Radiative Transfer Modeling of a Coniferous Canopy Characterized by Airborne Remote Sensing

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ABSTRACT

Solar radiation beneath a forest canopy can have large spatial variations, but this is frequently neglected in radiative transfer models for large-scale applications. To explicitly model spatial variations in subcanopy radiation, maps of canopy structure are required. Aerial photography and airborne laser scanning are used to map tree locations, heights, and crown diameters for a lodgepole pine forest in Colorado as inputs to a spatially explicit radiative transfer model. Statistics of subcanopy radiation simulated by the model are compared with measurements from radiometer arrays, and scaling of spatial statistics with temporal averaging and array size is discussed. Efficient parameterizations for spatial averages and standard deviations of subcanopy radiation are developed using parameters that can be obtained from the model or hemispherical photography.

1. Introduction

Forest canopies strongly modify radiative fluxes reaching the underlying surface. This has important implications for hydrological and ecological processes, such as snowmelt and succession, in forested environments (Pomeroy and Dion 1996; Battaglia et al. 2002; Hardy et al. 2004). Conversely, radiation reflected and emitted from trees complicates the retrieval of forest snow properties by remote sensing (Chang et al. 1996; Klein et al. 1998). Land surface models and remote sensing algorithms, therefore, often include simple representations of radiative transfer in canopies. Variants of Beer’s law or two-stream approximations are generally used (e.g., Sellers et al. 1986; Verseghy et al. 1993); these treat canopies as horizontally homogeneous turbid media and only predict the average radiation. The radiative environment beneath real canopies, however, is highly heterogeneous because of sun flecks, canopy gaps, and clearings on wide ranges of length scales. The significance of spatial heterogeneity at a particular length scale will depend on the time scale and nonlinearity of the process of interest. In snowmelt, for example, the spatial variance of shortwave radiation influences the depletion of snow-covered area (Essery and Pomeroy 2004) and longwave radiation from sunlit trunks (Faria et al. 2000; Woo and Giesbrecht 2000).

Geometrical optics and ray-tracing models have been used to simulate radiative transfer in canopies; the Radiation Transfer Model Intercomparison (Pinty et al. 2004) found that such models now compare well for homogeneous canopies but still have large discrepancies for complex heterogeneous canopies. These models are also computationally expensive and require large amounts of data on canopy structure and the optical properties of canopy elements. A great deal of work on small-scale radiative transfer through heterogeneous canopies has used statistical models that assume random tree distributions or spatially explicit models with randomly generated tree distributions.
(e.g., Satterlund 1983; Li et al. 1995; Yang et al. 2001; Song and Band 2004). Fewer studies have used real structural data from natural or managed forests (e.g., Courbaud et al. 2003; Stadt et al. 2005). Hemispherical photography provides a method for relatively rapid gathering of canopy structure information in the field (Rich 1990), and several software packages have been developed for modeling forest light environments from hemispherical photography, but it is difficult to apply this to large areas or inaccessible locations. Airborne remote sensing enables collection of large amounts of canopy data but has not yet been widely used in radiation modeling.

The aims of this paper are to demonstrate the use of remote sensing in mapping of forest stand characteristics for radiative transfer modeling, to develop a model that uses stand maps to simulate patterns of solar radiation beneath the canopy, to evaluate the model in comparison with ground-based measurements, to investigate the spatial and temporal scaling of subcanopy radiation statistics, and to develop parameterizations of those statistics. Data from aerial photography and lidar (light detection and ranging) scanning of a coniferous forest with areas of varying canopy density and uniformity are used, as described in the next section. Crowns are delineated in the photograph to map the location and crown diameter of each tree, and tree heights are assigned from lidar elevation returns. A spatially explicit model that uses these data to simulate transmission of solar radiation to the forest floor is developed in section 3; the complex pattern of transmission through canopy gaps is explicitly represented, but, for numerical efficiency and to minimize the number of parameters required, a very simple scheme is used for transmission through crowns. Model results are compared with ground-based hemispherical photography and distributed measurements of radiation under the canopy on clear and cloudy days in section 4. Because the spatially explicit model is too computationally expensive to run for large areas or long times, efficient parameterizations of radiation statistics are sought in section 5. Finally, section 6 presents conclusions and discusses future plans.

