data or reanalysis)
$c$	Subscript denoting output from model control runs
$f$	Subscript denoting output from model forced experiments

#### *Indices*

$i$	Index over number of maximally overlapping analysis periods in observations
$j$	Index over number of models
$k$	Index over number of HIST+RCP8.5 or HIST+SSP5 realizations

#### *Sample sizes*

$L$	Length of period for trend/regression calculations (in months)
$N_o$	Total number of overlapping $L$ -month analysis periods in observed data set (calculated over 1979 to 2019)
$N_c$	Total number of overlapping $L$ -month analysis periods in control run MMSD
$N_f$	Total number of overlapping $L$ -month analysis periods in HIST+RCP8.5 or HIST+SSP5 MMSD (calculated over 1979 to 2019)
$N_c(j)$	Total number of overlapping $L$ -month analysis periods in $j^{th}$ model control run (varies with control run length)
$N_{mod}$	Total number of models (36 and 30 for CMIP5 and CMIP6 control runs; 28 for CMIP5 forced runs; 22 or 21 for CMIP6 forced runs)
$N_r(j)$	Total number of HIST+RCP8.5 or HIST+SSP5 realizations for $j^{th}$ model

*Metrics (trends or regression coefficients)*

$b_o(i)$	Metric for $i^{th}$ overlapping $L$ -month analysis period in observations
$b_c(i, j)$	Metric for $i^{th}$ overlapping $L$ -month analysis period in $j^{th}$ model control run
$b_f(i, j, k)$	Metric for $i^{th}$ overlapping $L$ -month analysis period from $j^{th}$ model and $k^{th}$ realization of HIST+RCP8.5 or HIST+SSP5 run
$\overline{b_o}$	Average of $b_o(i)$ over all overlapping $L$ -month analysis periods between 1979 and 2019

28 *b. Maximally overlapping analysis periods in Figure 8*

29 As used here and in the main text, ‘maximally overlapping’ signifies overlap by all but one month.  
30 For  $L = 120$  months, for example, the first analysis period is over January 1979 to December 1988,  
31 the second period is over February 1979 to January 1989, *etc.* All metrics were computed from  
32 time series of monthly-mean anomalies of spatially-averaged TLS, corrected TMT, and TLT data.  
33 In the satellite and reanalysis data and the HIST+RCP8.5 and HIST+SSP5 simulations, anomalies  
34 were defined relative to climatological monthly means over the full 492-month period from January  
35 1979 to December 2019. Control run anomalies were defined relative to climatological monthly  
36 means calculated over the full length of each model’s control integration.

37 Here,  $N_o$ ,  $N_c$ , and  $N_f$  are the total number of maximally overlapping  $L$ -month analysis periods  
38 in observations, the control run multi-model sampling distribution (MMSD), and the MMSD of  
39 extended HIST simulations (respectively). In each observational record,  $N_o = 373$  for  $L = 120$   
40 months. For the case of  $L = 120$  and CMIP5 control run data,  $N_c = 224904$ . For  $L = 120$  months and  
41 CMIP5 HIST+RCP8.5 runs,  $N_f = 45879$  ( $373$  maximally overlapping trends  $\times$   $123$  realizations).

42 The time series of spatially-averaged temperature anomalies from individual models are not  
43 concatenated prior to calculating  $L$ -month trends and regression coefficients. Concatenating could  
44 spuriously inflate trends and regression coefficients spanning the ‘splice point’ between two model  
45 control runs or two model extended HIST runs with large differences in the amplitude of their  
46 variability. Instead, metrics for maximally overlapping analysis periods are calculated separately  
47 from each individual model’s control run or extended HIST simulation. Metrics for each model are  
48 then accumulated in multi-model distributions of unforced and unforced results. These multi-model  
49 distributions are shown in Fig. 8.

50 *c. Use of overlapping analysis periods*

51 Our use of maximally overlapping  $L$ -month analysis periods has the advantage of reducing the  
52 impact of seasonal and interannual noise on the temperature trends and the tropical amplification  
53 metric that are of interest here. However, it has the disadvantage of decreasing the statistical  
54 independence of the metrics calculated for the individual  $L$ -month “sliding windows”.