2. Site and data description

The Cold Land Processes Experiment (CLPX) was conducted in Colorado during the winters of 2002 and 2003. Data used in this study were obtained at the Local Scale Observation Site (LSOS; Hardy et al. 2004, 2007, manuscript submitted to J. Hydrometeor.), which was within the U.S. Forest Service Fraser Experimental Forest [39.9°N, 105.9°W, 2780 m above sea level (ASL)] and is shown by the color infrared orthophotograph in Fig. 1a. A clearing separates two stands of contrasting structure. To the south of the clearing, there is a uniform lodgepole pine plantation; from manual
surveying, the trees have an average height of 12.6 m with standard deviation 2.4 m. To the north of the clearing, there is a discontinuous mixed-age stand, predominantly of lodgepole pine but with some subalpine fir and Engelmann spruce; the average tree height is 9.3 m and the standard deviation is 4.9 m. The histograms in Fig. 2 show that the tree heights have an approximately normal distribution for the uniform stand but a bimodal distribution of short and tall trees for the discontinuous stand.

Solar radiation was measured beneath the uniform and discontinuous canopies within the areas shown by boxes in Fig. 1b with two radiometer arrays (Link et al. 2004; Pomeroy et al. 2008, hereafter POM), each consisting of 10 Eppley pyranometers (0.3–3-μm wavelength, 160° sky view, 5% accuracy). Figure 3 shows 5-min averages of 10-s measurements from each array for days 84 and 85 (24 and 25 March) in 2003. Also shown is the above-canopy radiation measured by a radiometer mounted at a height of 18 m on a mast in a clearing 200 m to the southwest of the study area. Day 84 was clear, with strong direct illumination in open...
areas, whereas day 85 was overcast. Averages and standard deviations across the arrays are larger for the discontinuous stand than the uniform stand and larger for the clear day than the overcast day.

Hemispherical photographs were taken at points on a staggered 20-m grid (Melloh et al. 2003); example photographs from the discontinuous stand, the clearing, and the uniform stand at the points marked by crosses in Fig. 1b are shown in Fig. 4, overlain with the sun track for day 84. These photographs were used by Melloh et al. (2003) to study gap fraction distributions and by Hardy et al. (2004) to model transmission of solar radiation through the canopy with the Gap Light Analyzer software package (Frazer et al. 1999).
Before delineation of the orthophotograph to identify individual tree crowns, forest and nonforest classes have to be discriminated. Because the radiative properties of snow and vegetation differ strongly, the normalized difference vegetation index (NDVI) between the near-infrared (NIR) and red bands of the photograph,

$$\text{NDVI} = \frac{\text{NIR} - \text{RED}}{\text{NIR} + \text{RED}},$$

is found to give good discrimination between tree crowns and areas of sunlit or shaded snow, as shown in Fig. 1b. By varying the threshold for discrimination across the image by an image segmentation procedure using the local standard deviation, smaller crowns that are increasingly confused with snow because of reflection from ground beneath the canopy can be identified while providing good definition of the forest boundary in denser areas.

Four main techniques have been developed for automatic crown delineation in images: valley following (Gougeon 1995), pattern matching (Pollock 1996), crown centroid identification (Culvenor 2002), and wavelet analysis (Strand et al. 2006). The crown centroid method used here is described by Bunting and Lucas (2006). Local maxima in NDVI are identified as crown centers and expanded to minima to form crown edges. A classification procedure identifies and removes objects identified as complete crowns, and the remaining objects are further split until all objects are classified as crowns or a maximum number of iterations has been reached. Finally, correction procedures to identify and merge oversplit crowns are used to produce the final result. The method has been particularly successful in identifying crowns of varying size and shape, achieving accuracies of 70% for complex mixed species forests in Australia. Although the LSOS stands are relatively homogeneous in crown shape and size, many crowns overlap or have interlocking branch structures. Compared with many other algorithms that leave a pixel-wide gap between crowns, it is believed that the algorithm used here is more robust for overlapping crowns.

The CLPX lidar data have an approximately 1.5-m horizontal spacing and were supplied filtered into ground and vegetation elevation returns (Miller 2003). The ground returns were triangulated and interpolated onto a regular grid to form a digital elevation model, but the site is nearly level; surface elevations for the area shown in Fig. 1 only increase by 2 m from the southwest corner to the northeast corner. Surface heights were subtracted from the vegetation returns to generate the map of vegetation heights shown in Fig. 5. Histograms of lidar heights for trees in the manually mapped areas of the uniform and discontinuous stands are plotted in Fig. 2. Compared with the ground survey results, the average tree height is underestimated in the uniform stand and the short trees in the discontinuous stand are underrepresented, but the histogram shapes are similar. Lidar can miss small trees and can underestimate the height of a tree if the highest point is not sampled or if the laser penetrates some distance into the canopy before being reflected; methods have been developed to correct for this (Magnussen et al. 1999), but the lidar elevation data are used here without adjustment.

3. Model development

The model developed here represents individual trees as geometric primitives to allow analytic calculations of pathlengths for radiation beams passing through the canopy. This approach has been used in several other models (e.g., Satterlund 1983; Li et al. 1995; Song and Band 2004), but the actual implementation used here is based on Price (1997). Trees are assumed to have ellipsoidal canopies and cylindrical trunks; the pathlength calculation for a single tree is shown schematically in Fig. 6. A ray from point \((x_s, y_s)\)
on the surface in the direction of the sun is defined by the parametric vector

\[ r(l) = (x_t + l \cos \theta \sin \phi, y_t - l \cos \theta \cos \phi, l \sin \theta), \]

where \( l \) is the distance from the surface, \( \theta \) is the solar elevation, and \( \phi \) is the solar azimuth, measured anti-clockwise from south by convention. For a tree at point \((x, y)\) with height \( h\), crown radius \( r_c\), and canopy base height \( h_b\), the crown surface is defined by the solutions of the equation

\[ \frac{(x - x_t)^2}{r_c^2} + \frac{(y - y_t)^2}{r_c^2} + \frac{(z - h + r_v)^2}{r_v^2} = 1, \]

where \( r_v = (h - h_b)/2 \) is the vertical half axis of the crown ellipsoid. Substituting Eq. (2) into Eq. (3) to find the points at which the ray intersects the crown gives a quadratic equation:

\[ a l^2 + bl + c = 0, \]

where

\[ a = \frac{\cos^2 \theta}{r_c^2} + \frac{\sin^2 \theta}{r_v^2}, \]

\[ b = \frac{2 \cos \theta (x_t - x_e) \sin \phi - (y_t - y_e) \cos \phi}{r_c^2} + \frac{2 \sin \theta (r_v - h)}{r_v^2}, \]

and

\[ c = \frac{(x_t - x_e)^2 + (y_t - y_e)^2}{r_c^2} + \frac{(r_v - h)^2}{r_v^2} - 1. \]

The ray intersects the crown if and only if \( D = b^2 - 4ac > 0 \). The pathlength through the crown is then \( l_c = a^{-1}D^{1/2} \), and the total pathlength is found by summing the pathlengths through all crowns that the ray intersects.

Points in the shade of a cylindrical trunk can be found by replacing \( r_v \) with trunk radius \( r_t \) and deleting terms involving \( r_v \) in Eqs. (5)–(7), rejecting solutions with intersection heights lying outside the range \([0, h]\). Trunks and canopy elements are assumed to be opaque, and multiple scattering within the canopy or between the canopy and the ground are neglected as a first approximation, but light can pass through gaps within the canopy. Following Nilson (1971), the probability that a beam will pass through the canopy without interception is

\[ p_t = \exp[-G(\theta) \Sigma \lambda l_i], \]

where \( G \) is a projection function determined by the orientation of canopy elements, \( \lambda \) is the effective foliage area density, and the summation is over all crowns that the beam intersects. Random orientations are assumed, for which \( G = 0.5 \). Foliage area and crown volume could, in principal, be measured by lidar, but this requires a relationship with the density of ground returns from under the canopy to be developed (Riaño et al. 2004). Ground measurements are used here instead. Kaufmann et al. (1982) measured leaf areas for lodgepole pine at Fraser and obtained an allometric relationship with tree height; dividing by the volume of an ellipsoidal crown gives

\[ \lambda = \frac{2.925 h^2}{4 \pi r_c r_t}. \]

The effective value of \( \lambda \) in Eq. (8) is increased by woody material in the canopy but decreased by clumping of canopy elements (Chen et al. 1997); lacking sufficient information for lodgepole pine, Eq. (9) is used without adjustment.