55 While non-independence of samples is an important issue in formal statistical significance testing,  
56 it is not a serious concern here. This is because our metrics are not used as a basis for formal  
57 statistical tests. Instead, they simply provide useful information on whether the observed metrics

58 in Fig. 8 are unusually large relative to model-based estimates of unforced metric values, or  
59 are unusually small relative to model estimates of metrics obtained from forced runs. Note also  
60 that we process observations and model output in identical ways, with the same overlap between  
61 successive  $L$ -month analysis periods – *i.e.*, we are not generating fundamentally different temporal  
62 autocorrelation structure in the model and observational metrics.

63 Whether we employ overlapping or non-overlapping analysis periods has very small impact on the  
64 MMSDs in Fig. 8. This suggests that in both the control runs and the forced runs, the sample sizes  
65 of metrics computed from non-overlapping  $L$ -month analysis periods are adequate for obtaining  
66 reliable estimates of empirical  $p$ -values (which are not shown here).

67 In the case of the observations, however, satellite temperature records are relatively short, and the  
68 choice of whether to use overlapping or non-overlapping observed analysis periods can have a large  
69 impact on comparisons between modeled and observed metrics. For example, each observational  
70 data set contains only four non-overlapping 10-year time series segments. These four segments do  
71 not adequately sample the impact of monthly and interannual variability on observed linear trends  
72 or regression coefficients. We reduce this sampling variability by using maximally overlapping  
73  $L$ -month analysis periods and displaying timescale-average observed results in Fig. 8.

74 Even with our use of maximally overlapping trends, a 41-year record is clearly sub-optimal for  
75 reliable assessment of observed multi-decadal variability. In related work with a wide range of  
76 different statistical models of short- and/or long-term memory, however, we find no evidence that  
77 either CMIP5 or CMIP6 models systematically underestimate the amplitude of observed decadal-  
78 timescale TMT variability (Pallotta and Santer 2020).

#### 79 *d. Model independence*

80 An implicit assumption in Fig. 8 is that results from individual models are independent. This  
81 assumption is almost certainly unjustified (Masson and Knutti 2011). While it would be interesting  
82 to explore the sensitivity of our results to the selection of different subsets of independent CMIP5  
83 and CMIP6 models, we do not perform such an analysis here. The identification of independent  
84 model subsets is likely to be sensitive to the variables, statistical procedures, and metrics used to  
85 assess model dependencies (Caldwell et al. 2014).

#### 86 *e. Multi-model average time series, metrics, and spread of metrics*

87 The weighted MMA shown in Fig. 1 is calculated by first computing the average over the  $N_r(j)$   
88 HIST+RCP8.5 or HIST+SSP5 realizations of the  $j^{\text{th}}$  model, and then by averaging results over  
89 all  $N_{\text{mod}}$  models. For the weighted versions of statistical metrics (the RMS differences in Fig. 3,  
90 zonal-mean trends in Fig. 5, and MMA trends Figs. 4, 6, and 7), these two separate averaging  
91 steps are performed with the individual metrics rather than with the individual time series.

#### 92 *f. Weighting of histograms*

93 All histograms are weighted to account for model differences in either the number of extended  
94 HIST realizations or the length of control runs. Without weighting, models with more extended

95 HIST realizations or with longer control runs would have a disproportionately large effect on the  
96 multi-model sampling distributions of trends and regression coefficients.

97 The histograms in Figs. 6, 8, and 10 were plotted with the Matplotlib `pyplot.hist` function with  
98 arrays of weights and with the “`density=True`” option.<sup>i</sup> The “`density=True`” option ensures that  
99 “each bin will display the bin’s raw count divided by the total number of counts and the bin width...  
100 so that the area under the histogram integrates to 1”. Two types of weighting were performed,  
101 depending on whether the processing involves maximally overlapping analysis periods (as in Fig.  
102 8) or non-overlapping analysis periods (as in Figs. 6 and 10).