Crown radii and centers are found by delineation of the orthophotograph, as described above. The tree height is taken to be given by the highest lidar elevation within the crown profile, without correction. Trunk radii and canopy base heights cannot be directly determined from the above-canopy measurements. Instead, allometric relationships obtained from manual measurements of 198 trees in the LSOS area are used. Regression against tree height gives \( r_t = 0.01 h^{1.15} \) \((r_t^2 = 0.81, \text{rms error 0.04 m})\) and \( h_b = 0.02 h^{1.86} \) \((r_b^2 = 0.64, \text{rms error 1.59 m})\).

Because rays are traced from the ground surface upward in the direction of the sun, sloping surfaces can easily be included in an extension of the model; topography has important influences on radiative transfer through canopies (Melloh et al. 2003; Liu et al. 2004).
but the site considered here is level. The ellipsoidal
crowns can be replaced by conical or parabolic canopies;
more general geometric shapes (Sheng et al. 2001)
or realistic crown shape models could also be used, but
analytic solutions for the pathlength are then no longer
available and the computational expense is greatly in-
creased.

To generate sun flecks within a tree shadow, rather
than a homogeneous shadow, $p_{t}$ is taken to be a random
variable with values of 0 or 1 and average given by Eq.
(8). In general, the downward radiation at a point $(x, y)$
on the surface is

$$S_{d}(x, y) = \frac{1}{\pi} \int_{0}^{2\pi} d\phi \int_{\theta_{b}(\phi)}^{\pi/2} S_{0}(\theta, \phi) p_{t}(x, y; \theta, \phi) \times \sin\theta \cos\theta \, d\theta,$$

(10)

where $S_{0}(\theta, \phi)$ is the radiation from elevation $\theta$ and
azimuth $\phi$ above the canopy, $p_{t}(x, y; \theta, \phi)$ is the prob-
ability of transmission through the canopy from that
direction, and $\theta_{b}(\phi)$ is the elevation angle of the hori-
zon, which can be calculated from the DEM (Dozier
and Frew 1990). Two assumptions are made to simplify
the evaluation of Eq. (10): taking diffuse radiation from
the sky to be isotropic and treating the sun as a point
source gives

$$S_{d}(x, y) = v(x, y) S_{\text{dif}} + p_{t}(x, y; \theta, \phi) S_{\text{dir}},$$

(11)

where $S_{\text{dif}}$ is the diffuse component of the above-
canopy radiation, $S_{\text{dir}}$ is the direct component, and

$$v(x, y) = \frac{1}{\pi} \int_{0}^{2\pi} d\phi \int_{\theta_{b}(\phi)}^{\pi/2} p_{t}(x, y; \theta, \phi) \sin\theta \cos\theta \, d\theta$$

(12)

is the sky-view factor, which is evaluated by numerical
integration with values of $p_{t}$ provided by the model.

Separate measurements of diffuse radiation above
the canopy were not made, so it is estimated by the
empirical method of Erbs et al. (1982). First, atmo-
spheric transmissivity is found by dividing the above-
canopy radiation by the radiation at the top of the at-
mosphere, giving

$$k_{t} = \frac{S_{0}}{I_{0} \sin\theta},$$

(13)

where $I_{0} = 1367$ W m$^{-2}$ is the solar constant. The dif-
fuse radiation is then estimated as $S_{\text{dif}} = dS_{0}$, with

$$d = \begin{cases} 
1 - 0.09k_{t} \\
0.95 - 0.16k_{t} + 4.39k_{t}^{2} - 16.64k_{t}^{3} + 12.34k_{t}^{4} \\
0.165 
\end{cases}$$

(14)

Direct radiation is the remainder $S_{\text{dir}} = S_{0} - S_{\text{dif}}$.

4. Results

Figure 7 shows simulations of tree shadows for the
time at which the orthophotograph in Fig. 1 was taken
[1400 local standard time (LST) 8 April] and sky-view
factors, which are independent of time. There is good
subjective similarity between Figs. 1a and 7a, although
the shadows of isolated trees show that the ellipsoidal
crowns in the simulation are a little too rounded. Close
inspection suggests that the delineation tends to over-
segment the canopy in denser areas, giving too many
trees and too great a canopy coverage.

The sky view in Fig. 7b shows both small-scale vari-
bility within stands and the large-scale structure of
stands and gaps. Hemispherical sky views can be simu-
lated by dividing the sky hemisphere into azimuth and
elevation cells and blanking out cells that are ob-
structed by the canopy according to the model; Melloh
et al. (2003) previously did this for LSOS using manual
inventory maps and a tree model. Simulated hemi-
spherical images and differences between sky masks
obtained from simulations and photographs were in-
cluded in Fig. 4 for comparison with the photographs.
There are some evident errors in tree positions, heights,
and shapes, and the gaps between trees are too small in
the uniform stand, but the broad patterns are in good
agreement. Simulated sky-view factors are scattered
against values obtained from the full set of hemispheri-
cal photographs in Fig. 8; error bars for uncertainty in
the registration of measurement points within the
model were estimated by displacing the simulation
points by 2 m in each of the cardinal directions, and
error bars for uncertainty in creating sky masks from
the photographs were estimated by changing the
threshold brightness by ±10%. The overall agreement
is good, with bias −0.02, rms error 0.09, and $r^{2} = 0.8$.
Most of the points at which the sky view is underesti-
imated are in the uniform stand.

The model was run on a 1-m grid for days 84 and 85
with a 5-min time step, and statistics were calculated for
the 20 m × 20 m areas within which the radiometer
arrays were deployed. The measurements sample too
few points to calculate histograms of subcanopy radiation, but they can be used to calculate cumulative distributions giving fractions of the surface receiving less than some specified amount of radiation. Cumulative distributions at noon on clear-sky day 84 are shown in Fig. 9 for simulations and measurements in the uniform and discontinuous stands. The distributions can be expected to be highly bimodal on clear days, with some radiometers in direct sun and others shaded, and this gives sills that are evident in the measured and simulated distributions. The height of the sill corresponds to the fraction of the forest floor in shade, which is simulated as 75% for the uniform stand and 55% for the discontinuous stand. Because of the bimodal nature of the distributions, standard error estimates based on normal distributions are inappropriate. Instead, 90% confidence limits for the measured distributions were estimated by generating a large number of 10-point random samples from the simulated radiation distributions; these are shown by dotted lines on Fig. 9. The agreement between the simulation and measurements is good for the discontinuous stand, but the simulation underestimates the radiation in both sunlit and shaded fractions of the uniform stand, consistent with the underestimate of sky view noted above. Although it might be expected from the conclusions of Pinty et al. (2004) that radiation would be harder to simulate in the discontinuous stand, it turns out that it is harder to delineate the tree crowns accurately in the denser, more uniform parts of the canopy.

Fig. 7. (a) Simulated tree shadows and (b) sky-view factors for the area shown in Fig. 1.

Fig. 8. Sky-view factors simulated by the model and calculated from hemispherical photographs; crosses show points in open areas and the discontinuous stand, and diamonds show points in the uniform stand. Vertical bars give the range of values obtained by displacing the simulation points by 2 m in each of the cardinal directions, and horizontal bars give the range of values obtained by varying the brightness threshold applied to the photographs by ±10%.
Averages and standard deviations from the array measurements are compared with simulations in Fig. 10, and simulated 90% confidence intervals on the statistics for random 10-point samples are also shown. The average is underestimated for the discontinuous stand and the standard deviation is overestimated for the uniform stand on day 85 before noon, but the measurements generally lie within the confidence intervals on the simulation results. The simulated statistics are smoother than the measured statistics because some of the spatial variability appears as temporal variability when a moving pattern with high spatial variability is sampled. Confidence intervals on 5-min averages for 10-radiometer arrays turn out to be quite broad as a result. Figure 11 shows how simulated confidence intervals on sample averages tighten with increasing sample size for 5-min and daily averages. Both scale with $N^{-1/2}$ as expected, but many more radiometers are required to estimate 5-min averages with the same confidence as daily averages.