103 In the case of non-overlapping analysis periods and sampling distributions of metrics from model  
104 extended HIST runs, the weights passed to `pyplot.hist` are  $1/N_r(j)$ , where  $N_r(j)$  is the number  
105 of realizations for the  $j^{\text{th}}$  model. In the case of the maximally overlapping analysis periods, the  
106 weights for each analysis period of the  $j^{\text{th}}$  model are  $1/N_c(j)$  for control runs and  $1/N_r(j)$  for  
107 extended HIST runs, where  $N_c(j)$  is the total number of maximally overlapping  $L$ -month analysis  
108 periods for the  $j^{\text{th}}$  model control run.

109 The fits to the histograms in Figs. 6, 8, and 10 use kernel density estimation (KDE).<sup>ii</sup> As in the  
110 case of the histograms plotted with `pyplot.hist`, the same weighting and “`density=True`” option was  
111 employed in the KDE (see above). The KDE fits relied on the default Scott bandwidth estimator.

#### 112 *g. Weighted t-test*

113 We performed  $t$ -tests to determine whether there are significant differences between the CMIP5  
114 and CMIP6 volcanic TLS signals. Tests were conducted separately for the lower stratospheric  
115 temperature signals after the eruptions of El Chichón and Pinatubo. The samples in each test  
116 are the CMIP5 and CMIP6 root-mean-square (RMS) errors relative to the observed volcanic TLS  
117 signals (see caption of Fig. 3).

118 As in the case of the weighting of histograms (see Section f), we need to account for model  
119 differences in the number of extended HIST realizations. This was done with the Python module  
120 `statsmodels.stats.weightstats.ttest_ind`.<sup>iii</sup> The  $1/N_r(j)$  weights are the same as those used in  
121 histogram weighting. The  $t$ -test was conducted with `usevar='unequal'`, thus allowing for unequal  
122 variances in CMIP5 and CMIP6 RMS errors. Our null hypothesis is that there are no significant  
123 difference between CMIP5 and CMIP6 volcanic TLS signals. Estimated  $p$ -values for this null  
124 hypothesis are sensitive to whether or not weights are included (which has substantial influence on  
125 the degrees of freedom), but are insensitive to the whether the variances of the CMIP5 and CMIP6  
126 RMS errors are assumed to be equal or unequal.

#### 127 *h. Orthogonal Distance Regression*

128 We used Orthogonal Distance Regression (ODR) to calculate the slopes of the regression fits  
129 to the CMIP5 and CMIP6 trend data shown in Fig. 9. ODR has certain advantages relative to  
130 the more commonly used Ordinary Least-Squares (OLS) regression.<sup>iv</sup> In general, the regression  
131 slopes reported in Fig. 9 were consistently larger when estimated with ODR. For the regression

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<sup>i</sup>[https://matplotlib.org/3.3.3/api/\\_as\\_gen/matplotlib.pyplot.hist.html](https://matplotlib.org/3.3.3/api/_as_gen/matplotlib.pyplot.hist.html)

<sup>ii</sup><https://scikit-learn.org/stable/modules/density.html>

<sup>iii</sup>[https://www.statsmodels.org/stable/generated/statsmodels.stats.weightstats.ttest\\_ind.html](https://www.statsmodels.org/stable/generated/statsmodels.stats.weightstats.ttest_ind.html)

<sup>iv</sup>See <https://docs.scipy.org/doc/scipy/reference/odr.html>. We employed the `scipy.odr` package for ODR performing ODR.

132 between WV trends and corrected TMT trends in Fig. 9C, for example, OLS yields slopes of  
133 5.1%/decade for both the CMIP5 and CMIP6 ensembles, while the corresponding ODR slopes are  
134 5.3 and 5.5%/decade. Both the OLS and ODR regressions weighted individual trend samples to  
135 account for model differences in the number of extended HIST realizations (see Section f).