Because patches of sunlight on the forest floor move during the day, it can be expected that the standard deviation of solar radiation will decrease if the averaging period is increased. For the same sites considered here but a different period, POM investigated how measured coefficients of variation (CV) scale with averaging period. Figure 12 shows CVs calculated from array data averaged over periods from 5 min to 12 h centered on noon of clear-sky day 84. As noted by POM, the CV is greater for the uniform stand than the discontinuous stand over short intervals but decreases more rapidly as the averaging period is increased. Simulated CVs show the same qualitative behaviors, but the decrease in CV for the uniform stand is less dramatic in the simulation than in the measurements; this is because the average is lower and the standard deviation is higher in the simulated daily radiation. CVs for overcast days (not shown) have much less dependence on temporal averaging.

Standard deviations are plotted against averages in Fig. 13 for clear and overcast conditions, discriminated here as periods with diffuse radiation fraction $d < 0.17$ and $d > 0.9$, respectively. POM found the measured standard deviation to be a linear function of average radiation under overcast conditions, and the simulation produces the same behavior. For clear conditions, a nonlinear relationship is observed and simulated, with decreasing rates of change in standard deviations at higher averages. The simulation for the discontinuous stand shows hysteresis because of the greater openness to the southeast of this area than to the southwest.

5. Parameterization of radiation statistics

From Eq. (11), the average and variance of subcanopy radiation are

$$S \downarrow = \overline{S}_{\text{diff}} + \overline{p}_t S_{\text{dir}}$$

and

$$\sigma_S^2 = \sigma_c^2 S_{\text{diff}}^2 + \sigma_p^2 S_{\text{dir}}^2 + 2 \text{cov}(u, p)_t S_{\text{diff}} S_{\text{dir}},$$

where overbars denote spatial averages, $\sigma_p^2 = \overline{p}_t (1 - \overline{p}_t)$ is the variance of $p_t$, $\sigma_c^2$ is the variance of $v$, and...
cov(υ, pt) is their covariance. Equation (12) gives the covariance as an integral over the autocorrelation of the transmissivity. This autocorrelation is an important quantity related to the bidirectional reflectance of a forest scene and warrants further investigation, but neglecting covariance between sky view and transmission simplifies the parameterization of Eq. (16). The coefficient of variation is then given by

$$\text{CV} = \frac{\sigma^2 d + \bar{p}_t(1 - \bar{p}_t)(1 - d)}{\bar{u}d + \bar{p}_t(1 - d)},$$  \hspace{1cm} (17)$$

where $d$ is the diffuse fraction from Eq. (14) or measurements. This predicts that the CV should have a constant value of $\sigma_u/\bar{u}$ for overcast conditions and decrease with increasing transmission for clear conditions, as noted in the previous section for both observations and simulations.

A parameterization is required for $p_t$. With the assumption of opaque canopy elements, $p_t$ for a particular elevation is equal to the gap fraction at that elevation, which can be measured from real or simulated hemispherical images. Azimuthal averages of simulated gap

Fig. 10. (top) Averages and (bottom) std dev of subcanopy solar radiation from array measurements (black lines) and simulations (gray lines) for (left) uniform and (right) discontinuous stands. Dotted lines show simulated 90% confidence intervals for random 10-point samples.
fractions for the uniform stand, the discontinuous stand, and a 10 m × 10 m area in the middle of the clearing are shown in Fig. 14. It is found that Beer’s law, 

\[ p_t(\theta) = \exp \left( -\frac{g(\theta)}{\cos \theta} \right) \]  

with the apparent foliage projection function \( g \) given by the parametric form 

\[ g(\theta) = a + b \sin \theta + c \cos \theta, \]  

fits the modeled gap fractions closely for the parameter values given in Table 1. The value of \( p_t \) at \( \theta = 90^\circ \) gives the canopy openness; for the clearing, Eq. (18) has to be limited to give \( p_t \approx 1 \).