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147 **LIST OF TABLES**

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 149 in months) of the 123 CMIP5 historical and RCP8.5 simulations used in  
 150 this study. EM is the “ensemble member” identifier (see [http://cmip-  
 151 pcmdi.llnl.gov/cmip5/documents.html](http://cmip-pcmdi.llnl.gov/cmip5/documents.html) for further details). . . . . 9

152 **Table 2.** Start dates, end dates, and lengths ( $N_m$ , in months) of the 36 CMIP5 pre-  
 153 industrial control runs used in this study. EM is the “ensemble member” identi-  
 154 fier (see <http://cmip-pcmdi.llnl.gov/cmip5/documents.html> for further details).  
 155 10

156 **Table 3.** Basic information relating to the start dates, end dates, and lengths ( $N_m$ , in  
 157 months) of the 166 CMIP6 historical and SSP5 simulations used in this study<sup>§</sup>.  
 158 EM is the “ensemble member” identifier\* . . . . . 11

159 **Table 4.** Start dates, end dates, and lengths ( $N_m$ , in months) of the 30 CMIP6 pre-  
 160 industrial control runs used in this study.<sup>§</sup> EM is the “ensemble member”  
 161 identifier.\* . . . . 12

TABLE 1: Basic information relating to the start dates, end dates, and lengths ( $N_m$ , in months) of the 123 CMIP5 historical and RCP8.5 simulations used in this study. EM is the “ensemble member” identifier (see <http://cmip-pcmdi.llnl.gov/cmip5/documents.html> for further details).

Model	EM	Hist. Start	Hist. End	Hist. $N_m$	RCP8.5 Start	RCP8.5 End	RCP8.5 $N_m$
1 ACCESS1.0	rli1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
2 ACCESS1.3	rli1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
3 BCC-CSM1.1	rli1p1	1850-01	2012-12	1956	2006-01	2300-12	3540
4 BCC-CSM1.1(m)	rli1p1	1850-01	2012-12	1956	2006-01	2099-12	1128
5-14 CanESM2 historical r-1	rli1p1-r10i1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
15-24 CanESM2 historical r-2	rli1p1-r10i1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
25-34 CanESM2 historical r-3	rli1p1-r10i1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
35-44 CanESM2 historical r-4	rli1p1-r10i1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
45-54 CanESM2 historical r-5	rli1p1-r10i1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
55-57 CCSM4	rli1p1-r3i1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
58 CESM1-BGC	rli1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
59-98 CESM1-CAM5	rli1p1-r40i1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
99 CSIRO-Mk3.6.0	r10i1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
100 EC-EARTH	r8i1p1	1850-01	2012-12	1956	2006-01	2100-12	1140
101 GFDL-CM3	rli1p1	1860-01	2005-12	1752	2006-01	2100-12	1140
102 GFDL-ESM2G	rli1p1	1861-01	2005-12	1740	2006-01	2100-12	1140
103 GFDL-ESM2M	rli1p1	1861-01	2005-12	1740	2006-01	2100-12	1140
104 GISS-E2-H (p1)	rli1p1	1850-01	2005-12	1872	2006-01	2300-12	3540
105 GISS-E2-H (p3)	rli1p3	1850-01	2005-12	1872	2006-01	2300-12	3540
106 GISS-E2-R (p1)	rli1p1	1850-01	2005-12	1872	2006-01	2300-12	3540
107 GISS-E2-R (p2)	rli1p2	1850-01	2005-12	1872	2006-01	2300-12	3540
108 GISS-E2-R (p3)	rli1p3	1850-01	2005-12	1872	2006-01	2300-12	3540
109 HadGEM2-CC	rli1p1	1859-12	2005-11	1752	2005-12	2099-12	1129
110-111 HadGEM2-CC	r2i1p1-r3i1p1	1959-12	2005-12	553	2005-12	2099-12	1129
112 HadGEM2-ES	rli1p1	1859-12	2005-11	1752	2005-12	2299-12	3529
113 HadGEM2-ES	r2i1p1	1859-12	2005-12	1753	2005-12	2100-11	1140
114 MIROC5	rli1p1	1850-01	2012-12	1956	2006-01	2100-12	1140
115 MIROC-ESM-CHEM	rli1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
116 MIROC-ESM	rli1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
117 MPI-ESM-LR	rli1p1	1850-01	2005-12	1872	2006-01	2300-12	3540
118-119 MPI-ESM-LR	r2i1p1-r3i1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
120 MPI-ESM-MR	rli1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
121 MRI-CGCM3	rli1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
122 NorESM1-M	rli1p1	1850-01	2005-12	1872	2006-01	2100-12	1140
123 NorESM1-ME	rli1p1	1850-01	2005-12	1872	2006-01	2100-12	1140