Substituting Eq. (18) into Eq. (12), the sky-view statistics could be expressed in terms of elliptic integrals (Nijssen and Lettenmaier 1999). The simpler approach of taking values from the simulation, given in Table 1, is used here. Equations (15) and (16) are compared with observations and simulations in Fig. 13. The parameterizations match the statistics of the spatially ex-

Fig. 11. Simulated 90% confidence intervals on estimates of spatial averages for varying sample sizes and 5-min (diamonds) or daily (crosses) temporal averaging for the (a) uniform and (b) discontinuous stands. The fitted lines are \( N^{-1/2} \) power laws.

Fig. 12. Coefficients of variation in subcanopy radiation averaged over varying periods centered on noon of clear-sky-day 84 for the (a) uniform and (b) discontinuous stands from array measurements (solid lines) and simulations (dashed lines). Dotted lines show simulated 90% confidence intervals for random 10-point samples.
explicit model well but do not reproduce the clear-sky hysteresis for the discontinuous stand; hysteresis could be represented at the expense of replacing the constant parameters in Eq. (19) with functions of azimuth.

6. Conclusions and discussion

An orthophotograph and lidar elevations were used to map the location, height, and crown diameter of coniferous trees in an area of varying canopy density and structure. The resulting map, along with above-canopy measurements of incoming solar radiation and an estimation of the diffuse fraction, was used in a spatially explicit model of the transmission of direct and diffuse radiation to the surface beneath the canopy. Spatial statistics of simulated subcanopy radiation were compared with radiometer array measurements. The simulation was better for a discontinuous stand than for a uniform stand; discrepancies can largely be attributed to an overestimate of canopy cover in the denser areas.

Confidence intervals for sample statistics were estimated by repeated sampling of the model output; these turn out to be rather broad for 5-min averages with a 10-radiometer array, but are greatly reduced when

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**Fig. 13.** Std dev plotted against average for subcanopy solar radiation in the (left) uniform and (right) discontinuous stands under (top) clear and (bottom) overcast conditions. Diamonds show measurements, crosses show simulations, and lines show parameterizations.
Daily average statistics are considered. The standard deviation in subcanopy radiation decreases as the averaging period is increased, and decreases more rapidly for the uniform stand than the discontinuous stand.

Efficient parameterizations for the spatial average and standard deviation of subcanopy solar radiation were derived from the spatially explicit model. Five parameters were used in addition to above-canopy radiation and solar elevation inputs: the average and standard deviation of the sky-view factor under a stand, and three parameters fitted to the gap fraction. These were taken from model simulations, but could equally well be obtained with hemispherical photography. For application on larger scales, it may be possible to relate the parameters to more readily available canopy measures by applying the model to a wide range of canopy types. All of the parameters have physical meaning; the average and standard deviation of sky view are strongly related to the average and standard deviation of transmission for diffuse radiation, and the gap fraction parameters can be regarded as the first three terms in a Fourier expansion of the apparent foliage projection function.

In future work, we intend to extend the model to include thermal radiation and use it to investigate the spatial variation of snowmelt beneath forest canopies (Faria et al. 2000; Woo and Giesbrecht 2000). The model will be run with a range of real and synthetic stand maps and slopes to investigate how subcanopy radiation statistics scale with canopy characteristics and topography. Further consideration will be given to methods of mapping canopy structure using photography and lidar; as lidar may underestimate tree heights because of the probability of the laser beam penetrating some distance into the canopy, and the model simulates the probability of radiation penetrating the canopy, it may be possible to use the model to assimilate lidar data.

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TABLE 1. Parameter values fitting Eq. (18) to gap fractions and statistics of sky view used in parameterizations of radiation statistics.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Uniform</th>
<th>Discontinuous</th>
<th>Clearing</th>
</tr>
</thead>
<tbody>
<tr>
<td>(a)</td>
<td>-0.48</td>
<td>-0.16</td>
<td>1.6</td>
</tr>
<tr>
<td>(b)</td>
<td>1.2</td>
<td>0.48</td>
<td>-0.96</td>
</tr>
<tr>
<td>(c)</td>
<td>0.88</td>
<td>0.48</td>
<td>-1.28</td>
</tr>
<tr>
<td>(\psi)</td>
<td>0.25</td>
<td>0.45</td>
<td>0.83</td>
</tr>
<tr>
<td>(\sigma_\psi)</td>
<td>0.059</td>
<td>0.142</td>
<td>0.021</td>
</tr>
</tbody>
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