TABLE 2: Start dates, end dates, and lengths ( $N_m$ , in months) of the 36 CMIP5 pre-industrial control runs used in this study. EM is the “ensemble member” identifier (see <http://cmip-pcmdi.llnl.gov/cmip5/documents.html> for further details).

	Model	EM	Start	End	$N_m$
1	ACCESS1.0	r1i1p1	300-01	799-12	6000
2	ACCESS1.3	r1i1p1	250-01	749-12	6000
3	BCC-CSM1.1	r1i1p1	1-01	500-12	6000
4	BCC-CSM1.1(m)	r1i1p1	1-01	400-12	4800
5	CanESM2	r1i1p1	2015-01	3010-12	11952
6	CCSM4	r1i1p1	800-01	1300-12	6012
7	CESM-BGC	r1i1p1	101-01	600-12	6000
8	CESM-CAM5	r1i1p1	1-01	319-12	3828
9	CMCC-CESM	r1i1p1	4324-01	4600-12	3324
10	CMCC-CM	r1i1p1	1550-01	1879-12	3960
11	CMCC-CMS	r1i1p1	3684-01	4183-12	6000
12	CSIRO-Mk3.6.0	r1i1p1	1651-01	2150-12	6000
13	FGOALS-g2	r1i1p1	201-01	900-12	8400
14	FIO-ESM	r1i1p1	401-01	1200-12	9600
15	GFDL-CM3	r1i1p1	1-01	500-12	6000
16	GFDL-ESM2G	r1i1p1	1-01	500-12	6000
17	GFDL-ESM2M	r1i1p1	1-01	500-12	6000
18	GISS-E2-H (p1)	r1i1p1	2410-01	2949-12	6480
19	GISS-E2-H (p2)	r1i1p2	2490-01	3020-12	6372
20	GISS-E2-H (p3)	r1i1p3	2490-01	3020-12	6372
21	GISS-E2-R (p1)	r1i1p1	3981-01	4530-12	6600
22	GISS-E2-R (p2)	r1i1p2	3590-01	4120-12	6372
23	HadGEM2-CC	r1i1p1	1859-12	2099-12	2881
24	HadGEM2-ES	r1i1p1	1859-12	2435-11	6912
25	INM-CM4	r1i1p1	1850-01	2349-12	6000
26	IPSL-CM5A-LR	r1i1p1	1800-01	2799-12	12000
27	IPSL-CM5A-MR <sup>§</sup>	r1i1p1	1800-01	2068-12	3228
28	IPSL-CM5B-LR	r1i1p1	1830-01	2129-12	3600
29	MIROC5	r1i1p1	2000-01	2669-12	8040
30	MIROC-ESM-CHEM	r1i1p1	1846-01	2100-12	3060
31	MIROC-ESM	r1i1p1	1800-01	2330-12	6372
32	MPI-ESM-LR	r1i1p1	1850-01	2849-12	12000
33	MPI-ESM-MR	r1i1p1	1850-01	2849-12	12000
34	MRI-CGCM3	r1i1p1	1851-01	2350-12	6000
35	NorESM1-M	r1i1p1	700-01	1200-12	6012
36	NorESM1-ME	r1i1p1	901-01	1152-12	3024

<sup>§</sup>The IPSL-CM5A-MR control run has a large discontinuity in year 2069. We therefore truncated its control run after December 2068.

TABLE 3: Basic information relating to the start dates, end dates, and lengths ( $N_m$ , in months) of the 166 CMIP6 historical and SSP5 simulations used in this study<sup>§</sup>. EM is the “ensemble member” identifier\*.

	Model	EM	Hist. Start	Hist. End	Hist. $N_m$	SSP5 Start	SSP5 End	SSP5 $N_m$
1-3	ACCESS-CM2	r1i1p1f1-r3i1p1f1	1850-01	2014-12	1980	2015-01	2100-12	1032
4-6	ACCESS-ESM1.5	r1i1p1f1-r3i1p1f1	1850-01	2014-12	1980	2015-01	2100-12	1032
7-31 32-56	CanESM5 CanESM5	r1i1p1f1-r25i1p1f1 r1i1p1f2-r25i1p1f2	1850-01 1850-01	2014-12 2014-12	1980 1980	2015-01 2015-01	2100-12 2100-12	1032 1032
57-61	CESM2 CESM2 CESM2	r1i1p1f1, r2i1p1f1 r4i1p1f1, r10i1p1f1 r1i1p1f1	1850-01 1850-01 1850-01	2014-12 2014-12 2014-12	1980 1980 1980	2015-01 2015-01 2015-01	2100-12 2100-12 2100-12	1032 1032 1032
63	CIESM	r1i1p1f1	1850-01	2014-12	1980	2015-01	2100-12	1032
64-69	CNRM-CM6.1	r1i1p1f2-r6i1p1f2	1850-01	2014-12	1980	2015-01	2100-12	1032
70-75	EC-Earth3 EC-Earth3 EC-Earth3	r1i1p1f1, r4i1p1f1 r6i1p1f1, r1i1p1f1 r13i1p1f1, r15i1p1f1	1850-01 1850-01 1850-01	2014-12 2014-12 2014-12	1980 1980 1980	2015-01 2015-01 2015-01	2100-12 2100-12 2100-12	1032 1032 1032
76-79 80	EC-Earth3-Veg EC-Earth3-Veg	r1i1p1f1-r4i1p1f1 r6i1p1f1	1850-01 1850-01	2014-12 2014-12	1980 1980	2015-01 2015-01	2100-12 2100-12	1032 1032
81	GFDL-CM4	r1i1p1f1	1850-01	2014-12	1980	2015-01	2100-12	1032
82	GFDL-ESM4	r1i1p1f1	1850-01	2014-12	1980	2015-01	2100-12	1032
83-85	HadGEM3-GC31-LL	r1i1p1f3-r3i1p1f3	1850-01	2014-12	1980	2015-01	2100-12	1032
86-88	HadGEM3-GC31-MM	r1i1p1f3-r3i1p1f3	1850-01	2014-12	1980	2015-01	2100-12	1032
89 90 91-92 93-94	IPSL-CM6A-LR IPSL-CM6A-LR IPSL-CM6A-LR IPSL-CM6A-LR	r1i1p1f1 r2i1p1f1 r3i1p1f1, r4i1p1f1 r6i1p1f1, r14i1p1f1	1950-01 1950-01 1950-01 1950-01	2014-12 2014-12 2014-12 2014-12	780 780 780 780	2015-01 2015-01 2015-01 2015-01	2300-12 2100-12 2054-12 2100-12	3432 1032 480 1032
95-144	MIROC6	r1i1p1f1-r50i1p1f1	1850-01	2014-12	1980	2015-01	2100-12	1032
145	MIROC-ES2L	r1i1p1f2	1850-01	2014-12	1980	2015-01	2100-12	1032
146-147	MPI-ESM-1.2-HR	r1i1p1f1, r2i1p1f1	1850-01	2014-12	1980	2015-01	2100-12	1032
148-157	MPI-ESM-1.2-LR	r1i1p1f1-r10i1p1f1	1850-01	2014-12	1980	2015-01	2100-12	1032
158	MRI-ESM2.0	r1i1p1f1	1850-01	2014-12	1980	2015-01	2300-12	3432
159-160	NESM3	r1i1p1f1, r2i1p1f1	1850-01	2014-12	1980	2015-01	2100-12	1032
161	NorESM2-MM	r1i1p1f1	1850-01	2014-12	1980	2015-01	2100-12	1032
162-165 166	UKESM1.0-LL UKESM1.0-LL	r1i1p1f2-r4i1p1f2 r8i1p1f2	1850-01 1850-01	2014-12 2014-12	1980 1980	2015-01 2015-01	2100-12 2100-12	1032 1032

<sup>§</sup> CMIP6 model acronyms are from: [https://pcmdi.llnl.gov/CMIP6/ArchiveStatistics/esgf\\_data\\_holdings/](https://pcmdi.llnl.gov/CMIP6/ArchiveStatistics/esgf_data_holdings/)

\* See: [https://docs.google.com/document/d/1h0r8RZr\\_f3-8egBMMh7aqLwy3snpD6\\_MrDz1q8n5XUk/edit](https://docs.google.com/document/d/1h0r8RZr_f3-8egBMMh7aqLwy3snpD6_MrDz1q8n5XUk/edit)

TABLE 4: Start dates, end dates, and lengths ( $N_m$ , in months) of the 30 CMIP6 pre-industrial control runs used in this study.<sup>§</sup> EM is the “ensemble member” identifier.\*

	Model	EM	Start	End	$N_m$
1	ACCESS-CM2	rli1p1f1	950-01	1449-12	6000
2	ACCESS-ESM1.5	rli1p1f1	101-01	1000-12	10800
3	CESM2	rli1p1f1	1-01	1200-12	14400
4	CESM2-FV2	rli1p1f1	1-01	500-12	6000
5	CESM2-WACCM	rli1p1f1	1-01	499-12	5988
6	CESM2-WACCM-FV	rli1p1f1	1-01	500-12	6000
7	CNRM-CM6.1-HR	rli1p1f2	1850-01	2149-12	3600
8	CNRM-ESM2.1	rli1p1f2	1850-01	2105-12	3072
9	E3SM-1.0	rli1p1f1	1-01	500-12	6000
10	E3SM-1.1	rli1p1f1	1850-01	2014-12	1980
11	E3SM-1.1-ECA	rli1p1f1	1850-01	2014-12	1980
12	EC-Earth3	rli1p1f1	2259-01	2759-12	6012
13	EC-Earth3-Veg	rli1p1f1	1850-01	2349-12	6000
14	GFDL-CM4	rli1p1f1	151-01	650-12	6000
15	GFDL-ESM4	rli1p1f1	1-01	500-12	6000
16	HadGEM3-GC31-LL	rli1p1f1	1850-01	2349-12	6000
17	INM-CM4.8	rli1p1f1	1850-01	2380-12	6372
18	INM-CM5.0	rli1p1f1	1996-01	3196-12	14412
19	IPSL-CM6A-LR	rli1p1f1	1850-01	3049-12	14400
20	MIROC6	rli1p1f1	3200-01	3999-12	9600
21	MIROC-ES2L	rli1p1f2	1850-01	2349-12	6000
22	MPI-ESM-1.2-HAM	rli1p1f1	1850-01	2629-12	9360
23	MPI-ESM-1.2-HR	rli1p1f1	1850-01	2349-12	6000
24	MPI-ESM-1.2-LR	rli1p1f1	1850-01	2849-12	12000
25	MRI-ESM2.0	rli1p1f1	1850-01	2550-12	8412
26	NorCPM1	rli1p1f1	1-01	500-12	6000
27	NorESM2-LM	rli1p1f1	1600-01	2100-12	6012
28	NorESM2-MM	rli1p1f1	1200-01	1699-12	6000
29	SAM0-UNICON	rli1p1f1	1-01	700-12	8400
30	UKESM1.0-LL	rli1p1f2	1960-01	2709-12	9000

<sup>§</sup> CMIP6 model acronyms are from: [https://pcmdi.llnl.gov/CMIP6/ArchiveStatistics/esgf\\_data\\_holdings/](https://pcmdi.llnl.gov/CMIP6/ArchiveStatistics/esgf_data_holdings/)

\* See: [https://docs.google.com/document/d/1h0r8RZr\\_f3-8egBMMh7aqLwy3snpD6\\_MrDz1q8n5XUk/edit](https://docs.google.com/document/d/1h0r8RZr_f3-8egBMMh7aqLwy3snpD6_MrDz1q8n5XUk/edit)